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A COMPUTER MODEL INVESTIGATION
OF A
HALF SQUARE LOG-PERIODIC ARRAY

by

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December 1987

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A Computer Model Investigation of A Half Square Log-Periodic Array

by

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ABSTRACT

This thesis investigates the potential of a half square log-periodic array for use by the military over the frequency range of 2 to 30 MHz using a computer simulation technique by numerical methods. Using the Numerical Electromagnetics Code (NEC), a selected model was run in free space and over perfect ground to obtain data for radiation patterns and element currents on the array. After the evaluation of the NEC data, the results of the investigation show that half square log-periodic array with dual feed and switched transmission line has characteristics of a successful log-periodic structure with a unidirectional radiation pattern, over the design frequency range of 2 to 30 MHz, showing promise for military applications.

TABLE OF CONTENTS

I. INTRODUCTION 11

A. THE EMERGENCE OF A HALF SQUARE LOG-PERIODIC ARRAY 11

B. BROADBAND ANTENNAS 12

C. THE FREQUENCY INDEPENDENT CONCEPT AND LOG-PERIODIC ANTENNAS 12

D. GENERAL CHARACTERISTICS OF SUCCESSFUL LOG-PERIODIC ANTENNAS 16

II. NUMERICAL CONSIDERATIONS AND PROCEDURE 18

A. SELECTED METHOD OF INVESTIGATION 18

B. NUMERICAL ELECTROMAGNETICS CODE (NEC) 19

C. DEVELOPMENT OF THE COMPUTER MODEL 19

D. FAR-FIELD RADIATION PATTERNS 21

III. EXPERIMENTAL RESULTS 24

A. RADIATION PATTERNS 24

B. AMPLITUDE AND PHASE DISTRIBUTIONS OF ELEMENT CURRENTS 25

IV. CONCLUSIONS AND RECOMMENDATIONS 30

A. CONCLUSIONS 30

B. RECOMMENDATIONS 31

APPENDIX A: NEC DATA FILE FOR FREE SPACE 32

APPENDIX B: NEC DATA FILE FOR PERFECT GROUND 35

APPENDIX C: RADIATION PATTERNS IN FREE SPACE 38

APPENDIX D: RADIATION PATTERNS OVER PERFECT GROUND 72

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APPENDIX E: AMPLITUDE AND PHASE PLOTS IN FREE SPACE 88

APPENDIX F: AMPLITUDE AND PHASE PLOTS OVER PERFECT GROUND 122

LIST OF REFERENCES 156

INITIAL DISTRIBUTION LIST 157

LIST OF TABLES

1. HLPA DESIGN PARAMETERS 23
2. NUMERICAL RESULTS IN FREE SPACE 27
3. NUMERICAL RESULTS OVER PERFECT GROUND 29

LIST OF FIGURES

1.1 Log-periodic toothed structure (self complementary) 14
1.2 Log-periodic dipole construction 15
2.1 Half Square Log-Periodic Array 22
3.1 Horizontal Pattern, Frequency: 9.60 MHz 26
3.2 Horizontal Pattern, Frequency: 13.61 MHz 28
C.1 Horizontal Pattern, Frequency: 2 MHz 38
C.2 Horizontal Pattern, Frequency: 2.38 MHz 39
C.3 Horizontal Pattern, Frequency: 2.83 MHz 40
C.4 Horizontal Pattern, Frequency: 3.37 MHz 41
C.5 Horizontal Pattern, Frequency: 4.01 MHz 42
C.6 Horizontal Pattern, Frequency: 4.78 MHz 43
C.7 Horizontal Pattern, Frequency: 5.69 MHz 44
C.8 Horizontal Pattern, Frequency: 6.77 MHz 45
C.9 Horizontal Pattern, Frequency: 8.06 MHz 46
C.10 Horizontal Pattern, Frequency: 11.43 MHz 47
C.11 Horizontal Pattern, Frequency: 13.61 MHz 48
C.12 Horizontal Pattern, Frequency: 16.20 MHz 49
C.13 Horizontal Pattern, Frequency: 19.29 MHz 50
C.14 Horizontal Pattern, Frequency: 22.96 MHz 51
C.15 Horizontal Pattern, Frequency: 27.34 MHz 52
C.16 Horizontal Pattern, Frequency: 30.0 MHz 53
C.17 Horizontal Pattern, Frequency: 2.15 MHz 54
C.18 Horizontal Pattern, Frequency: 2.60 MHz 55
C.19 Horizontal Pattern, Frequency: 3.0 MHz 56
C.20 Horizontal Pattern, Frequency: 3.7 MHz 57
C.21 Horizontal Pattern, Frequency: 5.0 MHz 58
C.22 Horizontal Pattern, Frequency: 5.95 MHz 59
C.23 Horizontal Pattern, Frequency: 6.5 MHz 60

C.24 Horizontal Pattern, Frequency: 7.0 MHz 61
C.25 Horizontal Pattern, Frequency: 7.5 MHz 62
C.26 Horizontal Pattern, Frequency: 8.25 MHz 63
C.27 Horizontal Pattern, Frequency: 8.5 MHz 64
C.28 Horizontal Pattern, Frequency: 8.75 MHz 65
C.29 Horizontal Pattern, Frequency: 9.0 MHz 66
C.30 Horizontal Pattern, Frequency: 9.25 MHz 67
C.31 Horizontal Pattern, Frequency: 9.5 MHz 68
C.32 Horizontal Pattern, Frequency: 9.75 MHz 69
C.33 Horizontal Pattern, Frequency: 10.0 MHz 70
C.34 Horizontal Pattern, Frequency: 10.5 MHz 71
D.1 Horizontal Pattern, Frequency: 2 MHz 72
D.2 Horizontal Pattern, Frequency: 2.38 MHz 73
D.3 Horizontal Pattern, Frequency: 2.83 MHz 74
D.4 Horizontal Pattern, Frequency: 3.37 MHz 75
D.5 Horizontal Pattern, Frequency: 4.07 MHz 76
D.6 Horizontal Pattern, Frequency: 4.78 MHz 77
D.7 Horizontal Pattern, Frequency: 5.69 MHz 78
D.8 Horizontal Pattern, Frequency: 6.77 MHz 79
D.9 Horizontal Pattern, Frequency: 8.06 MHz 80
D.10 Horizontal Pattern, Frequency: 9.60 MHz 81
D.11 Horizontal Pattern, Frequency: 11.43 MHz 82
D.12 Horizontal Pattern, Frequency: 16.20 MHz 83
D.13 Horizontal Pattern, Frequency: 19.29 MHz 84
D.14 Horizontal Pattern, Frequency: 22.96 MHz 85
D.15 Horizontal Pattern, Frequency: 27.34 MHz 86
D.16 Horizontal Pattern, Frequency: 30.0 MHz 87
E.1 Current Amplitude, Frequency : 2 MHz 88
E.2 Current Phase, Frequency : 2 MHz 89
E.3 Current Amplitude, Frequency : 2.38 MHz 90
E.4 Current Phase, Frequency : 2.38 MHz 91
E.5 Current Amplitude, Frequency : 2.83 MHz 92
E.6 Current Phase, Frequency : 2.83 MHz 93

E.7 Current Amplitude, Frequency : 3.37 MHz 94
E.8 Current Phase, Frequency : 3.37 MHz 95
E.9 Current Amplitude, Frequency : 4.01 MHz 96
E.10 Current Phase, Frequency : 4.01 97
E.11 Current Amplitude, Frequency : 4.78 MHz 98
E.12 Current Phase, Frequency : 4.78 MHz 99
E.13 Current Amplitude, Frequency : 5.69 MHz 100
E.14 Current Phase, Frequency : 5.69 MHz 101
E.15 Current Amplitude, Frequency : 6.77 MHz 102
E.16 Current Phase, Frequency : 6.77 MHz 103
E.17 Current Amplitude, Frequency : 8.06 MHz 104
E.18 Current Phase, Frequency : 8.06 MHz 105
E.19 Current Amplitude, Frequency : 9.6 MHz 106
E.20 Current Phase, Frequency : 9.6 MHz 107
E.21 Current Amplitude, Frequency : 11.43 MHz 108
E.22 Current Phase, Frequency : 11.43 MHz 109
E.23 Current Amplitude, Frequency : 13.61 MHz 110
E.24 Current Phase, Frequency : 13.61 MHz 111
E.25 Current Amplitude, Frequency : 16.2 MHz 112
E.26 Current Phase, Frequency : 16.2 MHz 113
E.27 Current Amplitude, Frequency : 19.29 MHz 114
E.28 Current Phase, Frequency : 19.29 MHz 115
E.29 Current Amplitude, Frequency : 22.96 MHz 116
E.30 Current Phase, Frequency : 22.96 MHz 117
E.31 Current Amplitude, Frequency : 27.34 MHz 118
E.32 Current Phase, Frequency : 27.34 MHz 119
E.33 Current Amplitude, Frequency : 30.0 MHz 120
E.34 Current Phase, Frequency : 30.0 MHz 121
F.1 Current Amplitude, Frequency : 2 MHz 122
F.2 Current Phase, Frequency : 2 MHz 123
F.3 Current Amplitude, Frequency : 2.38 MHz 124
F.4 Current Phase, Frequency : 2.38 MHz 125
F.5 Current Amplitude, Frequency : 2.83 MHz 126

F.6 Current Phase, Frequency : 2.83 MHz 127
F.7 Current Amplitude, Frequency : 3.37 MHz 128
F.8 Current Phase, Frequency : 3.37 MHz 129
F.9 Current Amplitude, Frequency : 4.01 MHz 130
F.10 Current Phase, Frequency : 4.01 131
F.11 Current Amplitude, Frequency : 4.78 MHz 132
F.12 Current Phase, Frequency : 4.78 MHz 133
F.13 Current Amplitude, Frequency : 5.69 MHz 134
F.14 Current Phase, Frequency : 5.69 MHz 135
F.15 Current Amplitude, Frequency : 6.77 MHz 136
F.16 Current Phase, Frequency : 6.77 MHz 137
F.17 Current Amplitude, Frequency : 8.06 MHz 138
F.18 Current Phase, Frequency : 8.06 MHz 139
F.19 Current Amplitude, Frequency : 9.6 MHz 140
F.20 Current Phase, Frequency : 9.6 MHz 141
F.21 Current Amplitude, Frequency : 11.43 MHz 142
F.22 Current Phase, Frequency : 11.43 MHz 143
F.23 Current Amplitude, Frequency : 13.61 MHz 144
F.24 Current Phase, Frequency : 13.61 MHz 145
F.25 Current Amplitude, Frequency : 16.2 MHz 146
F.26 Current Phase, Frequency : 16.2 MHz 147
F.27 Current Amplitude, Frequency : 19.29 MHz 148
F.28 Current Phase, Frequency : 19.29 MHz 149
F.29 Current Amplitude, Frequency : 22.96 MHz 150
F.30 Current Phase, Frequency : 22.96 MHz 151
F.31 Current Amplitude, Frequency : 27.34 MHz 152
F.32 Current Phase, Frequency : 27.34 MHz 153
F.33 Current Amplitude, Frequency : 30.0 MHz 154
F.34 Current Phase, Frequency : 30.0 MHz 155

I. INTRODUCTION

A. THE EMERGENCE OF A HALF SQUARE LOG-PERIODIC ARRAY

In order to meet military communications needs, today's military uses a wide variety of communication systems. Military high frequency (HF) communication systems provide different kinds of short, medium, and long range communications capability. The users of military HF communications vary from special teams to high level headquarters. These different requirements necessitate finding a solution to meet all these needs. In this respect, major important design factors for a military HF antenna are a frequency range of 2 to 30 MHz and practicability; that is the ease of deployment of the antenna under the combat conditions.

To meet these requirements, D.V. Campbell and his associates at Fort Monmouth, New Jersey designed a lightweight wire array consisting of half square elements arranged in a log-periodic configuration with dual feed. A prototype of the half square log-periodic antenna was constructed at Fort Monmouth for testing at a frequency range of 8 to 30 MHz. Test results gave an impedance behavior common to a log-periodic antenna thus warranting further investigation. [Ref. 1]

J.R. Johnsen, in his thesis research [Ref. 2] investigated near magnetic fields of a uniformly periodic half square array with dual feed in order to be able to determine the potential of the structure as a half square log-periodic array (HLPA) for use by the military. Taking 2 to 30 MHz as the design frequency range for his model, Johnsen chose 8 MHz as mid-frequency resonance (which is 2 octaves above the lowest and almost 2 octaves below the highest frequency). He modeled a uniformly periodic half square array of 10 elements with double feed. Using the Numerical Electromagnetics Code (NEC) [Ref. 3] he simulated the model on the computer for free space and perfect ground environments with in-phase and anti-phase feed options to obtain data for near magnetic fields and radiation patterns. After collecting the data for near magnetic fields, Johnsen used these data to obtain the k-β relationship of the array. By inspecting the k-β diagrams he tried to identify the frequency regions where backward radiation occurred. Since backward radiation is an important characteristic of successful log-periodic antennas, he ran the model on the computer for the frequencies for which backward radiation on the k-β diagram was observed and obtained radiation

patterns. The results of his research led to the conclusion that the potential of designing a successful half square log-periodic antenna with dual feed is good.

The purpose of this thesis is to model a half square log-periodic antenna (HLPA) for different scaling and spacing factors and by using a computer simulation technique to investigate the characteristics of the antenna in order to be able to determine its applicability as a broadband military HF antenna.

B. BROADBAND ANTENNAS

In many applications an antenna must operate effectively over a wide range of frequencies. Generally an antenna with wide bandwidth is referred to as a broadband antenna. In this sense the term " broadband " is a relative measure of bandwidth and varies with the circumstances [Ref. 4]. In practice, a broadband antenna is considered to be the one which retains certain desired or specified radiation pattern, polarization, or impedance characteristics over more than an octave.

C. THE FREQUENCY INDEPENDENT CONCEPT AND LOG-PERIODIC ANTENNAS

The research work which led to the development of antennas whose performance is almost independent of frequency was carried out mainly at the University of Illinois in the period from 1955 to 1958. The work, along with several other projects was sponsored by the Air Force in order to relieve the problems associated with the increasing numbers of different electromagnetic systems and equipment being carried on high-speed military aircraft. So many different antennas were required that finding locations for the antennas was a serious problem. It was recognized that the problem would be relieved if a given antenna could serve several systems and frequencies, and consequently the Air Force sponsored a research program on the general subject of broadband antennas.

In connection with the sponsored research work on broadband antennas, Professor V.H. Rumsey, then antenna laboratory director at the University of Illinois realized that the features which introduce frequency dependence are the characteristic lengths of the structure. Antenna performance is generally a function of length/wavelength. On the other hand, by the principle of modeling or scaling, to ensure that a given type of structure has the same performance at different frequencies, it is only necessary to scale the size of the structure in the ratio of frequencies. Thus, Rumsey concluded that the structural feature required for frequency independent

operation is the absence of characteristic lengths. With this feature a structure could be self-scaling. But what kind of physical structure is there that has no characteristic lengths ? Rumsey's answer was that the structure should be completely described by angles. Thus he put forward the "angle concept," which said, essentially, that a structure whose shape is defined by angles alone, with no characteristic length, should be a frequency-independent structure.

In looking for structures that can be defined by angles alone, the first that come to mind are the infinite biconical antenna and the infinite bifin (bow-tie) antenna. However, practical versions of these structures are obviously finite in size, and although these structures do have comparatively broadband tendencies, the truncation to a finite size introduces a characteristic length and this destroys the frequency-independent behavior. [Ref. 5]

Next, R.H. DuHamel (then a research assistant professor at the University of Illinois) continued with the design of a broadband antenna with linear polarization. He realized that the bifin or bow-tie antenna could be constructed in a self complementary fashion and of course that it radiates linear polarization. But he also realized that the bandwidth of the bifin was limited because of the truncation, or more particularly, because the currents were not negligible at the point of truncation. Consequently, the problem was to somehow alter the bow-tie structure in such a way as to cause the currents to fall off with distance from the feed point more rapidly than usual. His method of accomplishing this was to introduce discontinuities, for example, teeth, into the fins in an attempt to increase the radiation and speed up the decay of current. But the question was,"How should the teeth be designed?" DuHamel decided to adhere to Rumsey's angle concept and to cut the teeth along circular arcs and let the length of the arcs be determined by an angle (see Figure 1.1).

However, this did not fix the tooth spacing, since the latter could not be specified by angles alone. In trying to solve the spacing problem, DuHamel noticed that on the equiangular structure (a successful structure), along a line drawn from the center outward, the spacings from one conductor to the next were in a constant ratio. He therefore considered spacing the teeth in the bifin such that the spacings were in a constant ratio. He accomplished this by choosing the radii of the circular arcs forming the corresponding parts of the successive teeth such that they were in a constant ratio, $R_{n+1} / R_n = \tau$. He recognized that the structure would not necessarily be frequency independent but that, on the other hand, the performance on an infinite structure

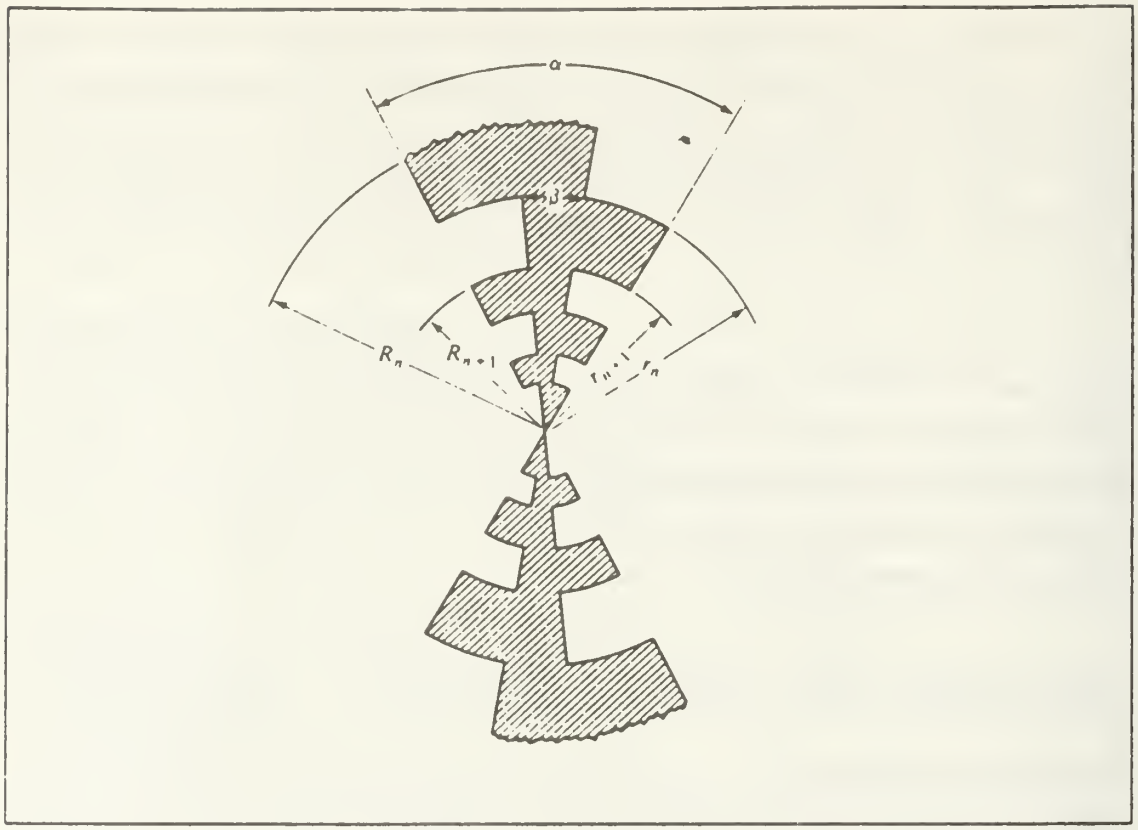

Figure 1.1 Log-periodic toothed structure (self complementary).

would be identical at a discrete number of frequencies. In fact, if the structure has a performance at frequency f_1, the performance should be identical at frequencies τf_1, $\tau^2 f_1$, $\tau^3 f_1$, and so on as long as the structure is modeled accurately at the feed point and is effectively infinite in size (i.e., current zero at the point of truncation). Again τ is the common ratio of distances. The frequencies at which the performance should be identical are related by the equation $f_n = f_{n+1}\tau$, or $\log f_{n+1} = \log f_n + \log (1/\tau)$. Inspection of this latter equation shows that the performance is a periodic function of the logarithm of the frequency (i.e., the frequencies at which the performance is the same are spaced equally when plotted on log paper). Thus, these types of structures were subsequently named *log-periodic* antennas.

After DuHamel's findings many structures of this type were built and tested. Some were less successful than others.

The next major step came with Isbell's invention of the log-periodic dipole array. His work was motivated by the desire to develop broadband arrays of more

conventional construction. Thus he decided to build and test an antenna array constructed of conventional wirelike elements; however, the length of the elements were determined by an angle α as before, and the spacings were such as to give the log-periodic type of behavior; that is successive distances between the apex and the elements were in a constant ratio, $R_{n+1} / R_n = \tau$ (Figure 1.2).

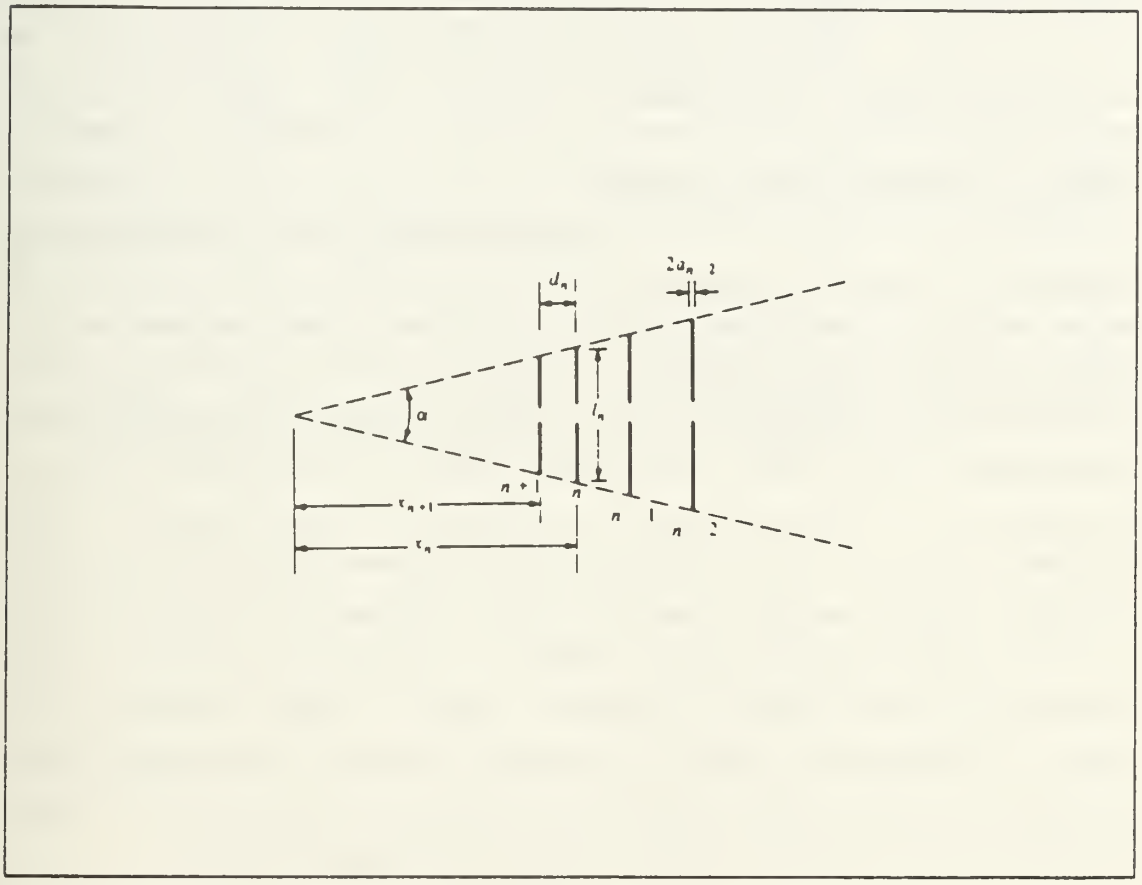

Figure 1.2 Log-periodic dipole construction.

The experiments with the structure demonstrated that in a certain range of values for τ and α, the structure was indeed a broadband log-periodic structure with a unidirectional pattern. Isbell also demonstrated experimentally that most of the radiation was coming from those dipole elements which were in the vicinity of a half wavelength long and that the currents and voltages at the large end of the structure were negligible within the operating band of frequencies. Finally, it was shown once again that the operating band of frequencies was bounded on the high side by frequencies corresponding to the size of the smallest elements and on the low side by the frequencies at which the largest dipole element is about a half wavelength long.

A careful and extremely valuable analysis of the log-periodic dipole array was made by R.L. Carrel in a doctoral dissertation. The physical makeup of the log-periodic array is such that an analysis of it may be based on more or less conventional theory of linear antennas and transmission lines. The main difficulty is the inherent complication. Carrel's analysis consisted of breaking the overall problem into parts, each of which was programmed for the digital computer. First, making the assumption that the element currents were sinusoidally distributed, he computed in the conventional way the mutual impedances between the dipole elements and the self-impedance of each element. In the second part of the problem, Carrel focused his attention on the parallel-wire transmission line, fed at one end shunt-loaded with impedances corresponding to the dipole antenna elements having sizes and spacings characteristic of log-periodic arrays; of course, the impedance values came from the first part of his computer program. He carried out (on a digital computer) a circuit analysis to find the input impedance, voltages, and the currents on the loaded transmission line, together with the base (i.e., input) currents at each antenna element. As the last part of the problem, with the specific values for the magnitude and phase of the currents in the antenna elements, he calculated the radiation patterns. Having developed a systematic computer program, Carrel completed calculations on more than 100 different log-periodic dipole designs. He then compared the results of several of these with corresponding experimental models. The measurements included not only impedances and radiation patterns but also the voltage and current distributions in the structure. The agreement between the computer output and the experimental results was excellent. Carrel's work provided a set of design curves which show how to adjust the dimensions of a structure in order to meet specified design objectives.

D. GENERAL CHARACTERISTICS OF SUCCESSFUL LOG-PERIODIC ANTENNAS

From the results of successful log-periodic antennas, some general characteristics can be cited as follows :

* Log-periodic antennas have a special kind of repetitiveness in their physical structure which results in a repetitive behavior of the electrical characteristics. The impedance is a logarithmically periodic function of frequency. That is, if a plot is made of the input impedance as a function of logarithm of the frequency, the variation will be periodic. Radiation patterns vary in the same manner, along with such parameters as the directive gain, beamwidth, and side-lobe level. [Ref. 6]
* Excitation of the antenna or array is from the high frequency or small end.

* Backfire radiation (in the case of unidirectional radiators) occurs, so that the antenna "fires" through the small part of the structure, with the radiation in the forward direction being zero or at least very small. For bidirectional antennas the backfire requirement is replaced by a requirement for broadside radiation. In any case the radiation in the forward direction along the surface of the antenna (which theoretically extends to infinity) must be zero or very small.
* A transmission region is formed by the inactive portion of the antenna between the feed point and the active region. This transmission line region should have the proper characteristic impedance and negligible radiation.
* An active region exists from which antenna radiates strongly because of a proper combination of current magnitudes and phasings. The position and phasing of these radiating currents produce a very small radiation field along the surface of the antenna or array in the forward direction, and a maximum radiation field in the backward direction.
* An inactive or reflection region exists beyond the active region. All successful frequency independent antennas must exhibit a rapid decay of current within and beyond the active region, so that operation will not be affected by truncation of the structure. A major cause of the rapid current decay is, of course, the large radiation of energy from the active region. [Ref. 7]

II. NUMERICAL CONSIDERATIONS AND PROCEDURE

A. SELECTED METHOD OF INVESTIGATION

The method of investigation of the Half Square Log-Periodic Array was planned in two steps. The first step was to design several computer models of the Half Square Log-Periodic Array with different scaling and spacing factors and to compare the performances of these models in terms of the antenna parameters, such as radiation patterns, half-power beamwidth, front-to-back ratio, and input impedance, and depending on the results, to determine the most promising model. The second step was to run the selected model on the computer by using NEC to get data both for radiation patterns and near magnetic fields. Examination of the radiation patterns is the most effective way to see the performance of log-periodic antennas. The purpose of getting near magnetic fields data in addition to radiation fields data was for an attempt to obtain the k-β diagrams of the half square log-periodic array by using near magnetic fields data and to see the relation between the radiation patterns and the k-β diagram. The importance of the k-β diagram comes from the fact that in uniformly periodic arrays it is possible to identify the frequency regions where backward radiation occurs by examining the k-β diagram. A uniformly periodic array is one in which all the elements, dimensions and, spacing between the elements are the same. Since backward radiation is an important characteristic of successful log-periodic antennas, a k-β diagram is a very useful tool in determining the potential of a candidate log-periodic structure by analyzing the k-β diagram of its uniformly periodic counterpart. For the log-periodic case it is not easy to obtain the k-β diagram. The k-β diagram approach used in the analysis of the uniformly periodic structures is based on the analysis of infinite length structures. Since practical structures are of finite length, their current distribution usually will be different than that of the infinite length structures and some deviations in behavior may occur even in uniformly periodic structures. For example, the boundary lines between the various length regions are not sharply defined. Effective radiation may occur from a finite structure at frequencies where the phase constant lies within the slow-wave region [Ref. 8]. Secondly, in the uniformly periodic case, d is constant and k is the controlled variable in obtaining the k-β diagram. For the log-periodic case, the period, d, continually increases as one moves away from the

feed with the frequency fixed. By fixing k and making d variable, a k-β diagram for the log-periodic structure may be obtained. With this approach, it is assumed that β on the log-periodic structure is determined only by local behavior of the structure [Ref. 9]. Also, since a log-periodic structure is not uniform, at a given frequency different space harmonic phase constants are found for each cell along the structure. For these reasons different approaches, other than the k-β diagram approach, are generally used in the analysis of log-periodic structures. One of the methods used in this thesis is evaluation of amplitude and phase plots of element currents to determine regions which create backfire radiation and comparison of this information with radiation patterns.

For accuracy, a double precision version of the Numerical Electromagnetics Code (NEC) was used throughout the simulation process.

B. NUMERICAL ELECTROMAGNETICS CODE (NEC)

Half square log-periodic arrays used in this thesis were modeled on the IBM system 370 main-frame computer by using the Numerical Electromagnetics Code (NEC), version three. NEC has been developed at the Lawrence Livermore Laboratory, Livermore, California, under the sponsorship of the Naval Ocean Systems Center and The Air Force Weapons Laboratory.

It is a user oriented computer code for analyzing the electromagnetic response of antennas and other metal structures by evaluating the numerical solutions of integral equations for currents induced on the structure by incident fields or sources.

The code can handle models with nonradiating networks and transmission lines connecting parts of the structure, imperfect or perfect conductors, and lumped element loading. Structures may also be modeled in free space or over a ground plane that may be either a perfect or imperfect conducter.

Structures may be excited either by voltage sources on the structure or by an incident plane wave which may be linearly or elliptically polarized. NEC outputs may include currents and charges, radiated fields and near electric or magnetic fields. For better accuracy calculations double precision versions are also available to the user.

C. DEVELOPMENT OF THE COMPUTER MODEL

The major consideration in selection of computer model was the tradeoff between antenna performance and deployment capability. As the number of the elements in the array increases, the performance of the antenna also increases, but, construction of the antenna will require more time and manpower, which are crucial factors under battle

conditions. Therefore a computer model must be chosen which is operationally practical.

Because the performance of the antenna can be determined from its far field radiation patterns, originally an array of 10 elements was modeled and run on the computer for radiation pattern evaluation. Far field radiation patterns for a 10-element half square log-periodic array did not show good performance. Following this, a 13-element array was modeled. The performance was better than that of the 10-element array, but was not good enough.

After observing the results of the 13-element half square log-periodic array the final model was designed. At the start of the design the only parameter available was the required operational frequency range of 2 to 30 MHz. Since the radiating elements are to be approximately half wavelength long at the operating frequency, the length of the longest element was 75 M. Considering that the length of the array should be around one wavelength long at the lowest frequency, the distance from the apex to the longest element was 150 M. From these parameters the apex angle α was found as 28.14 ° from $\tan \alpha/2 = L_n/2R_n$. Here L_n is the length of the longest element and R_n is the distance from apex to the longest element. The selection of the scale factor, τ, was somewhat arbitrary. Since, higher values of τ require more elements in the array Carrel's design curves for dipoles were examined (although it is not known whether his information is applicable to the half square or not) and a value of 0.84 was chosen. Using this scale factor and the length of the longest element, lengths of other elements were determined. Seventeen elements were required to cover the 2-30 MHz frequency range. Figure 2.1 shows the structural geometry of the half square log-periodic array. For ease of computer modeling, the structure was placed on the X-Y plane, the shortest element being at the origin and the array extending along the X axis. The lengths of the elements and their distances from the origin along with their corresponding resonant frequencies are shown in Table 1.

Based on Johnsen's findings for the uniformly periodic array, an implicit transmission line of 300 Ohms was used in the NEC model. An implicit transmission line model is one in which the currents on the wire segments which are connected to the ends of the transmission line are modified by using ideal, non-radiating transmission line equations. This neglects transmission line attenuation due to radiation, conductor and dielectric losses and assumes balanced currents. Johnsen showed that the half square log-periodic array is a balanced structure and NEC allows

transmission lines on balanced structures to be modeled by implicit transmission line equations. The use of implicit transmission line equations allows the treatment of transmission lines as two port networks by defining characteristic impedance and length and calculating response. Implicit transmission lines reduce the number of wire segments in a model, thus the size of the matrix necessary to evaluate currents is reduced.

Since the half square log-periodic array is constructed with half square elements and each element consists of two quarter square elements connected together by an insulated connector on the horizontal wire, to make the model precise to the highest degree possible the lengths of the insulators between the elements were scaled by scale factor. The insulators were modeled as open circuits. In order to see the effect of the scaling on element wire thickness, model was run for scaled wire diameters but no significant variation on performance was observed. Both "in-phase" and "anti-phase" excitation were tested to establish the usefulness of each. In-phase excitation is where both sets of corners on a half square element are fed with the same phase. In anti-phase excitation, the phase difference between corners is 180° Anti-phase excitation was chosen because the desired unidirectional azimuth radiation pattern is produced. With in-phase excitation, radiation from currents on the horizontal portion of the elements cancel producing azimuthal nulls on-axis, which are undesired.

Data sets used for the computer simulation are listed in Appendix A and Appendix B.

D. FAR-FIELD RADIATION PATTERNS

Since there is not a well established methodology for the analysis of log-periodic antennas, mostly the analysis of the performance is experimental. In this respect radiation patterns are one of the key parameters for evaluating the performance of log-periodic antennas. For this research, radiation patterns were calculated at the resonant, and also in-between frequencies in free space and on perfect ground environments with in-phase and anti-phase excitation options using NEC.

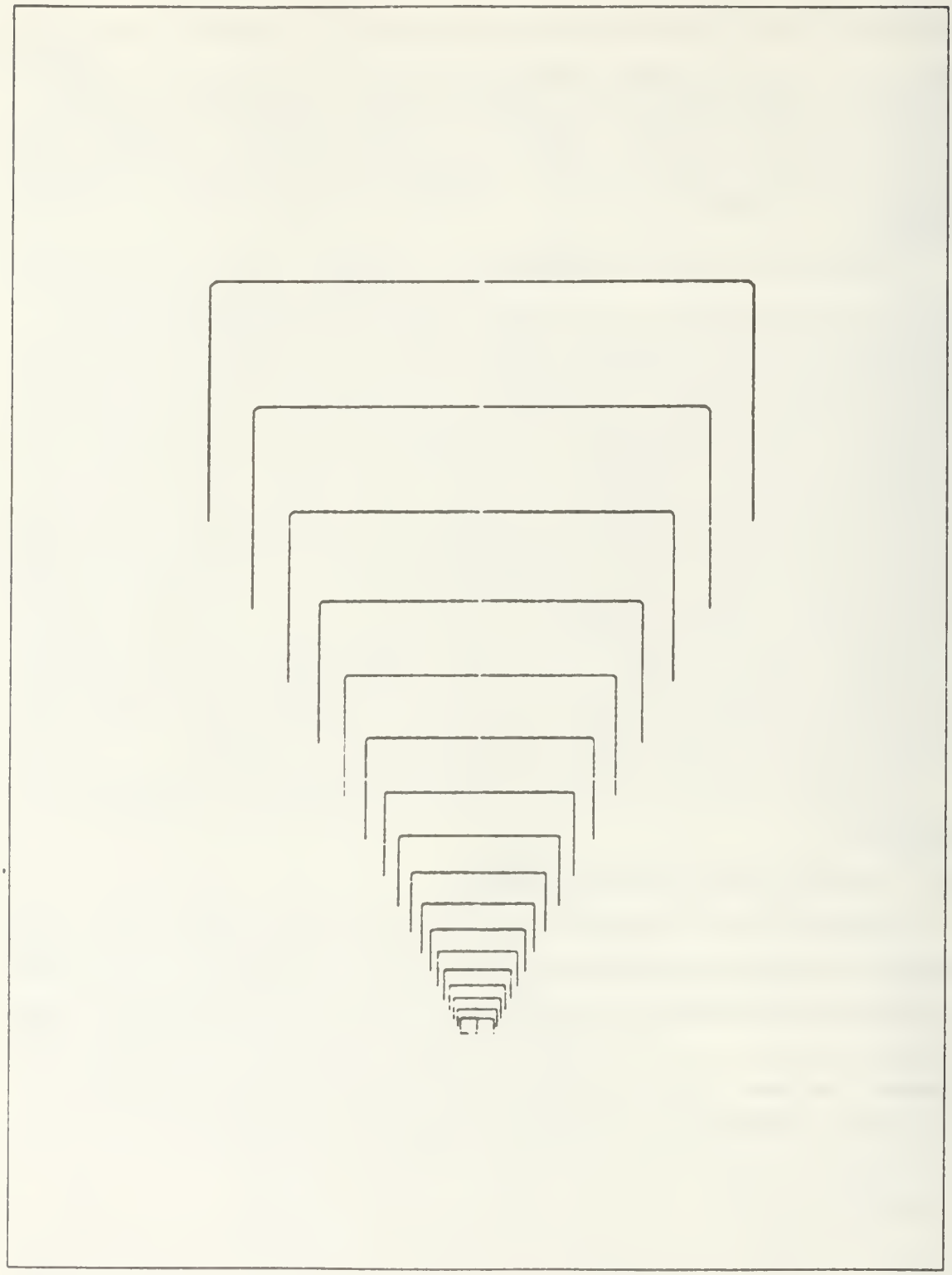

Figure 2.1 Half Square Log-Periodic Array.

TABLE 1

HLPA DESIGN PARAMETERS

Element No.	Frequency (MHz)	Distance (m)	Length (m)
1	32.55	0.0	4.61
2	27.34	1.76	5.49
3	22.96	3.85	6.53
4	19.29	6.33	7.77
5	16.20	9.29	9.25
6	13.61	12.82	11.02
7	11.43	17.02	13.12
8	9.60	22.02	15.62
9	8.06	27.96	18.59
10	6.77	35.05	22.13
11	5.69	43.48	26.34
12	4.78	53.52	31.37
13	4.01	65.46	37.34
14	3.37	79.68	44.45
15	2.83	96.62	52.92
16	2.38	116.78	63.00
17	2.00	140.78	75.00

III. EXPERIMENTAL RESULTS

The selected model was first run with in-phase and anti-phase excitation with a switched transmission line in free space, then over perfect ground. Switching is the transposition of the transmission line between adjacent elements as seen in Figure 1.2 to generate a 180° phase reversal. The data collected included radiation patterns and magnitude and phase plots of near magnetic fields.

A. RADIATION PATTERNS

Free space radiation patterns with anti-phase excitation showed the expected backfire radiation. (Backfire radiation is directed toward the point of excitation, a trait which appears to be inherent in most of the successful unidirectional log-periodic antennas, and is believed to be the result of a space wave traveling along the structure in the direction opposite to the phase progression of currents in the feed line.) The backward-traveling wave is due to the existence of backward space harmonics in the spectrum of the periodic structure. The periodic structure should be such as to produce only waves which are quite slow at the frequencies where radiation is not intended. At frequencies where radiation is intended, one or more of the space-harmonic waves should be "fast" or almost fast. Thus, for the log-periodic structure, a feeder wave progresses toward the active (radiating) region under slow wave conditions. According to this theory, the dominant space harmonic in the active region propagates in the backward direction [Ref. 8]. Between 2 and 5 MHz, although the main radiation is in the backfire direction, the front-to-back ratio is lower than that of for the rest of the frequency range. There seems to be one major reason for this, namely "truncation effect". If the structure were of infinite type the properties would repeat periodically and there would not be any performance variation. Near the low-frequency cutoff of 2 MHz, a sizable reflection of the fundamental wave (end effect) is produced by the rear truncation. This reflected wave then travels back along the structure in the opposite direction, passing through the active region a second time where it is partially radiated. The resulting radiation pattern from this second pass is a reduced mirror image of the main pattern from the first pass of the fundamental wave [Ref. 10]. As the frequency is increased the electrical properties of the truncated structure converge to characteristic values. So for our case 5 Mhz. presents a low-frequency limit; above this frequency

the properties display fairly small variations. Figure 3.1 shows a sample radiation pattern in free space. Appendix C includes other radiation patterns calculated in free space. Patterns show an average half power beamwidth of 56° and an average gain of 4 dB. at resonant frequencies. In Table 2 the antenna parameters, power gain, half power beamwidth, and input impedance are shown for resonant frequencies in free space.

Radiation patterns taken over perfect ground showed similar results except for higher and more stable gain and half power beamwidth values. A sample radiation pattern plotted over perfect ground is shown in Figure 3.2 and the antenna parameters, half power beamwidth, power gain, and input impedance values for resonant frequencies are shown in Table 3. Appendix D contains other radiation patterns taken over perfect ground. As can be seen from radiation patterns as the frequency increases the back lobe gets smaller and radiation in the forward direction gets stronger. This is an indication of the smooth transfer of functions of one resonant element to the next.

B. AMPLITUDE AND PHASE DISTRIBUTIONS OF ELEMENT CURRENTS

Appendix E shows amplitude and phase plots of element currents for the half square log-periodic array in free space for resonant frequencies. Appendix F shows amplitude and phase plots of element currents for resonant frequencies over perfect ground. These plots clearly show the possibility of obtaining a leading phase shift along some portion of the structure that will produce backfire radiation. On the plots, the leftmost point corresponds to the smallest element which is half-wavelength long at the highest cut-off frequency. The feed line is connected to the array at this element. The rightmost point corresponds to the longest element which is half wavelength long at lowest cut-off frequency of 2 Mhz. From the amplitude and phase plots of element currents it can be observed that small contributions from those elements close to feed point tend to cancel each other because of the a phase difference of almost 180°. Currents are strongest mainly on a few elements in front of the element which is closer in length to a half wavelength of the operating frequency. These elements form the active region of the array. For these elements, the phase shift along the structure shows a leading phase condition. The leading phase condition corresponds to a backward traveling wave and leads to directivity which is predominantly backfire. Following the element closest in length to the resonant frequency, the current amplitude falls off suddenly showing a desired end-effect. As the operating frequency is increased or decreased the active region moves along the array but radiation patterns vary only slightly.

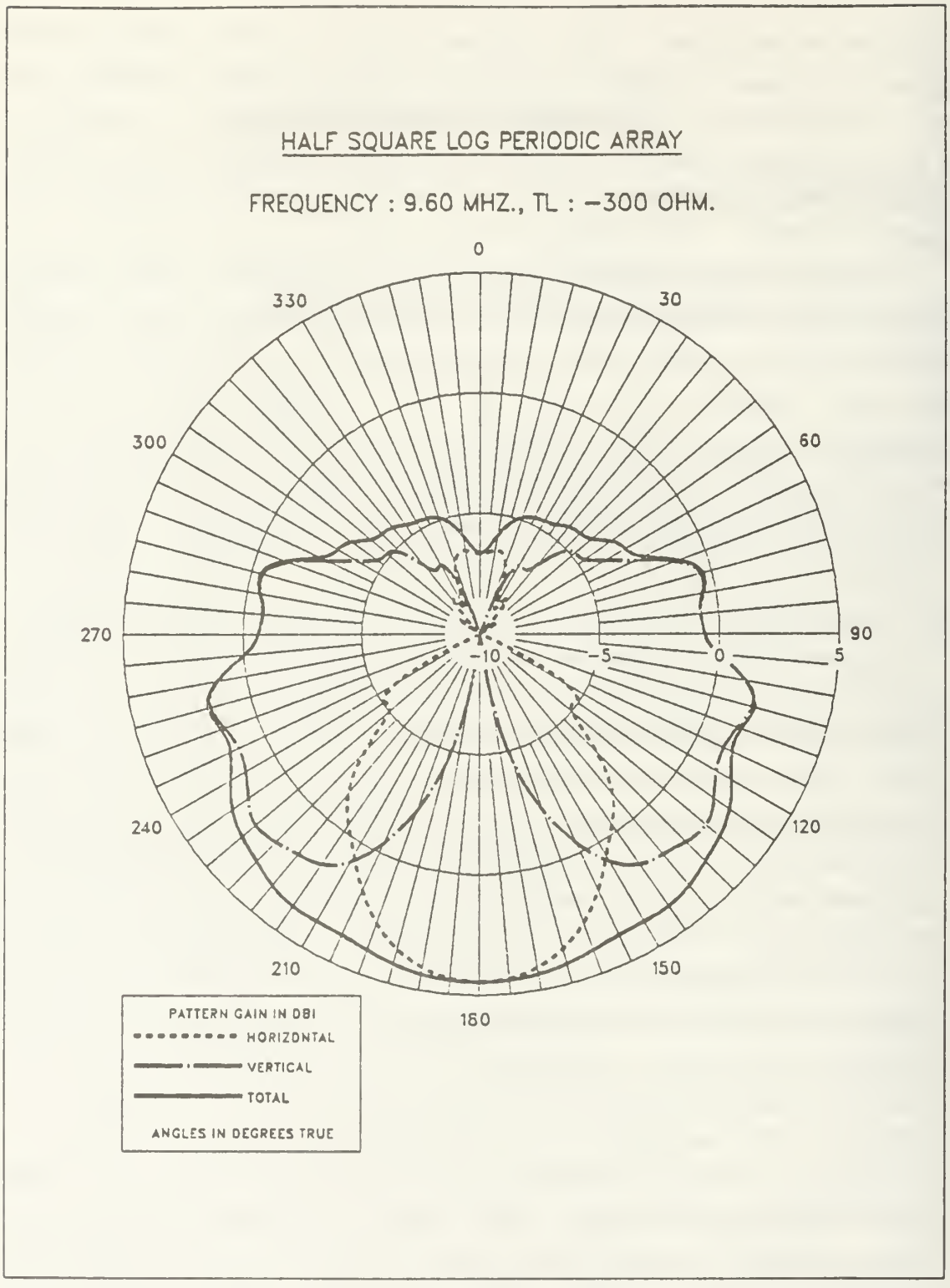

Figure 3.1 Horizontal Pattern, Frequency: 9.60 MHz.

TABLE 2

NUMERICAL RESULTS
IN FREE SPACE

Frequency (MHz)	HPBW (degrees)	Gain (dB)	Input impedance (real and imaginary)
2.0	68	2.15	236 -187
2.38	64	3.74	215 -180
2.83	66	3.26	256 -221
3.37	60	3.90	255 -189
4.07	58	4.08	333 -192
4.78	64	3.66	418 -195
5.69	58	4.20	462 -45.2
6.77	56	4.29	460 63
8.06	56	4.40	340 150
9.60	54	4.45	214 136
11.43	52	4.54	145 64.3
13.61	56	4.39	117 -22
16.20	54	4.41	151 -125
19.29	56	4.80	337 -193
22.96	58	4.26	219 38.8
27.34	54	3.65	77 -102

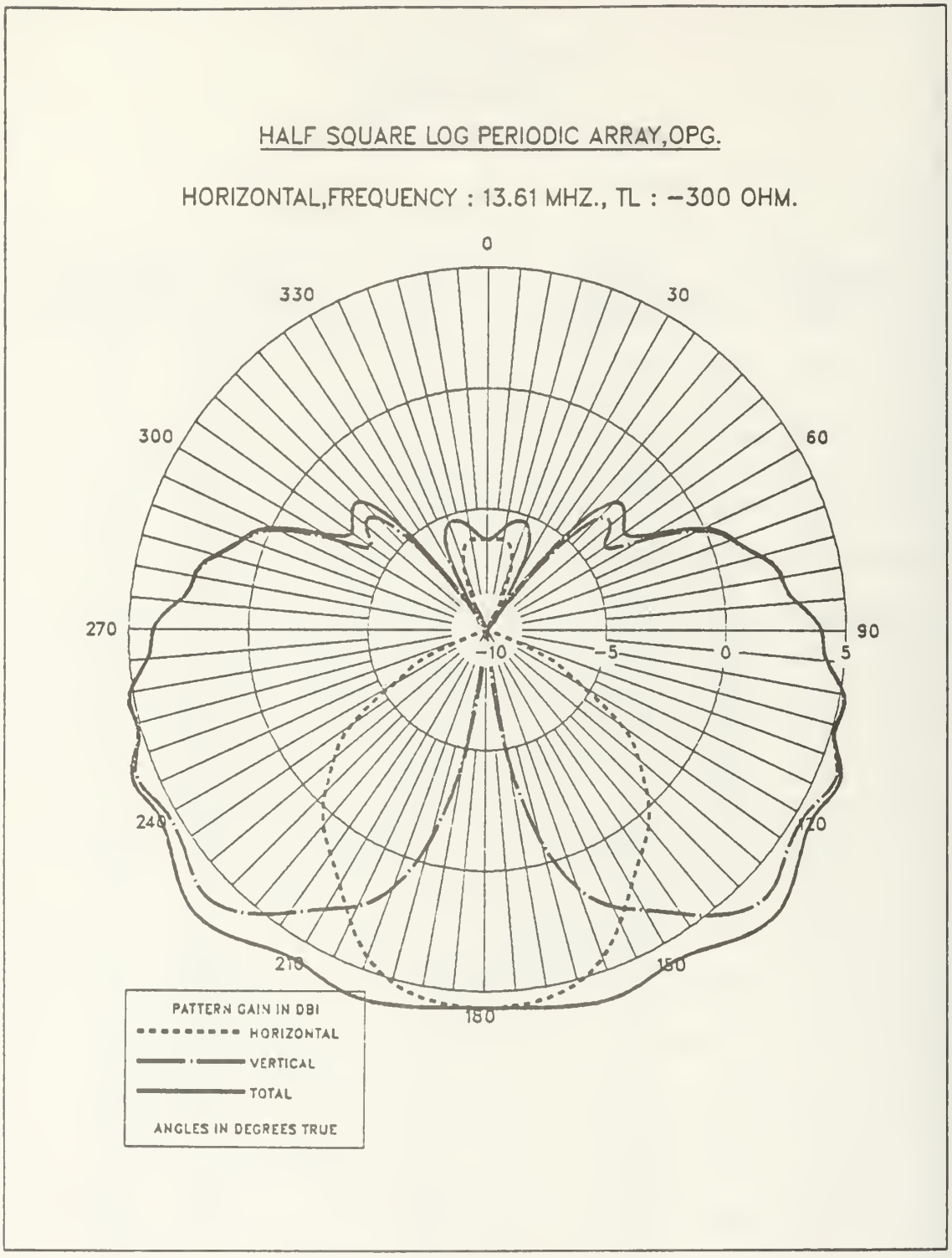

Figure 3.2 Horizontal Pattern, Frequency: 13.61 MHz.

TABLE 3

NUMERICAL RESULTS
OVER PERFECT GROUND

Frequency (MHz)	HPBW (degrees)	Gain (dB)	Input impedance (real and imaginary)
2.0	72	3.35	157 -47
2.38	66	5.31	135 -43.3
2.83	68	5.19	151 -83
3.37	62	5.14	136 -62
4.01	62	5.91	160 -79.1
4.78	70	6.28	186 -123
5.69	58	5.55	199 -118
6.77	58	5.56	239 -145
8.06	58	5.69	309 -143
9.60	56	5.66	387 -62
11.43	56	5.67	349 75
13.61	56	5.67	211 84
16.20	56	5.69	137 9.7
19.29	56	5.91	152 -110
22.96	60	5.21	257 -193
27.34	54	5.29	50 -37.5

IV. CONCLUSIONS AND RECOMMENDATIONS

A. CONCLUSIONS

This thesis investigated the potential of a half square log-periodic array for use by the military over the specific high frequency range of 2 to 30 MHz. Using the Numerical Electromagnetics Code (NEC) a computer model of half square log-periodic array with dual feed was used to obtain data for plotting radiation patterns and amplitude and phase plots of the element currents for evaluation of the performance of the array. The model was run with a transmission line impedance value of 300 Ohms which had been shown by Johnsen [Ref. 2] to be the optimum. The model was also run with impedance values below and above 300 Ohms verifying 300 Ohms as optimum.

The model was run in free space and over perfect ground with different combinations of switched and unswitched transmission line and in-phase and anti-phase feed options. Radiation patterns and amplitude and phase plots of the element currents were used to evaluate the performance of the antenna. Since there is not a well established method, examination of the radiation patterns was the major tool for determination of the performance of the array. The results can be listed as follows:

* The half square log-periodic array with dual feed shows the characteristics of a successful log-periodic structure. Structure shows a unidirectional "backfire" radiation pattern, radiation being directed towards the small end of the array.
* The structure keeps almost the same performance over the entire design frequency range with small variations. But, between 2 and 5 MHz, there is a performance degradation because of the truncation effect. As the frequency increases performance of the antenna is stabilized and variations get smaller.
* With these design parameters the array gives an average power gain of 5.2 dB. and an average half power beamwidth (HPBW) of 57°
* It can be said that it would be possible to get a more directive radiation pattern and higher gain from the structure using a higher scale factor, but this in turn would require more elements to cover the frequency range making the construction of the array unpractical when considered for military use. With these design parameters, although it is still a big structure, it would not be difficult to construct the array at high levels of command for this frequency.

The most important conclusion which can be drawn from this study is that the half square log-periodic array shows the characteristics of a successful log-periodic

structure. When considered for use at much higher frequencies the dimensions of the elements will be much smaller making it possible to use higher scale factor values for higher gain and directivity.

B. RECOMMENDATIONS

Based on the results of the study, the following recommendations are made :

* This study investigated the half square log-periodic array in free space and over perfect ground. Although, the results show satisfactory performance, a study of the array should be done over lossy ground to see what additional effects occur because of the lossy ground.

* The study was limited by considerations of frequency range and military application. To satisfy these considerations a lower value of scale factor was used in order to make the array practical for the military. Although performance is satisfactory with these design parameters over this frequency range, it should be possible to get better performance at much higher frequencies using higher values of scale factor (since the overall dimensions of the array will be much smaller). Even at the 2 to 30 MHz range, when considered for civilian use at a fixed site, the array can be constructed with more elements for better gain and directivity.

* Following near magnetic field analysis of uniformly periodic half square array by Johnsen [Ref. 2], this thesis formed the second step in study of half square log-periodic array. Johnsen investigated near magnetic fields of uniformly periodic half square array and obtained k-β diagrams. From the k-β diagrams, he identified frequency regions showing backward radiation, suggesting that a log-periodic half square array would support backward radiation. In the absence of a well established theoretical approach for log-periodic antenna design, the method used in this combined study and first suggested by Mayes, Deschamps, and Patton [Ref. 8] has proven to be very successful and less time consuming. It is therefore recommended that before attacking log-periodic structures directly, a near field investigation of the uniformly periodic counterparts may give insight to log-periodic performance. Analysis of k-β diagrams of uniformly periodic structures can provide clues to the performance of log-periodic counterparts. If the study of uniformly periodic structures proves fruitful, it is highly probable that log-periodic counterparts will give good broadband performance. Near field analysis of uniformly periodic counterparts of many successful and unsuccessful structures shows this to be the case.

APPENDIX A
NEC DATA FILE FOR FREE SPACE

```
CM HALF SQUARE LOG PERIODIC ARRAY
CM 17 ELEMENTS, TL:-300 , ANTI PHASE DUAL FEED
CM TAU:0.84,SIGMA:0.16,ALPHA:28.072 DEGREE
CM ARRAY LENGTH:140.784 M.
CM IN FREE SPACE
CE FREQUENCY:10.0 MHZ.
GW 31,6, 0,-.02,2.349, 0,-2.304,2.349, .000814
GW 1,1, 0,-2.304,2.349, 0,-2.349,2.304, .000814
GW 51,6, 0,-2.349,2.304, 0,-2.349,0, .000814
GW 32,6, 1.756,-.024,2.797, 1.756,-2.743,2.797, .000814
GW 2,1, 1.756,-2.743,2.797, 1.756,-2.797,2.743, .000814
GW 52,6, 1.756,-2.797,2.743, 1.756,-2.797,0, .000814
GW 33,6, 3.845,-.028,3.33, 3.845,-3.265,3.33, .000814
GW 3,1, 3.845,-3.265,3.33, 3.845,-3.33,3.265, .000814
GW 53,6, 3.845,-3.33,3.265, 3.845,-3.33,0, .000814
GW 34,6, 6.333,-.034,3.964, 6.333,-3.887,3.964, .000814
GW 4,1, 6.333,-3.887,3.964, 6.333,-3.964,3.887, .000814
GW 54,6, 6.333,-3.964,3.887, 6.333,-3.964,0, .000814
GW 35,6, 9.295,-.04,4.719, 9.295,-4.628,4.719, .000814
GW 5,1, 9.295,-4.628,4.719, 9.295,-4.719,4.628, .000814
GW 55,6, 9.295,-4.719,4.628, 9.295,-4.719,0, .000814
GW 36,6, 12.821,-.048,5.618, 12.821,-5.509,5.618, .000814
GW 6,1, 12.821,-5.509,5.618, 12.821,-5.618,5.509, .000814
GW 56,6, 12.821,-5.618,5.509, 12.821,-5.618,0, .000814
GW 37,6, 17.019,-.057,6.688, 17.019,-6.559,6.688, .000814
GW 7,1, 17.019,-6.559,6.688, 17.019,-6.688,6.559, .000814
GW 57,6, 17.019,-6.688,6.559, 17.019,-6.688,0, .000814
GW 38,6, 22.016,-.068,7.961, 22.016,-7.808,7.961, .000814
GW 8,1, 22.016,-7.808,7.961, 22.016,-7.961,7.808, .000814
GW 58,6, 22.016,-7.961,7.808, 22.016,-7.961,0, .000814
GW 39,6, 27.965,-.081,9.478, 27.965,-9.295,9.478, .000814
GW 9,1, 27.965,-9.295,9.478, 27.965,-9.478,9.295, .000814
GW 59,6, 27.965,-9.478,9.295, 27.965,-9.478,0, .000814
GW 40,6, 35.047,-.096,11.283, 35.047,-11.066,11.283, .000814
GW 10,1, 35.047,-11.066,11.283, 35.047,-11.283,11.066, .000814
GW 60,6, 35.047,-11.283,11.066, 35.047,-11.283,0, .000814
GW 41,6, 43.478,-.114,13.303, 43.478,-13.174,13.303, .000814
GW 11,1, 43.478,-13.174,13.303, 43.478,-13.303,13.174, .000814
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GW 42,6, 53.515,-.136,15.991, 53.515,-15.683,15.991, .000814
GW 12,1, 53.515,-15.683,15.991, 53.515,-15.991,15.683, .000814
GW 62,6, 53.515,-15.991,15.683, 53.515,-15.991,0, .000814
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GW 16,1, 116.784,-31.5,32.119, 116.784,-32.119,31.5, .000814
GW 66,6, 116.784,-32.119,31.5, 116.784,-32.119,0, .000814
GW 47,6, 140.784,-.326,38.237, 140.784,-37.5,38.237, .000814
GW 17,1, 140.784,-37.5,38.237, 140.784,-38.237,37.5, .000814
GW 67,6, 140.784,-38.237,37.5, 140.784,-38.237,0, .000814
GX 100,010
GE
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TL 2,1,3,1, -300, 2.09
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TL 7,1,8,1, -300, 4.997
TL 8,1,9,1, -300, 5.949
TL 9,1,10,1, -300, 7.082
TL 10,1,11,1, -300, 8.431
TL 11,1,12,1, -300, 10.037
TL 12,1,13,1, -300, 11.949
TL 13,1,14,1, -300, 14.225
TL 14,1,15,1, -300, 16.934
TL 15,1,16,1, -300, 20.16
TL 16,1,17,1, -300, 24.0
TL 101,1,102,1, -300, 1.755
TL 102,1,103,1, -300, 2.09
TL 103,1,104,1, -300, 2.488
TL 104,1,105,1, -300, 2.962
TL 105,1,106,1, -300, 3.526
TL 106,1,107,1, -300, 4.198
TL 107,1,108,1, -300, 4.997
TL 108,1,109,1, -300, 5.949
TL 109,1,110,1, -300, 7.082
TL 110,1,111,1, -300, 8.431
TL 111,1,112,1, -300, 10.037
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PL 2,2,1,1
NH 0,1,1,1, 116.784,-31.809,31.809, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 120.784,-32.819,32.819, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 124.784,-33.829,33.829, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 128.784,-34.839,34.839, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 132.784,-35.844,35.844, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 136.784,-36.858,36.858, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 140.784,-37.868,37.868, 1,1,1
XQ
PL 3, 2, 0, 4
RP 0, 1, 361, 1000, 90, 0, 0, 1     HORIZONTAL
XQ
PL 3, 1, 0, 4
RP 0, 181, 1, 1000, 90, 0, -1, 0      VERTICAL
XQ
EN
```

APPENDIX B
NEC DATA FILE FOR PERFECT GROUND

```
CM HALF SQUARE LOG PERIODIC ARRAY
CM 17 ELEMENTS, TL:-300 , ANTI PHASE DUAL FEED
CM TAU:0.84,SIGMA:0.16,ALPHA:28.072 DEGREE
CM ARRAY LENGTH:140.784 M.
CM OVER PERFECT GROUND
CE FREQUENCY: 30.0 MHZ.
GW 31,6, 0,-.02,2.349, 0,-2.304,2.349, .000814
GW 1,1, 0,-2.304,2.349, 0,-2.349,2.304, .000814
GW 51,6, 0,-2.349,2.304, 0,-2.349,0, .000814
GW 32,6, 1.756,-.024,2.797, 1.756,-2.743,2.797, .000814
GW 2,1, 1.756,-2.743,2.797, 1.756,-2.797,2.743, .000814
GW 52,6, 1.756,-2.797,2.743, 1.756,-2.797,0, .000814
GW 33,6, 3.845,-.028,3.33, 3.845,-3.265,3.33, .000814
GW 3,1, 3.845,-3.265,3.33, 3.845,-3.33,3.265, .000814
GW 53,6, 3.845,-3.33,3.265, 3.845,-3.33,0, .000814
GW 34,6, 6.333,-.034,3.964, 6.333,-3.887,3.964, .000814
GW 4,1, 6.333,-3.887,3.964, 6.333,-3.964,3.887, .000814
GW 54,6, 6.333,-3.964,3.887, 6.333,-3.964,0, .000814
GW 35,6, 9.295,-.04,4.719, 9.295,-4.628,4.719, .000814
GW 5,1, 9.295,-4.628,4.719, 9.295,-4.719,4.628, .000814
GW 55,6, 9.295,-4.719,4.628, 9.295,-4.719,0, .000814
GW 36,6, 12.821,-.048,5.618, 12.821,-5.509,5.618, .000814
GW 6,1, 12.821,-5.509,5.618, 12.821,-5.618,5.509, .000814
GW 56,6, 12.821,-5.618,5.509, 12.821,-5.618,0, .000814
GW 37,6, 17.019,-.057,6.688, 17.019,-6.559,6.688, .000814
GW 7,1, 17.019,-6.559,6.688, 17.019,-6.688,6.559, .000814
GW 57,6, 17.019,-6.688,6.559, 17.019,-6.688,0, .000814
GW 38,6, 22.016,-.068,7.961, 22.016,-7.808,7.961, .000814
GW 8,1, 22.016,-7.808,7.961, 22.016,-7.961,7.808, .000814
GW 58,6, 22.016,-7.961,7.808, 22.016,-7.961,0, .000814
GW 39,6, 27.965,-.081,9.478, 27.965,-9.295,9.478, .000814
GW 9,1, 27.965,-9.295,9.478, 27.965,-9.478,9.295, .000814
GW 59,6, 27.965,-9.478,9.295, 27.965,-9.478,0, .000814
GW 40,6, 35.047,-.096,11.283, 35.047,-11.066,11.283, .000814
GW 10,1, 35.047,-11.066,11.283, 35.047,-11.283,11.066, .000814
GW 60,6, 35.047,-11.283,11.066, 35.047,-11.283,0, .000814
GW 41,6, 43.478,-.114,13.303, 43.478,-13.174,13.303, .000814
GW 11,1, 43.478,-13.174,13.303, 43.478,-13.303,13.174, .000814
GW 61,6, 43.478,-13.303,13.174, 43.478,-13.303,0, .000814
GW 42,6, 53.515,-.136,15.991, 53.515,-15.683,15.991, .000814
GW 12,1, 53.515,-15.683,15.991, 53.515,-15.991,15.683, .000814
GW 62,6, 53.515,-15.991,15.683, 53.515,-15.991,0, .000814
GW 43,6, 65.464,-.162,19.037, 65.464,-18.670,19.037, .000814
GW 13,1, 65.464,-18.670,19.037, 65.464,-19.037,18.670, .000814
GW 63,6, 65.464,-19.037,18.670, 65.464,-19.037,0, .000814
GW 44,6, 79.689,-.193,22.663, 79.689,-22.226,22.663, .000814
GW 14,1, 79.689,-22.226,22.663, 79.689,-22.663,22.226, .000814
GW 64,6, 79.689,-22.663,22.226, 79.689,-22.663,0, .000814
GW 45,6, 96.624,-.23,26.980, 96.624,-26.460,26.980, .000814
GW 15,1, 96.624,-26.460,26.980, 96.624,-26.980,26.460, .000814
GW 65,6, 96.624,-26.980,26.460, 96.624,-26.980,0, .000814
GW 46,6, 116.784,-.273,32.119, 116.784,-31.5,32.119, .000814
GW 16,1, 116.784,-31.5,32.119, 116.784,-32.119,31.5, .000814
GW 66,6, 116.784,-32.119,31.5, 116.784,-32.119,0, .000814
GW 47,6, 140.784,-.326,38.237, 140.784,-37.5,38.237, .000814
GW 17,1, 140.784,-37.5,38.237, 140.784,-38.237,37.5, .000814
GW 67,6, 140.784,-38.237,37.5, 140.784,-38.237,0, .000814
GX 100,010
GE -1
GN 1
TL 1,1,2,1, -300, 1.755
```

```
TL 2,1,3,1, -300, 2.09
TL 3,1,4,1, -300, 2.488
TL 4,1,5,1, -300, 2.962
TL 5,1,6,1, -300, 3.526
TL 6,1,7,1, -300, 4.198
TL 7,1,8,1, -300, 4.997
TL 8,1,9,1, -300, 5.949
TL 9,1,10,1, -300, 7.082
TL 10,1,11,1, -300, 8.431
TL 11,1,12,1, -300, 10.037
TL 12,1,13,1, -300, 11.949
TL 13,1,14,1, -300, 14.225
TL 14,1,15,1, -300, 16.934
TL 15,1,16,1, -300, 20.16
TL 16,1,17,1, -300, 24.0
TL 101,1,102,1, -300, 1.755
TL 102,1,103,1, -300, 2.09
TL 103,1,104,1, -300, 2.488
TL 104,1,105,1, -300, 2.962
TL 105,1,106,1, -300, 3.526
TL 106,1,107,1, -300, 4.198
TL 107,1,108,1, -300, 4.997
TL 108,1,109,1, -300, 5.949
TL 109,1,110,1, -300, 7.082
TL 110,1,111,1, -300, 8.431
TL 111,1,112,1, -300, 10.037
TL 112,1,113,1, -300, 11.949
TL 113,1,114,1, -300, 14.225
TL 114,1,115,1, -300, 16.934
TL 115,1,116,1, -300, 20.16
TL 116,1,117,1, -300, 24.0
EX 0,0,7,0,-1,0
EX 0,0,228,0,1,0
FR 1,1,,,30.0,0,
PL 2,2,1,1
NH 0,1,1,1, 0,-2.327,2.327, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 1.756,-2.770,2.770, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 3.845,-3.298,3.298, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 6.333,-3.926,3.926, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 9.295,-4.673,4.673, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 12.821,-5.563,5.563, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 15.019,-6.118,6.118, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 17.019,-6.623,6.623, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 19.516,-7.254,7.254, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 22.016,-7.885,7.885, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 23.965,-8.377,8.377, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 25,965,-8.882,8.882, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 27.965,-9.387,9.387, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 30.347,-9.888,9.888, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 32.687,-10.579,10.579, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 35.047,-11.175,11.175, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 37.878,-11.889,11.889, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 40.678,-12.596,12.596, 1,1,1
```

```
PL 2,2,1,1
NH 0,1,1,1, 43.478,-13.303,13.303, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 46.815,-14.146,14.146, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 50.165,-14.991,14.991, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 53.515,-15.837,15.837, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 57.464,-16.181,16.181, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 61.464,-17.844,17.844, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 65.464,-18.854,18.854, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 68.889,-19.718,19.718, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 72.489,-21.536,21.536, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 76.089,-21.964,21.964, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 79.689,-22.445,22.445, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 83.874,-23.501,23.501, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 88.124,-24.574,24.574, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 92.374,-25.647,25.647, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 96.624,-26.72,26.72, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 100.784,-27.77,27.77, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 104.784,-28.779,28.779, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 108.784,-29.789,29.789, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 112.784,-30.799,30.799, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 116.784,-31.809,31.809, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 120.784,-32.819,32.819, 1,1,1
PL 2 2,1,1
NH 0,1,1,1, 124.784,-33.829,33.829, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 128.784,-34.839,34.839, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 132.784,-35.844,35.844, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 136.784,-36.858,36.858, 1,1,1
PL 2,2,1,1
NH 0,1,1,1, 140.784,-37.868,37.868, 1,1,1
XQ
PL 3, 2, 0, 4
RP 0, 1, 361, 1000, 60, 0, 0, 1     HORIZONTAL
PL 3, 2, 0, 4
RP 0, 1, 361, 1000, 90, 0, 0, 1     HORIZONTAL
XQ
PL 3, 1, 0, 4
RP 0, 181, 1, 1000, 90, 0, -1, 0      VERTICAL
XQ
EN
```

APPENDIX C
RADIATION PATTERNS IN FREE SPACE

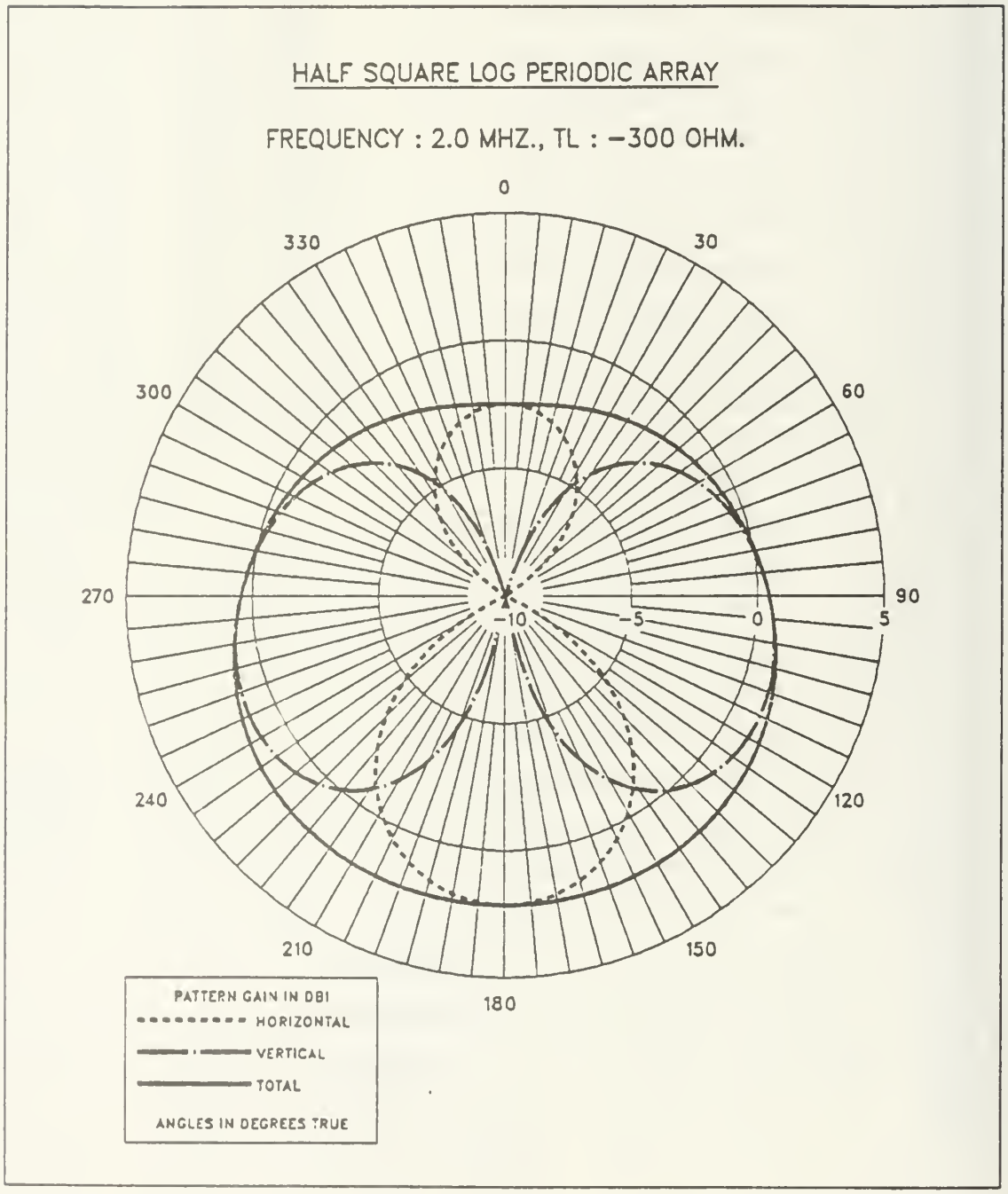

Figure C.1 Horizontal Pattern, Frequency: 2 MHz.

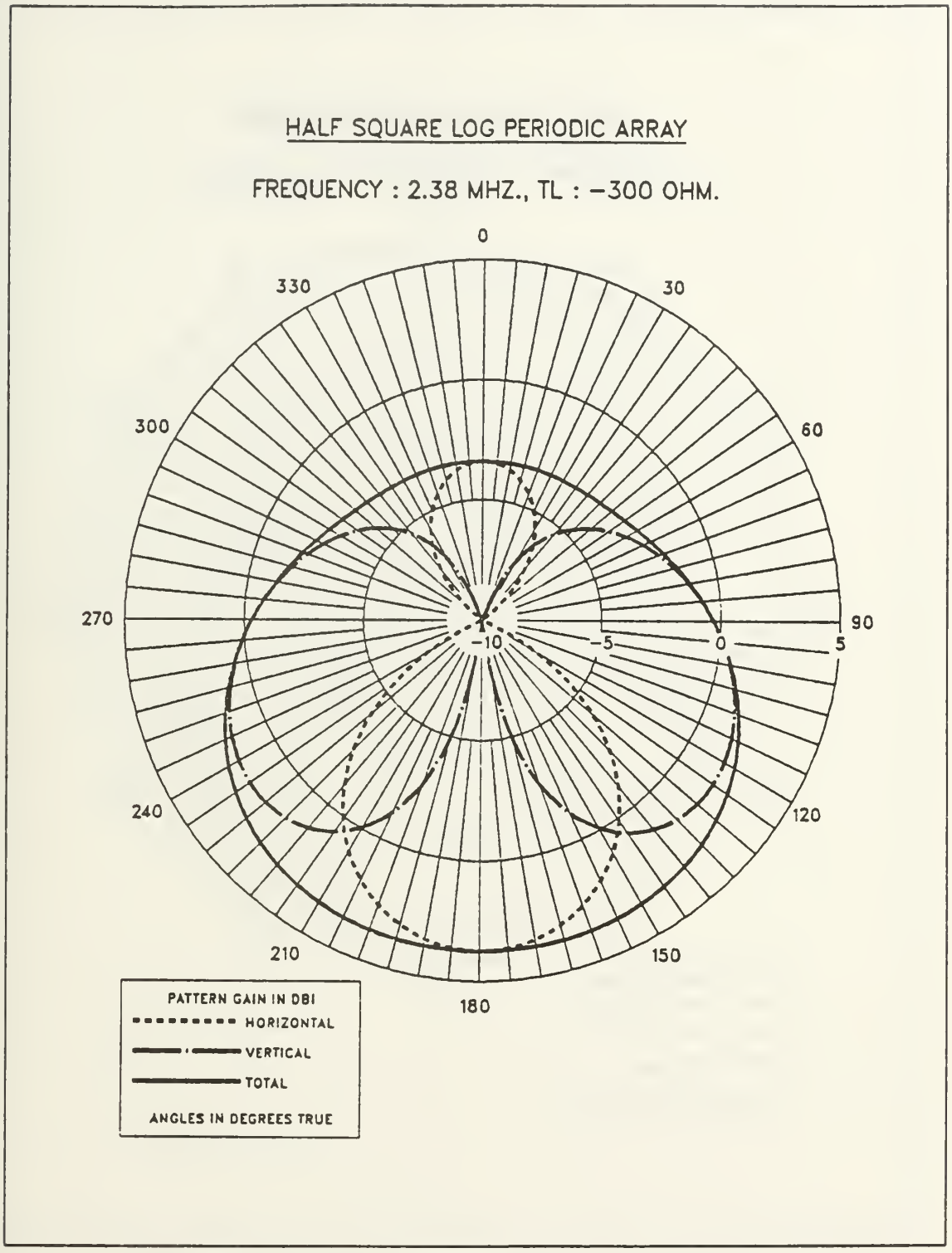

Figure C.2 Horizontal Pattern, Frequency: 2.38 MHz.

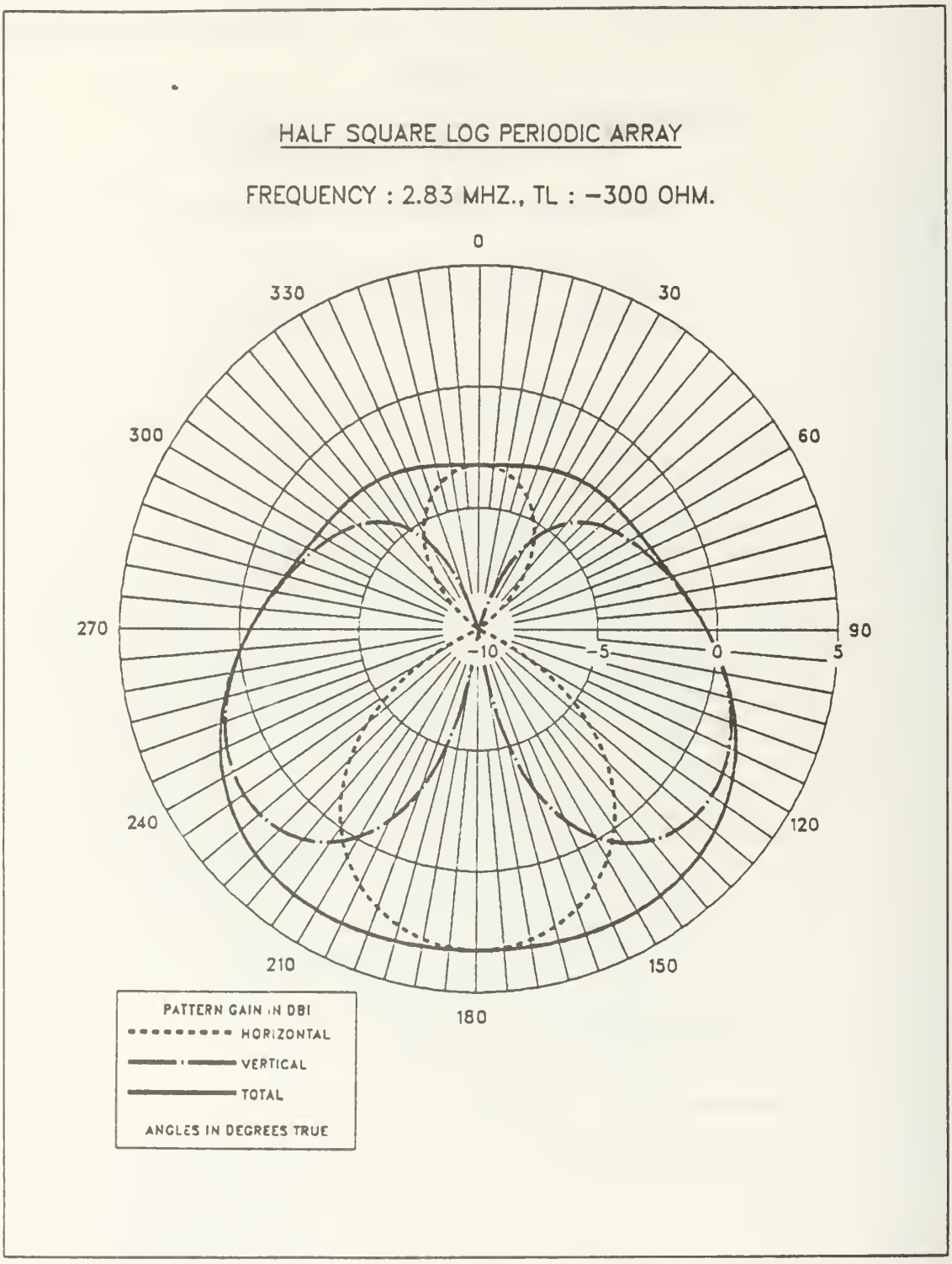

Figure C.3 Horizontal Pattern, Frequency: 2.83 MHz.

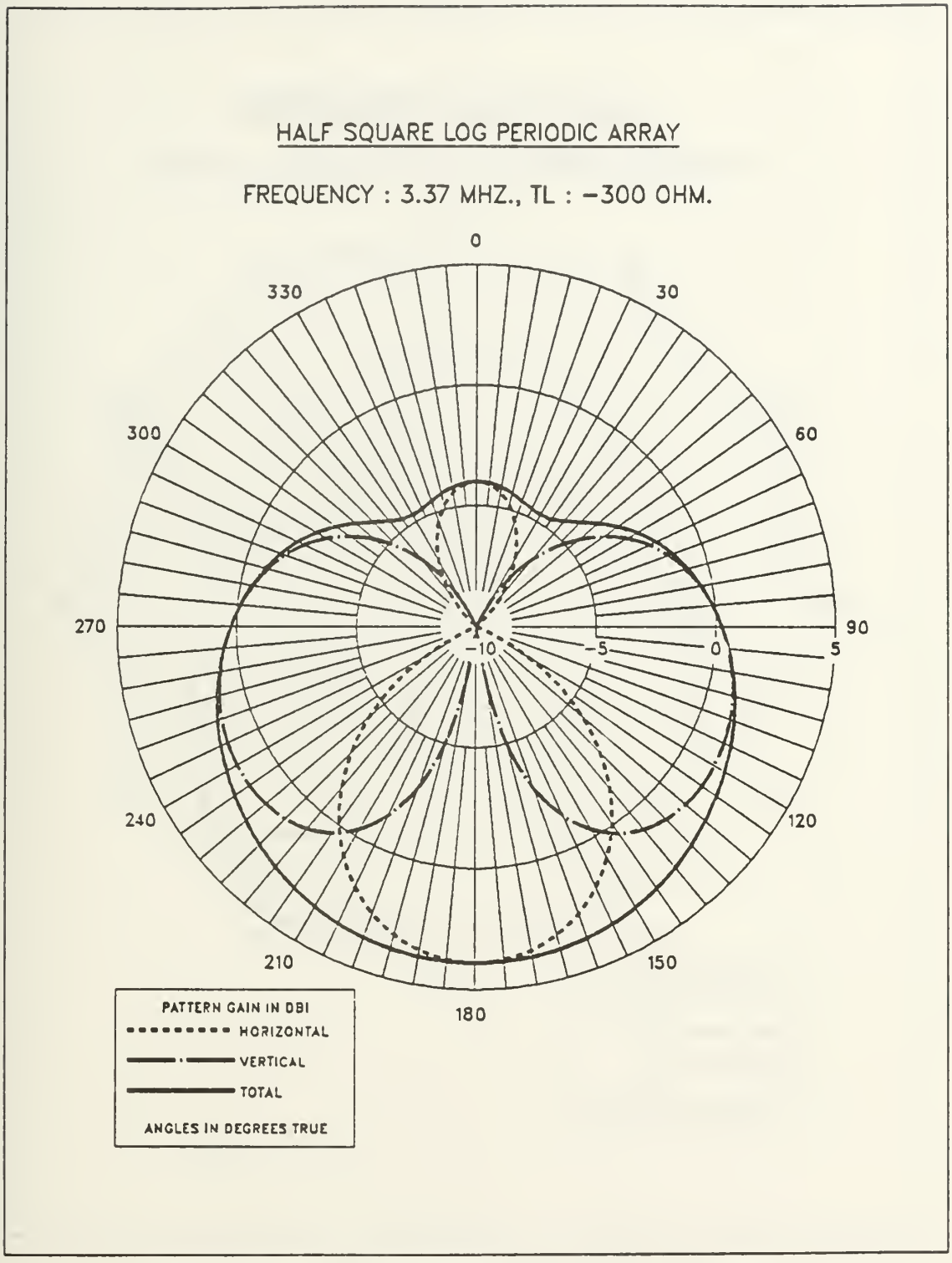

Figure C.4 Horizontal Pattern, Frequency: 3.37 MHz.

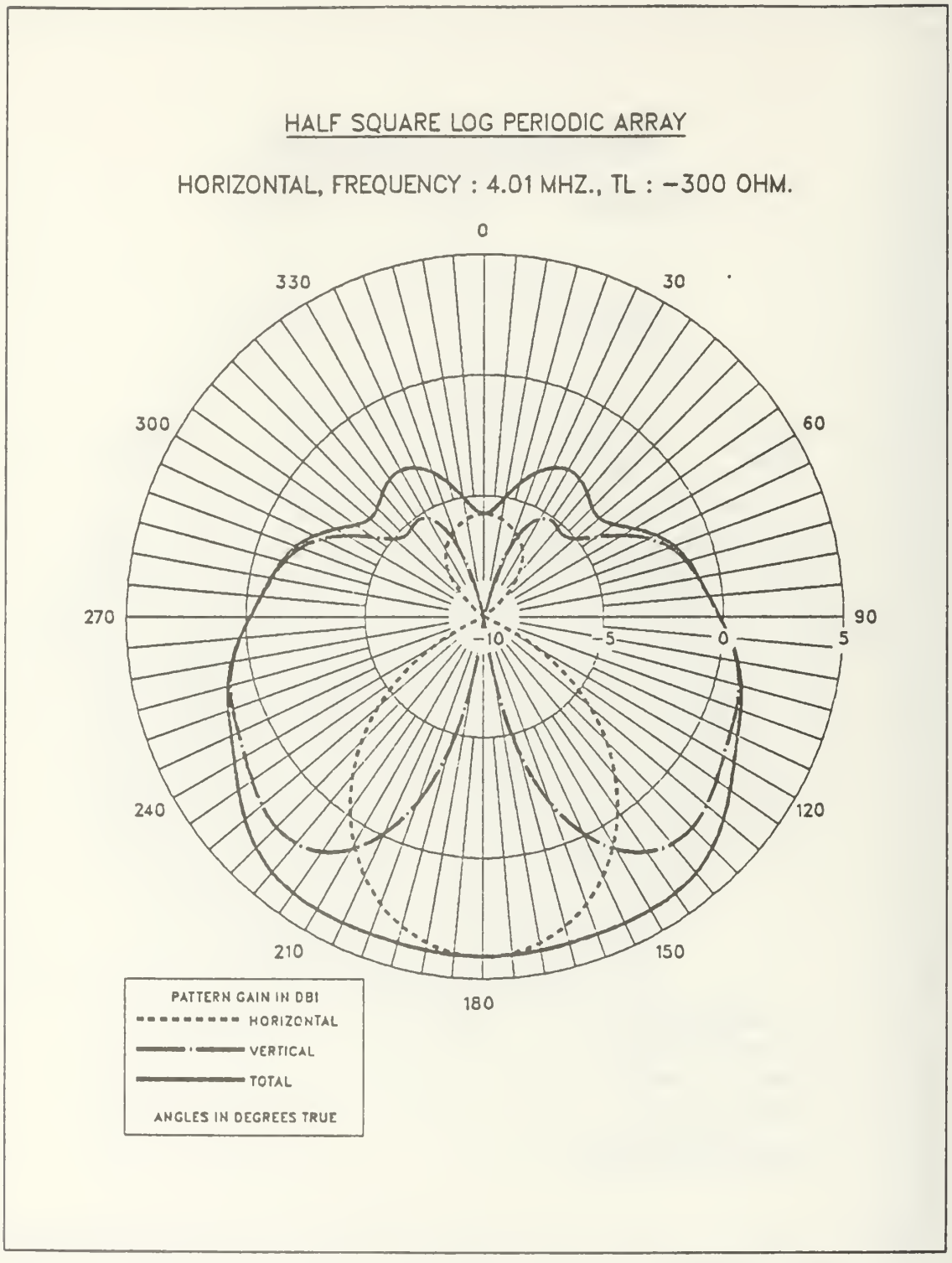

Figure C.5 Horizontal Pattern, Frequency: 4.01 MHz.

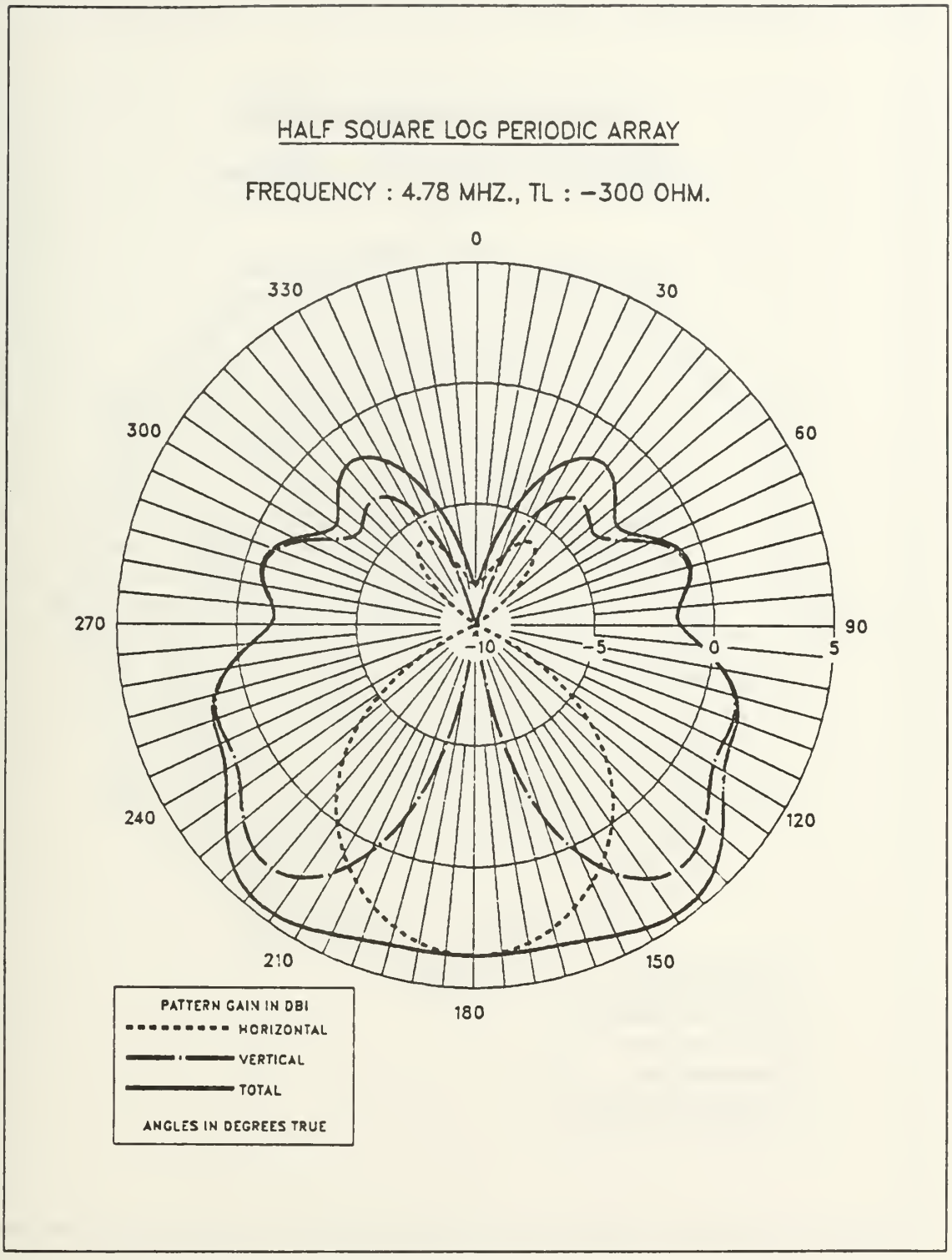

Figure C.6 Horizontal Pattern, Frequency: 4.78 MHz.

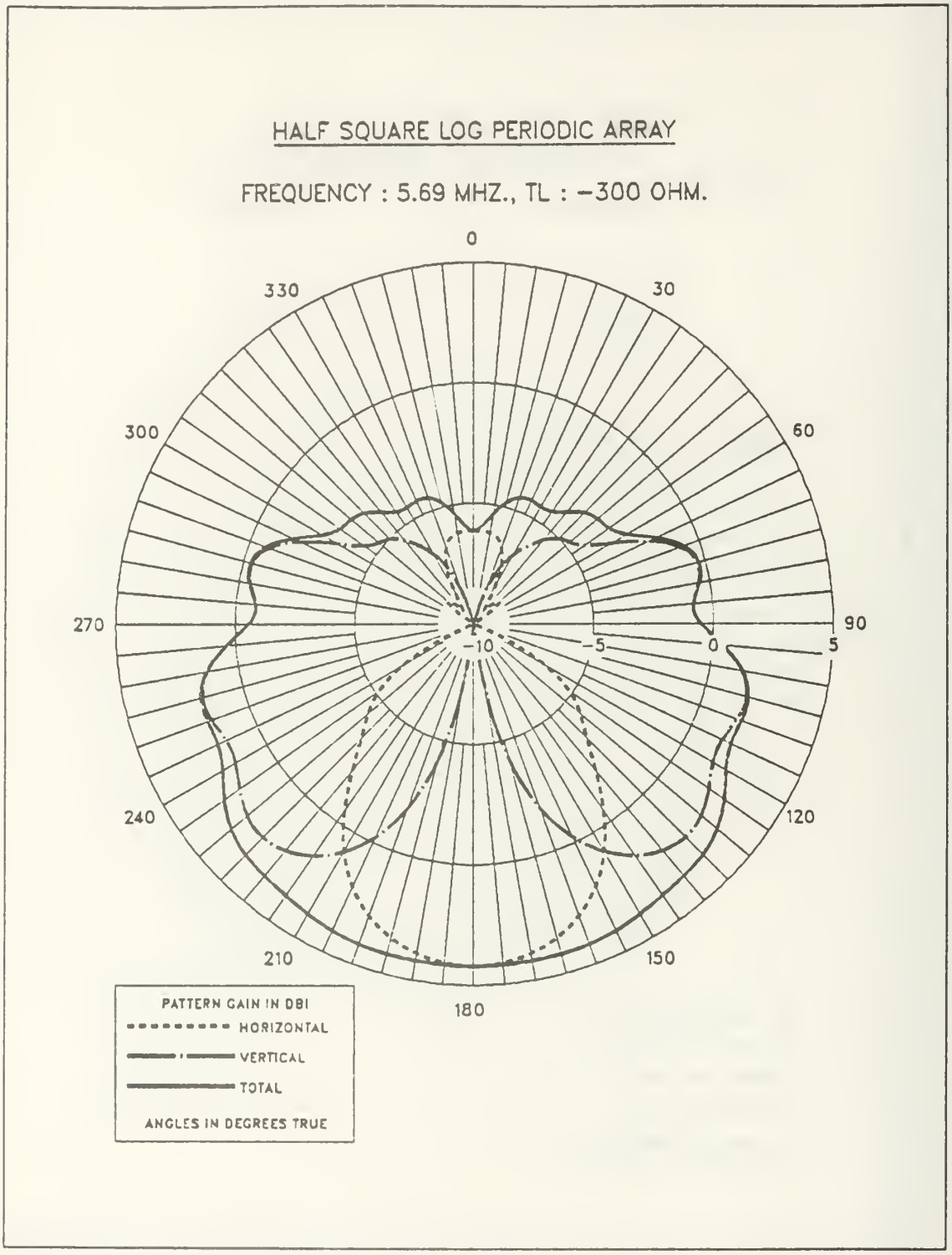

Figure C.7 Horizontal Pattern, Frequency: 5.69 MHz.

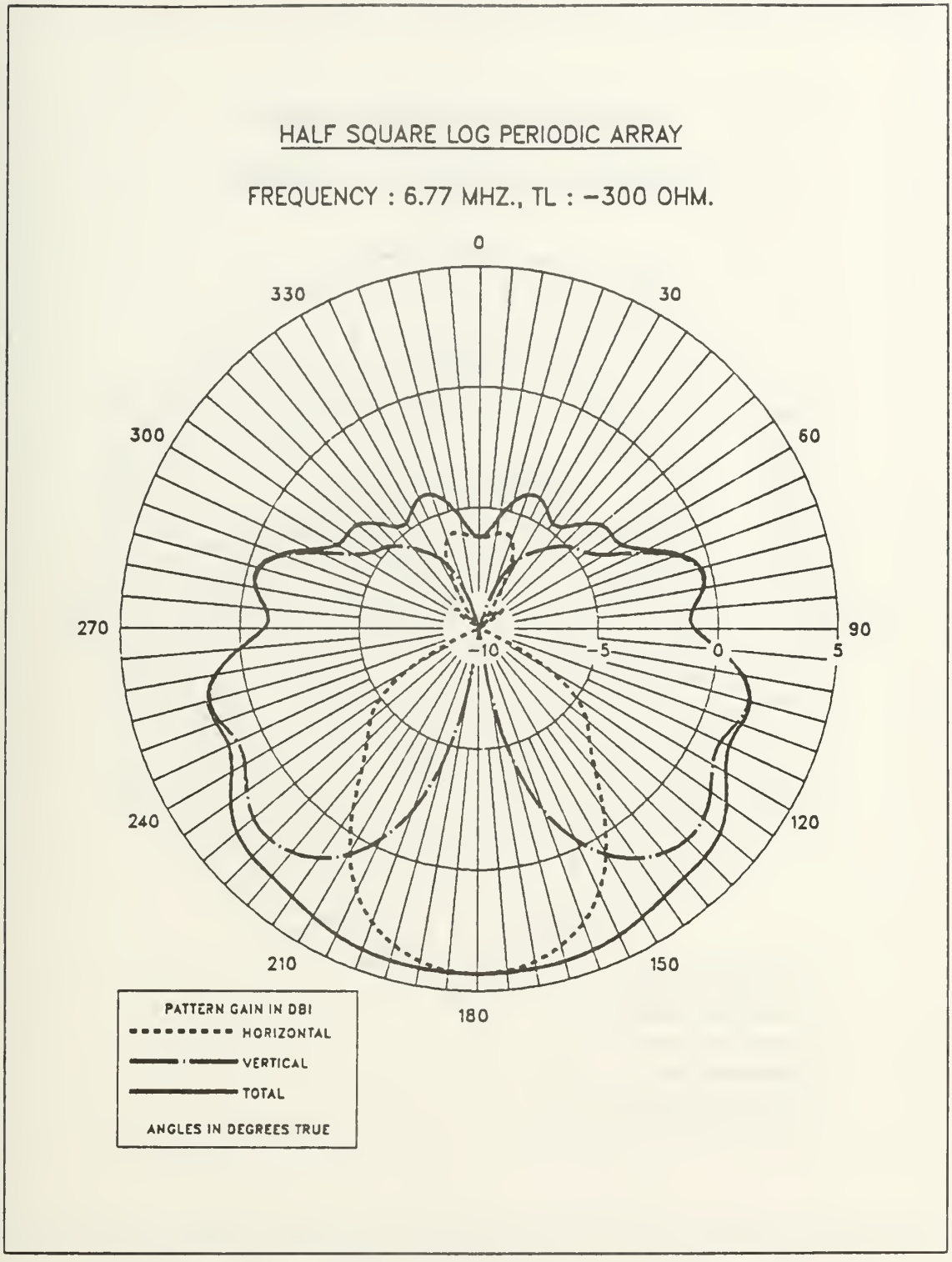

Figure C.8 Horizontal Pattern, Frequency: 6.77 MHz.

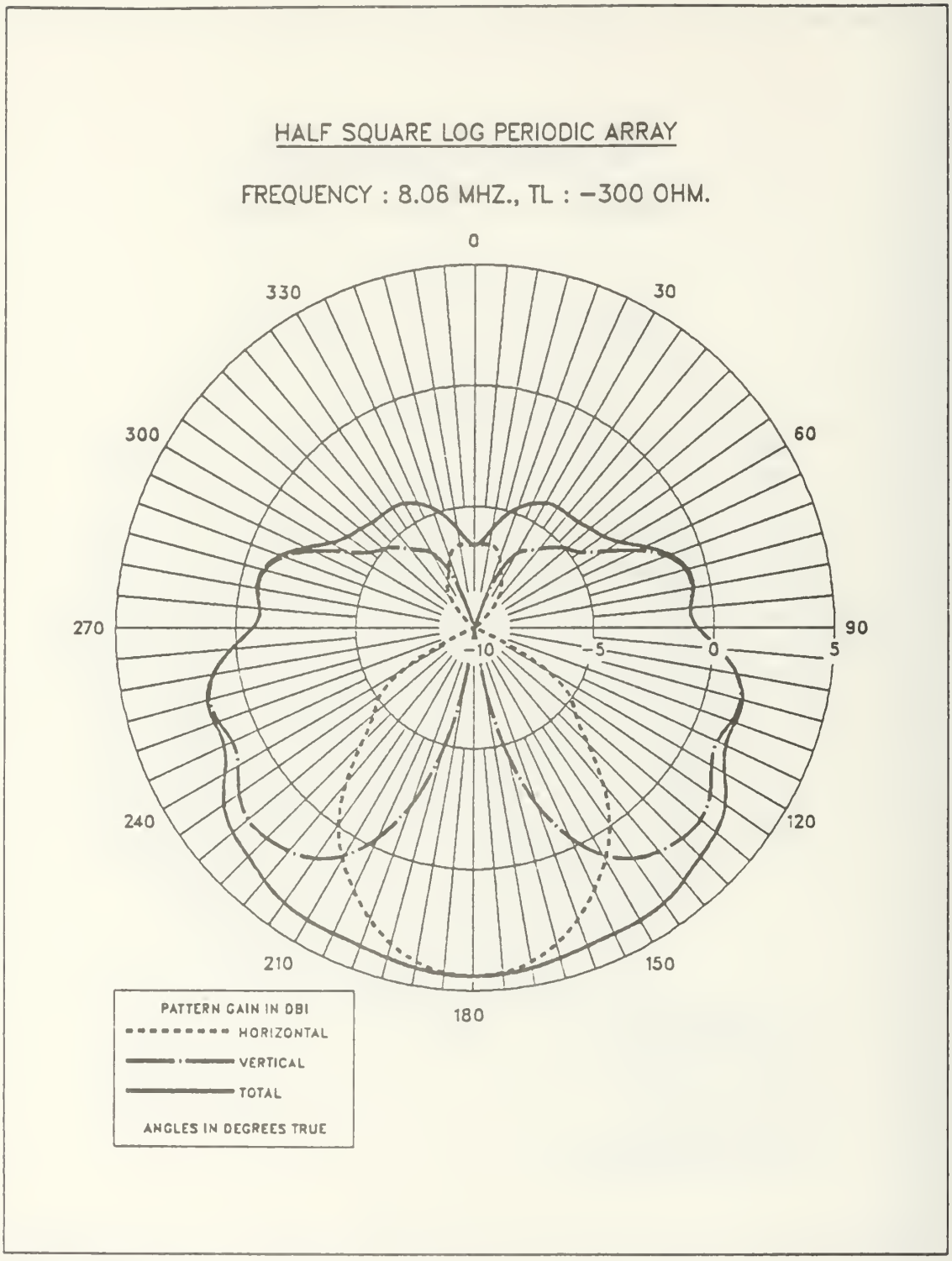

Figure C.9 Horizontal Pattern, Frequency: 8.06 MHz.

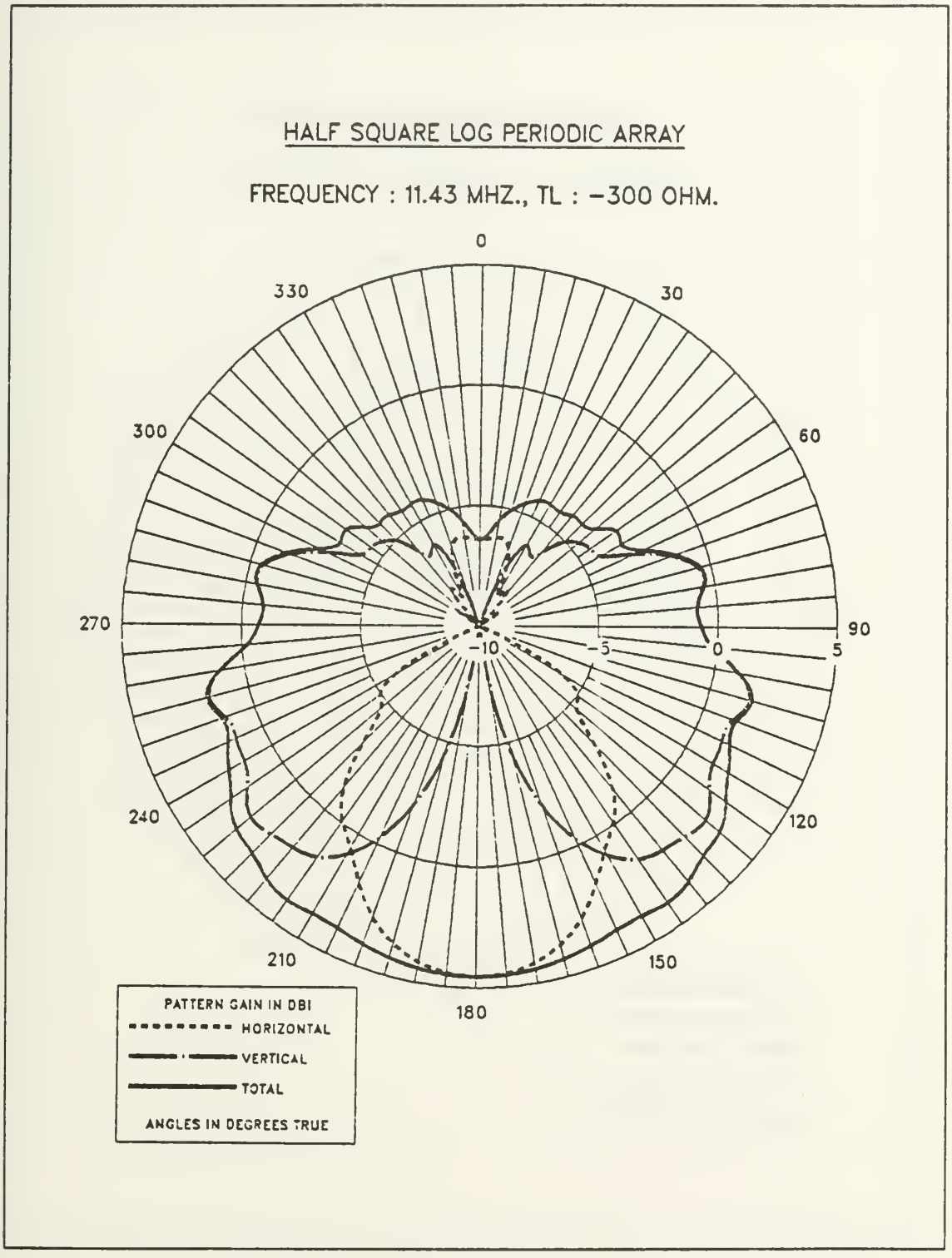

Figure C.10 Horizontal Pattern, Frequency: 11.43 MHz.

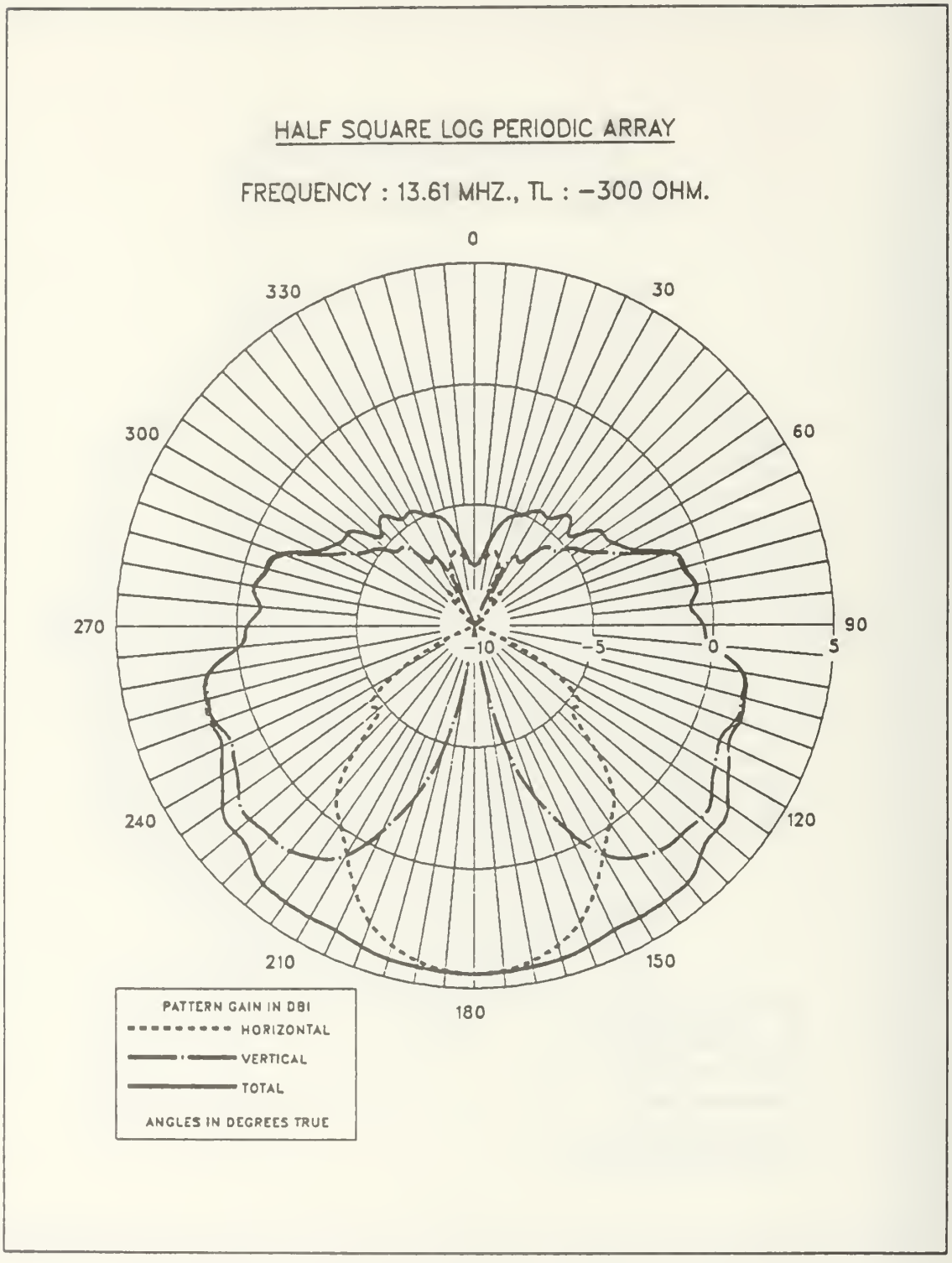

Figure C.11 Horizontal Pattern, Frequency: 13.61 MHz.

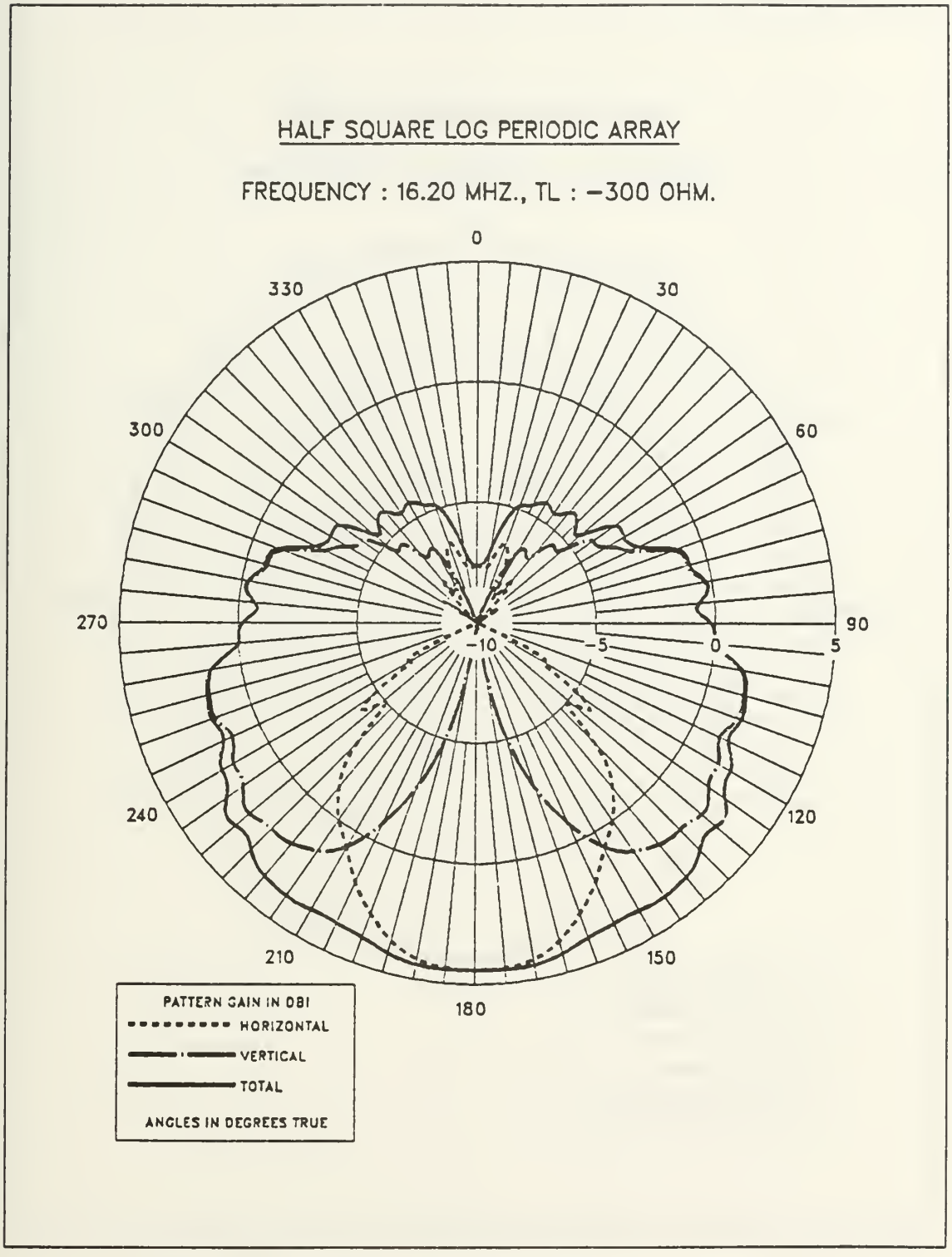

Figure C.12 Horizontal Pattern, Frequency: 16.20 MHz.

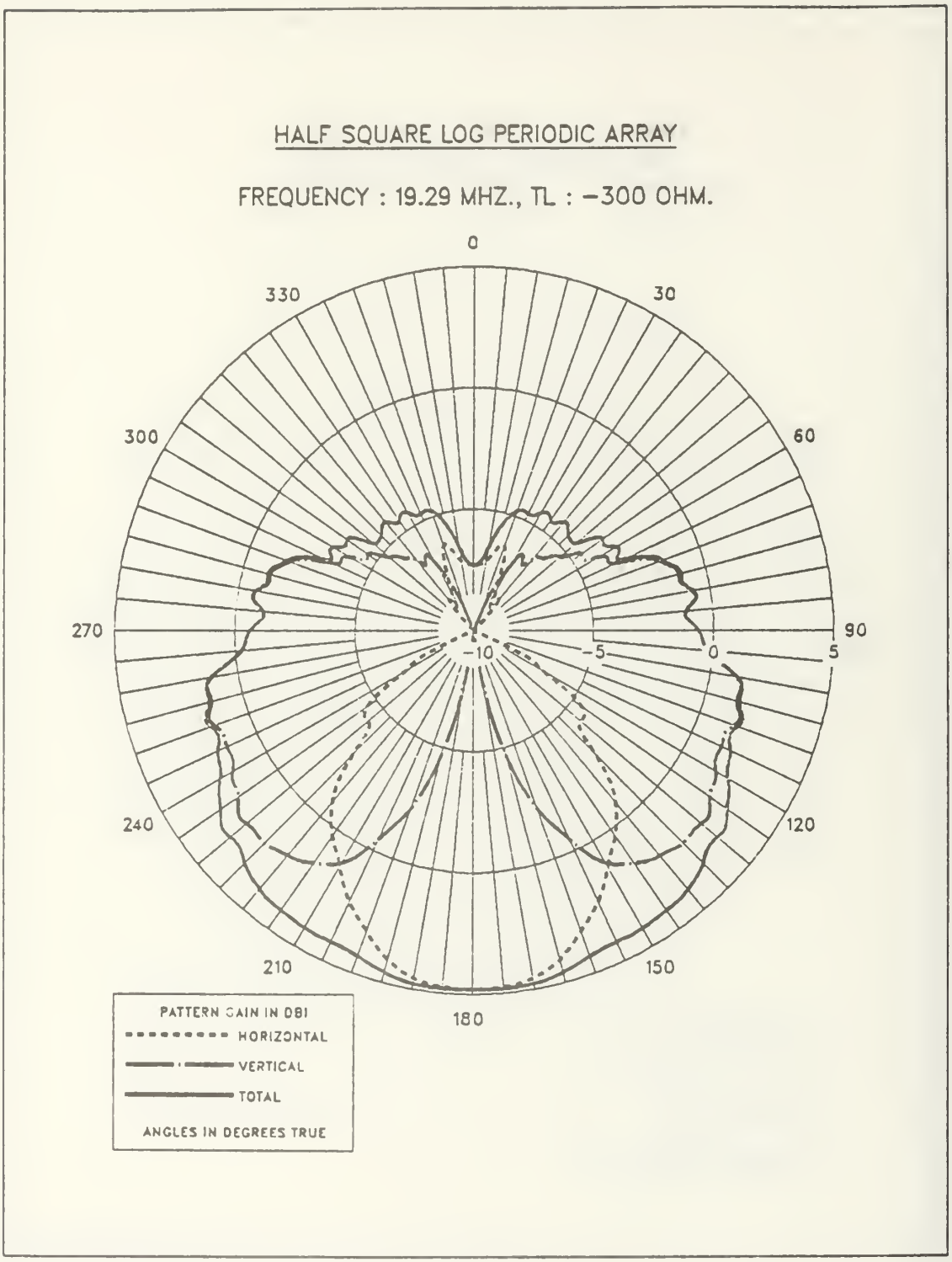

Figure C.13 Horizontal Pattern, Frequency: 19.29 MHz.

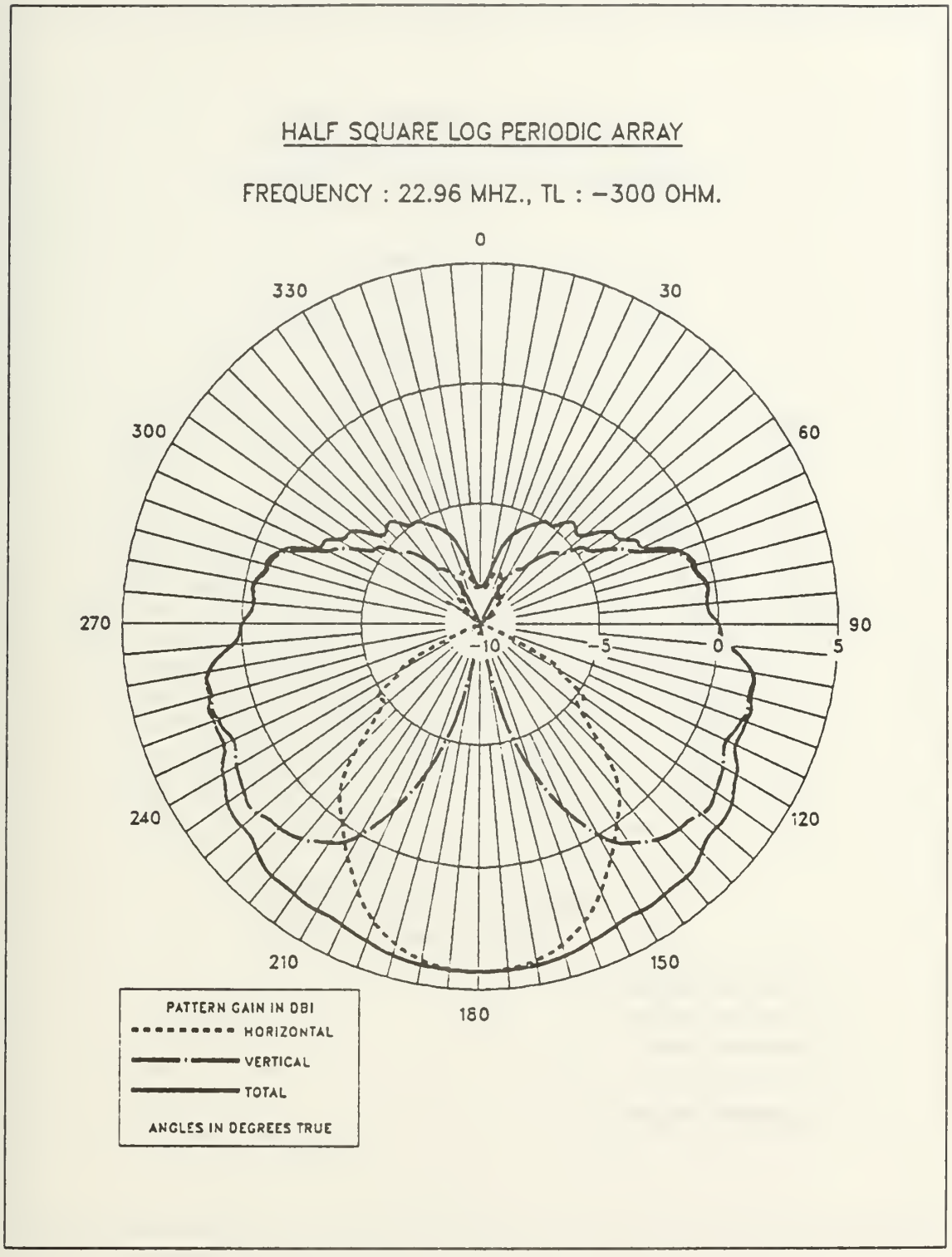

Figure C.14 Horizontal Pattern, Frequency: 22.96 MHz.

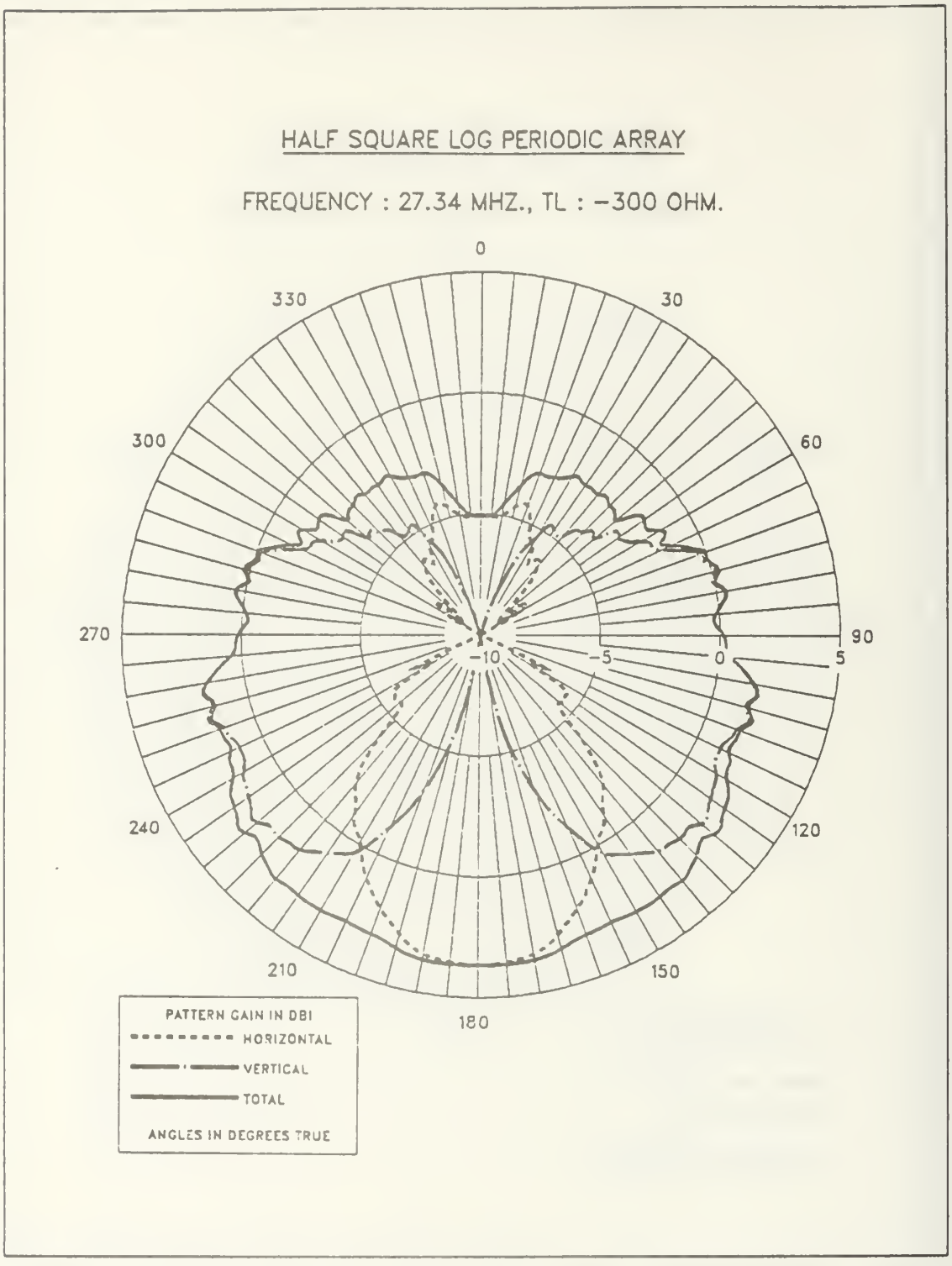

Figure C.15 Horizontal Pattern, Frequency: 27.34 MHz.

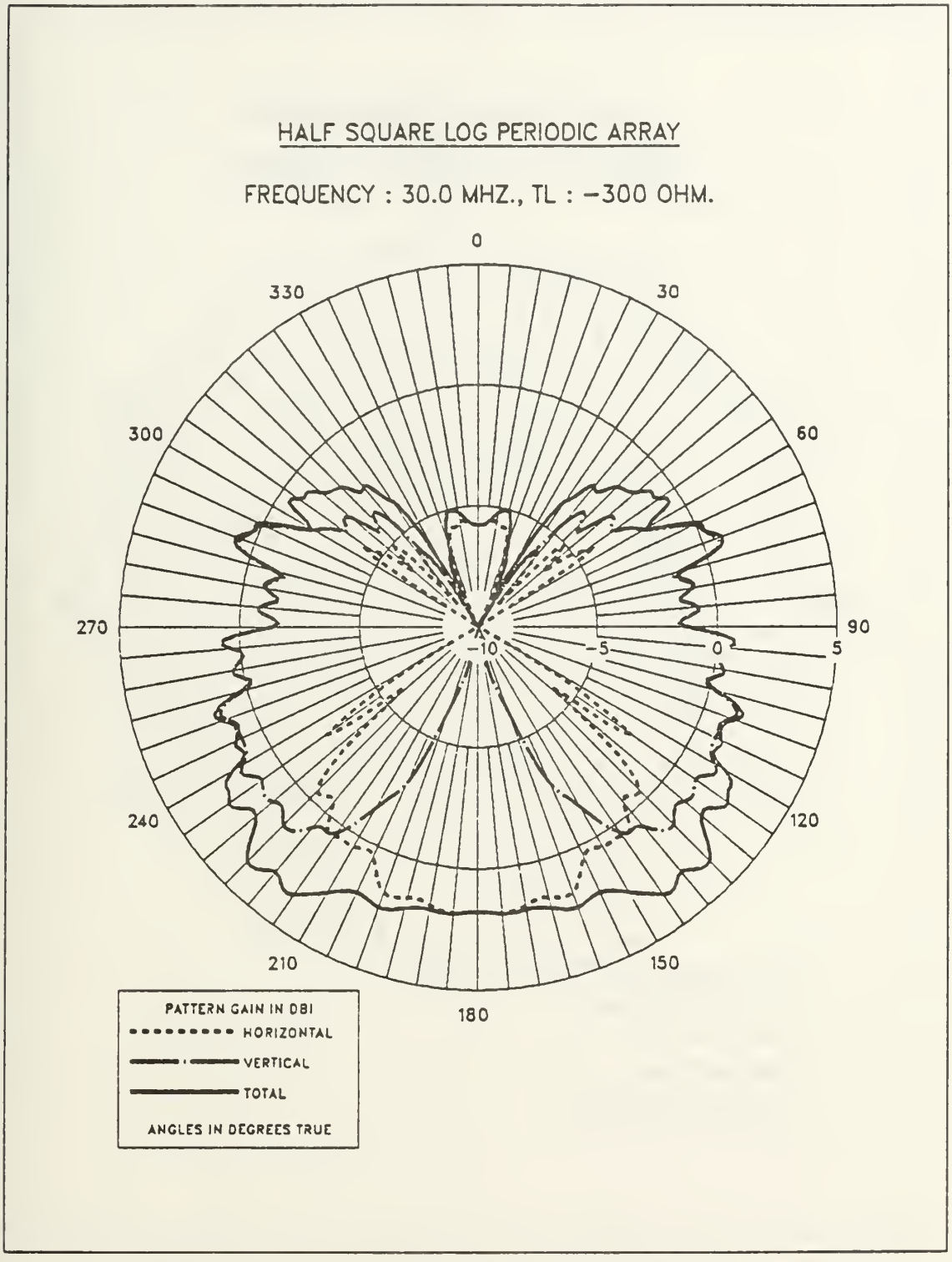

Figure C.16 Horizontal Pattern, Frequency: 30.0 MHz.

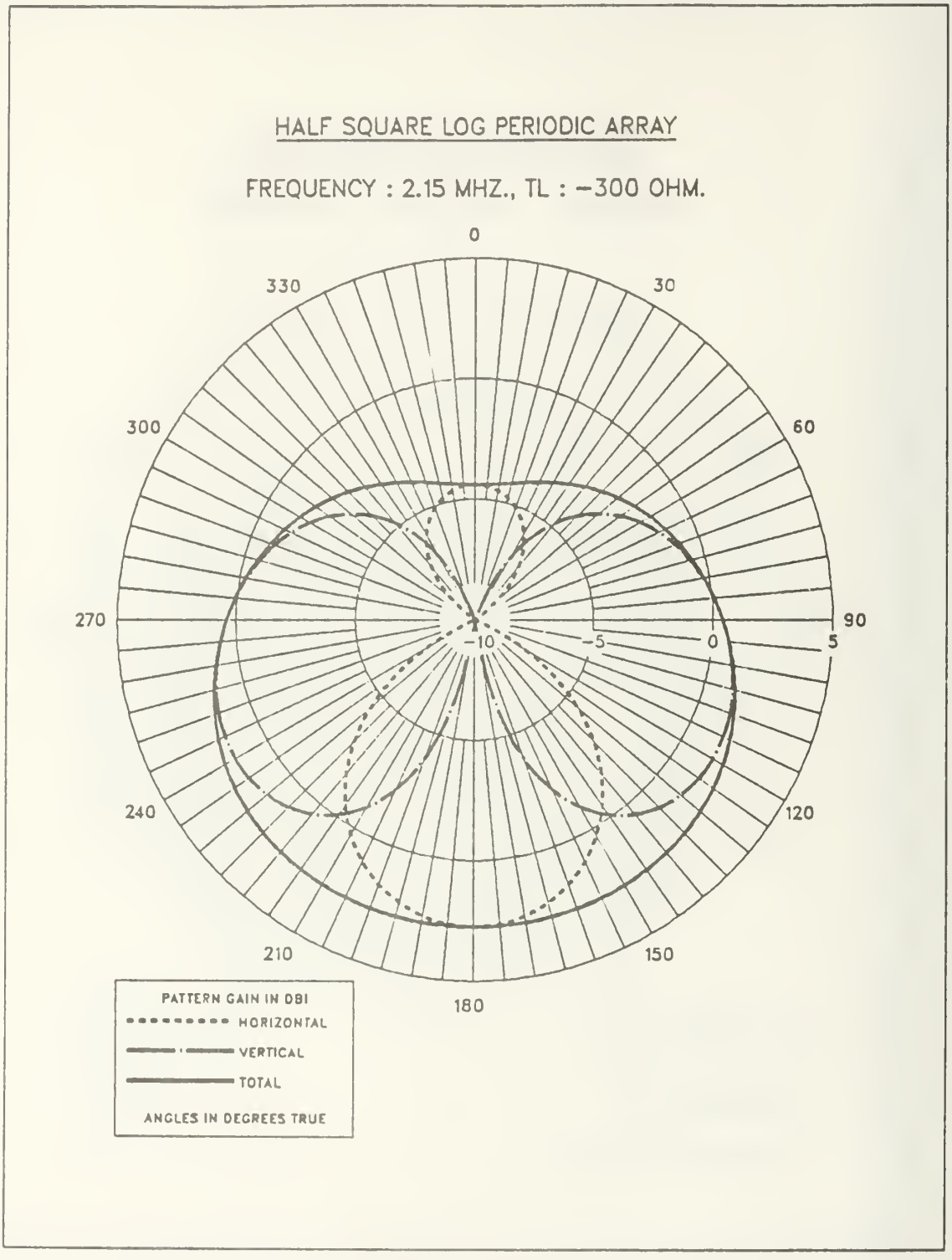

Figure C.17 Horizontal Pattern, Frequency: 2.15 MHz.

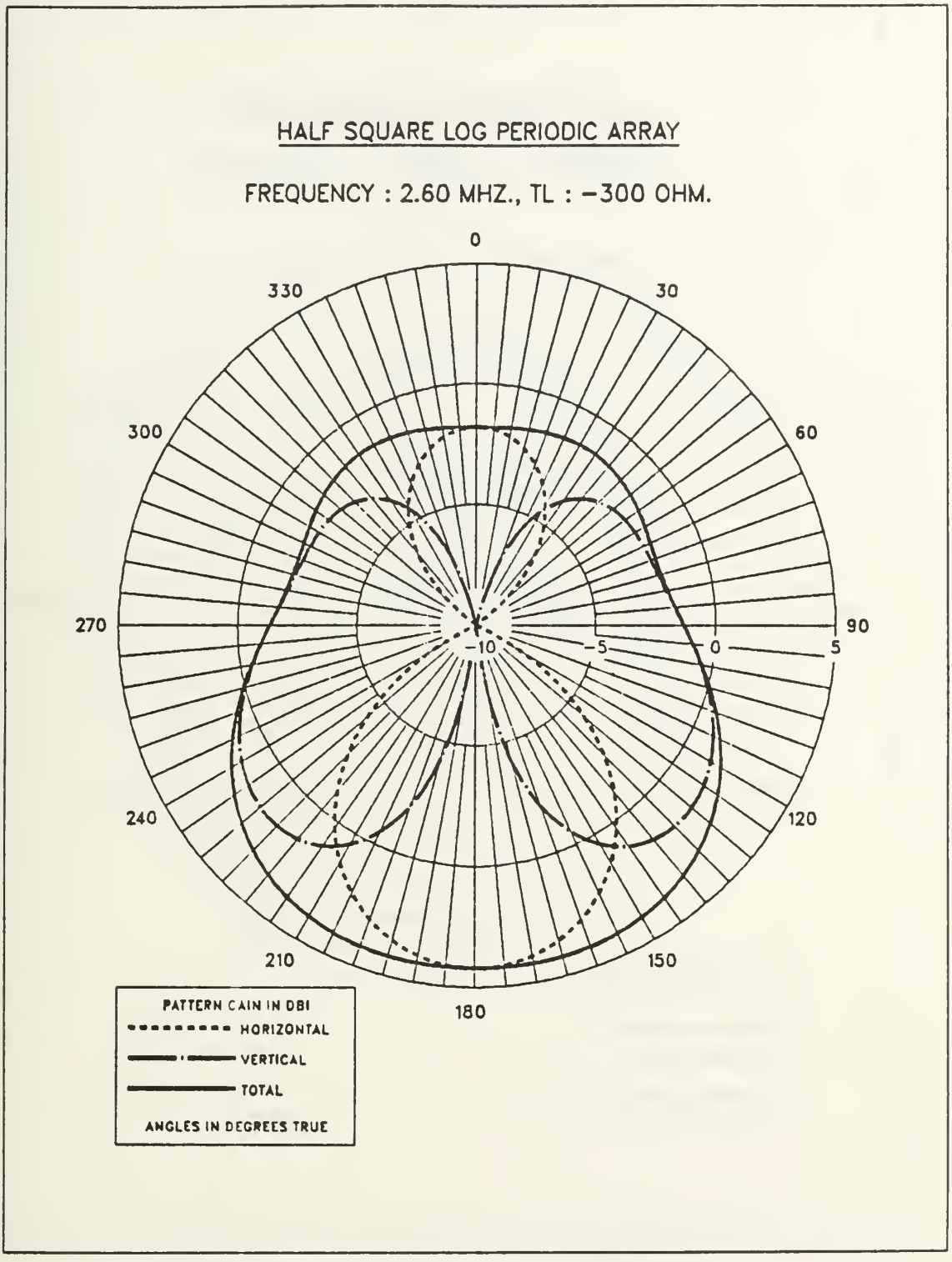

Figure C.18 Horizontal Pattern, Frequency: 2.60 MHz.

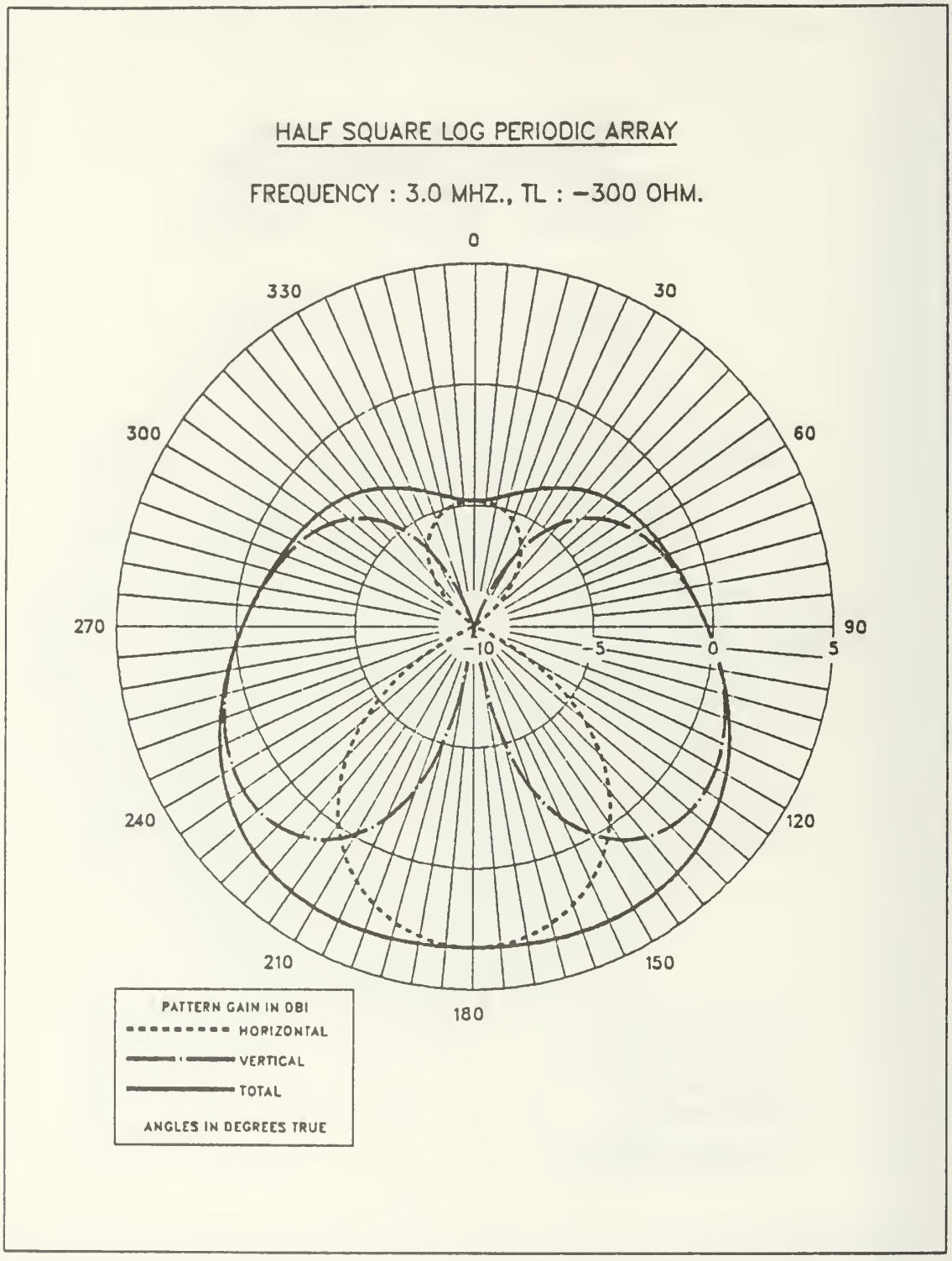

Figure C.19 Horizontal Pattern, Frequency: 3.0 MHz.

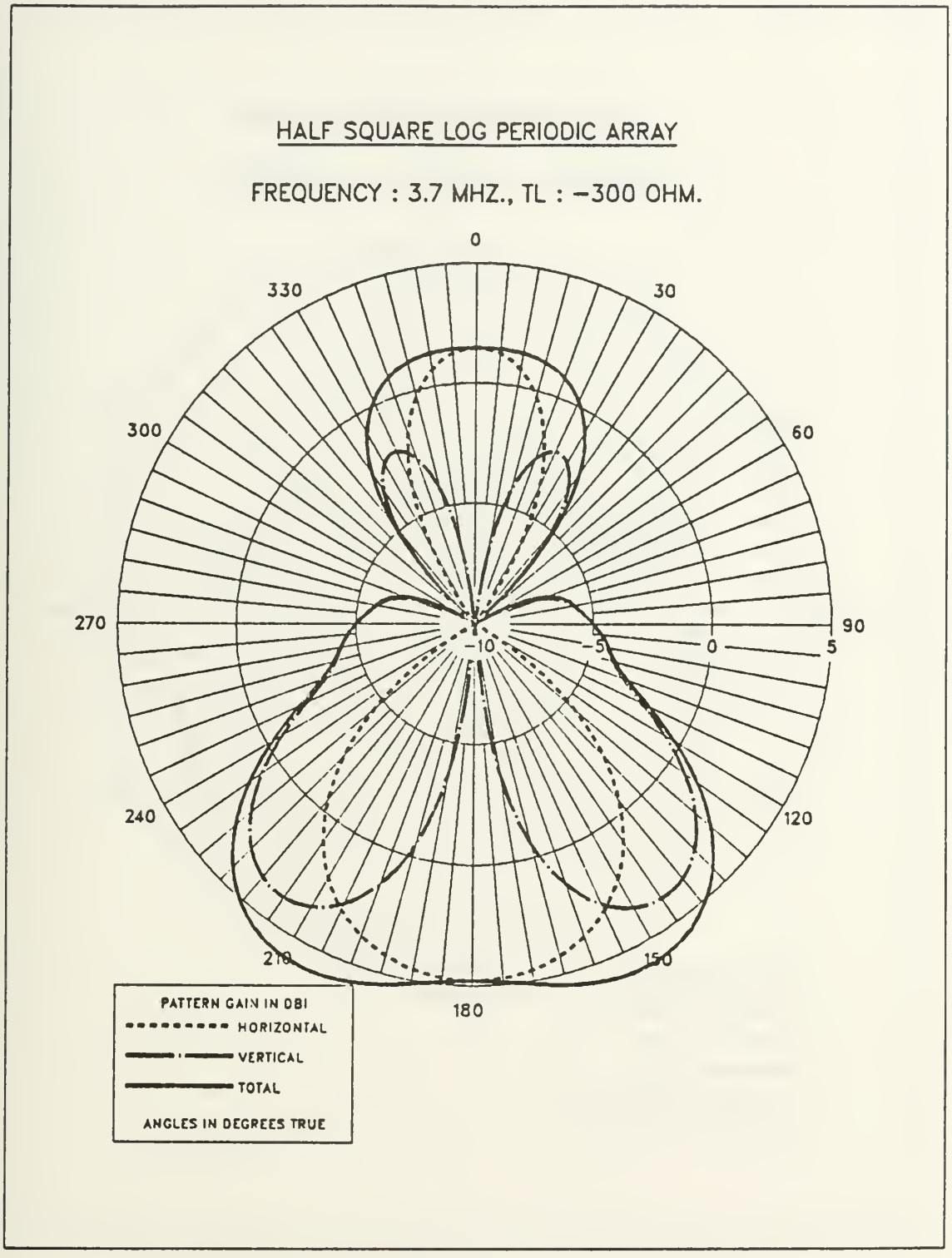

Figure C.20 Horizontal Pattern, Frequency: 3.7 MHz.

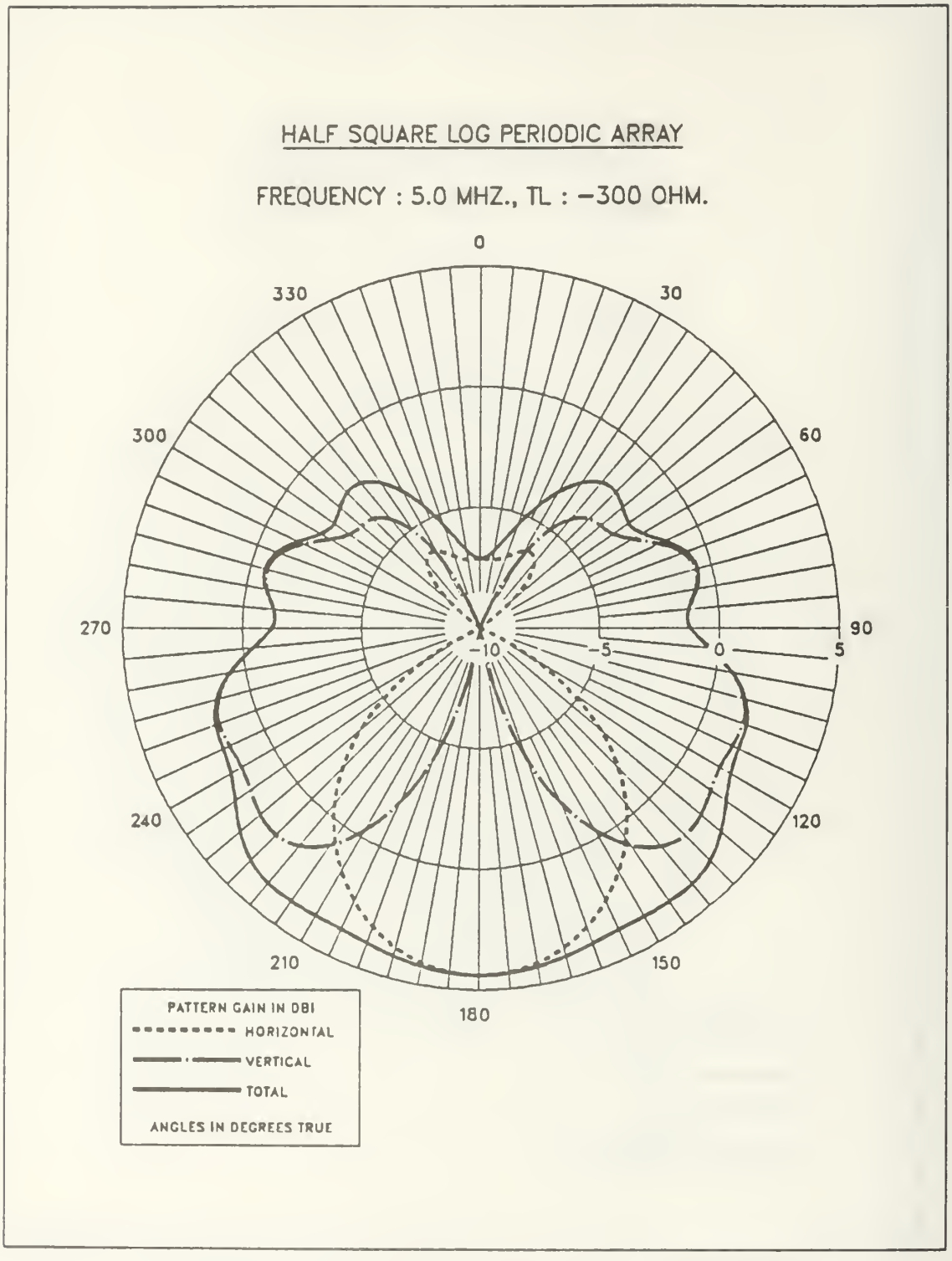

Figure C.21 Horizontal Pattern, Frequency: 5.0 MHz.

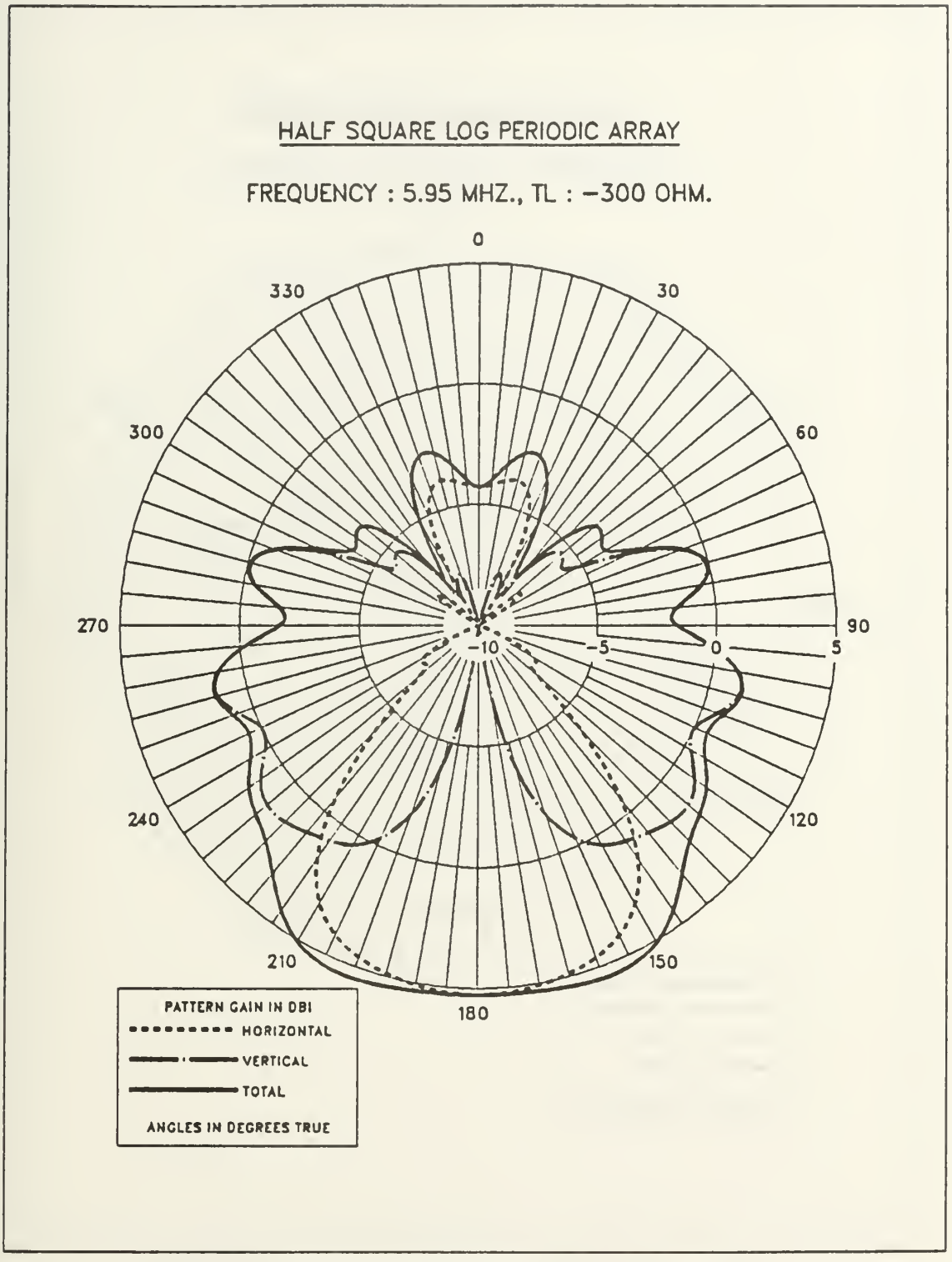

Figure C.22 Horizontal Pattern, Frequency: 5.95 MHz.

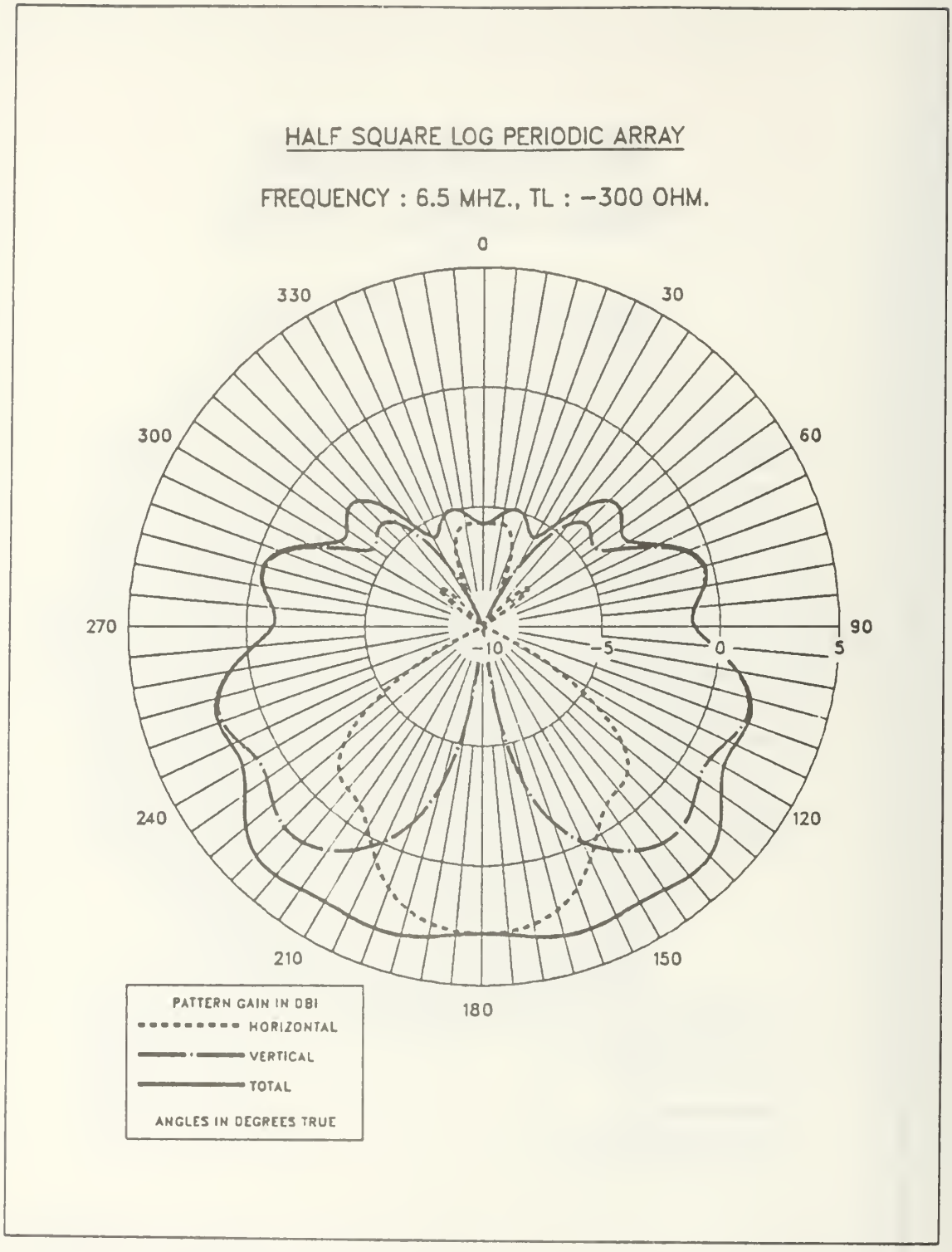

Figure C.23 Horizontal Pattern, Frequency: 6.5 MHz.

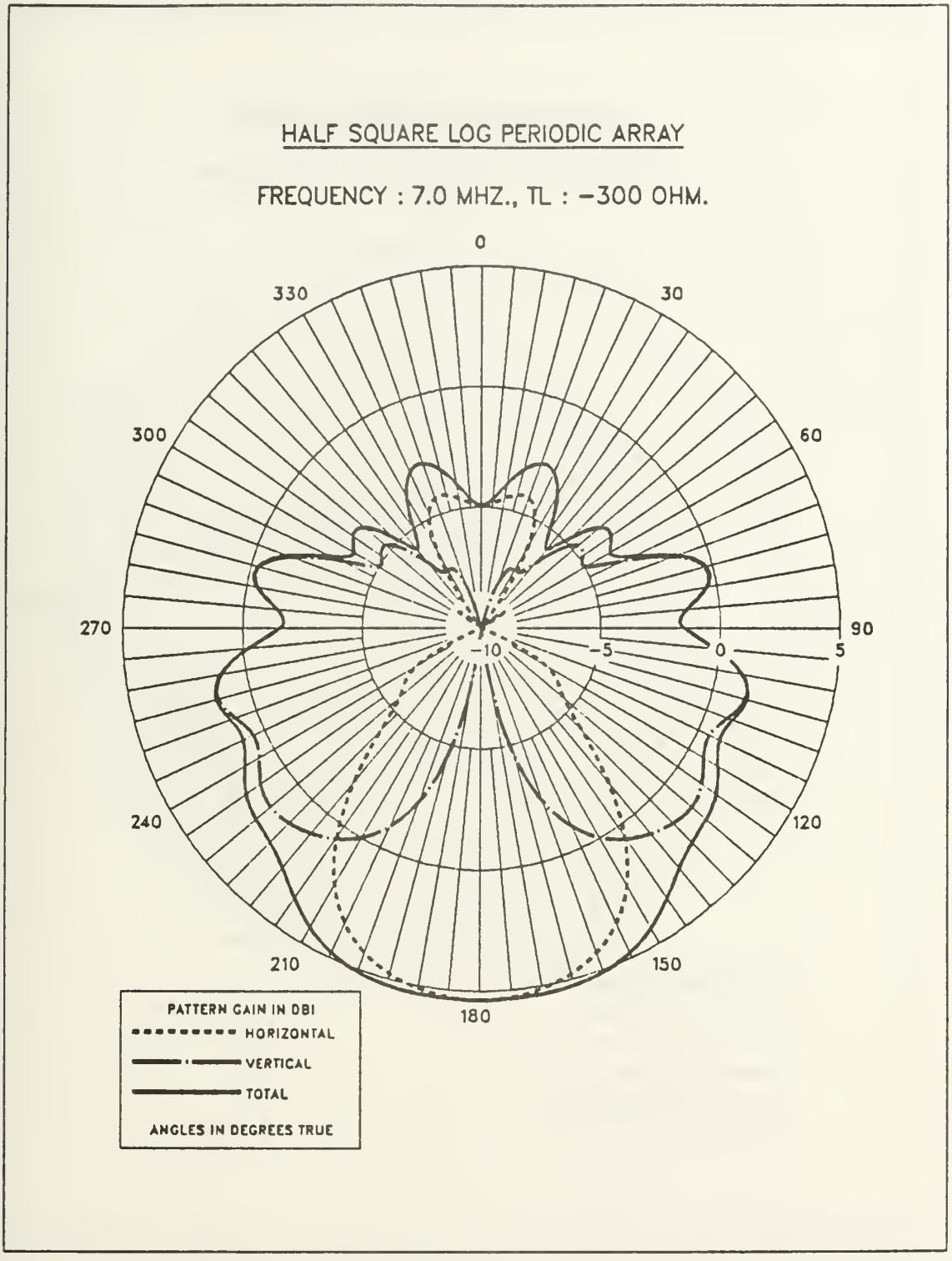

Figure C.24 Horizontal Pattern, Frequency: 7.0 MHz.

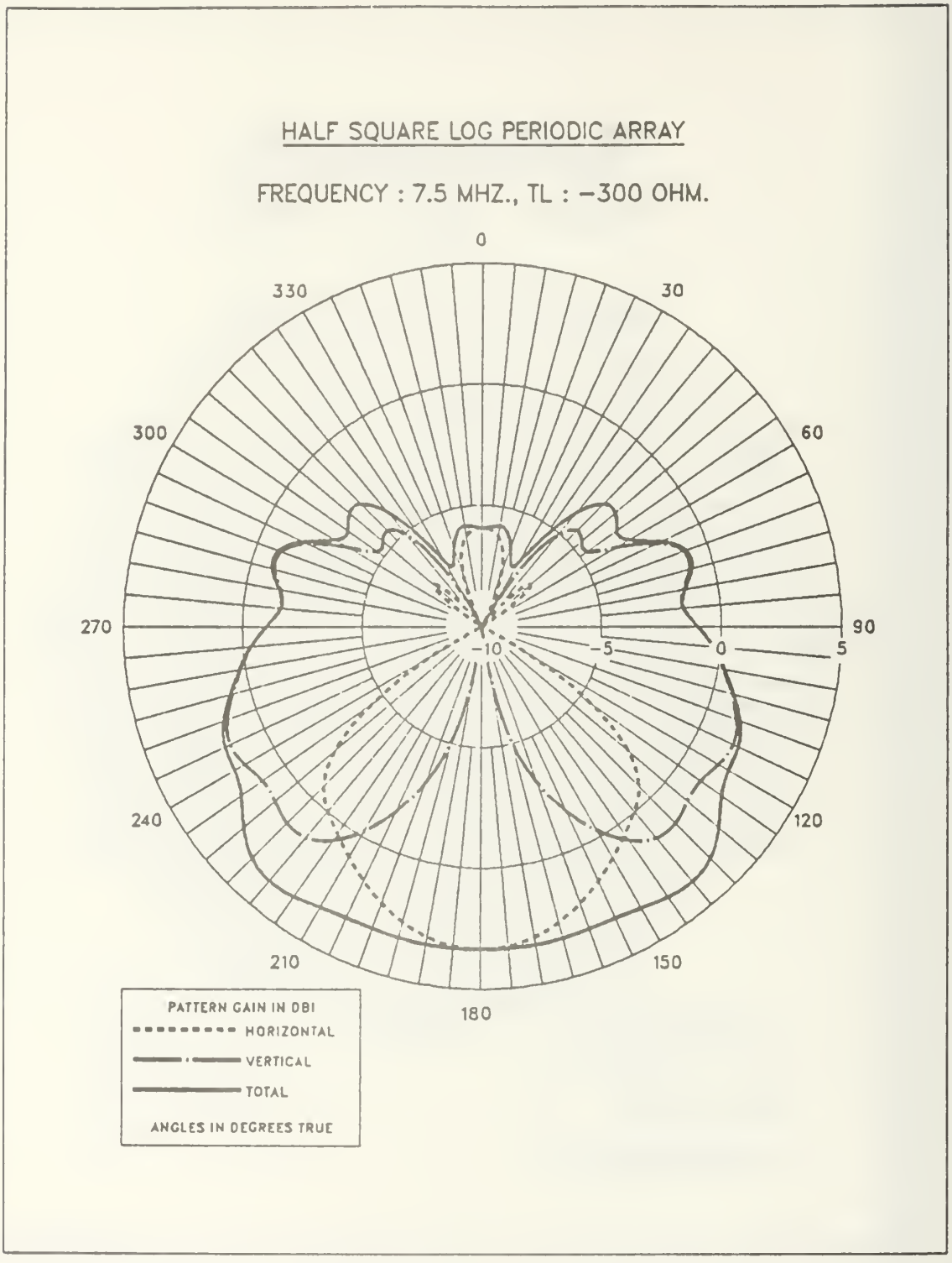

Figure C.25 Horizontal Pattern, Frequency: 7.5 MHz.

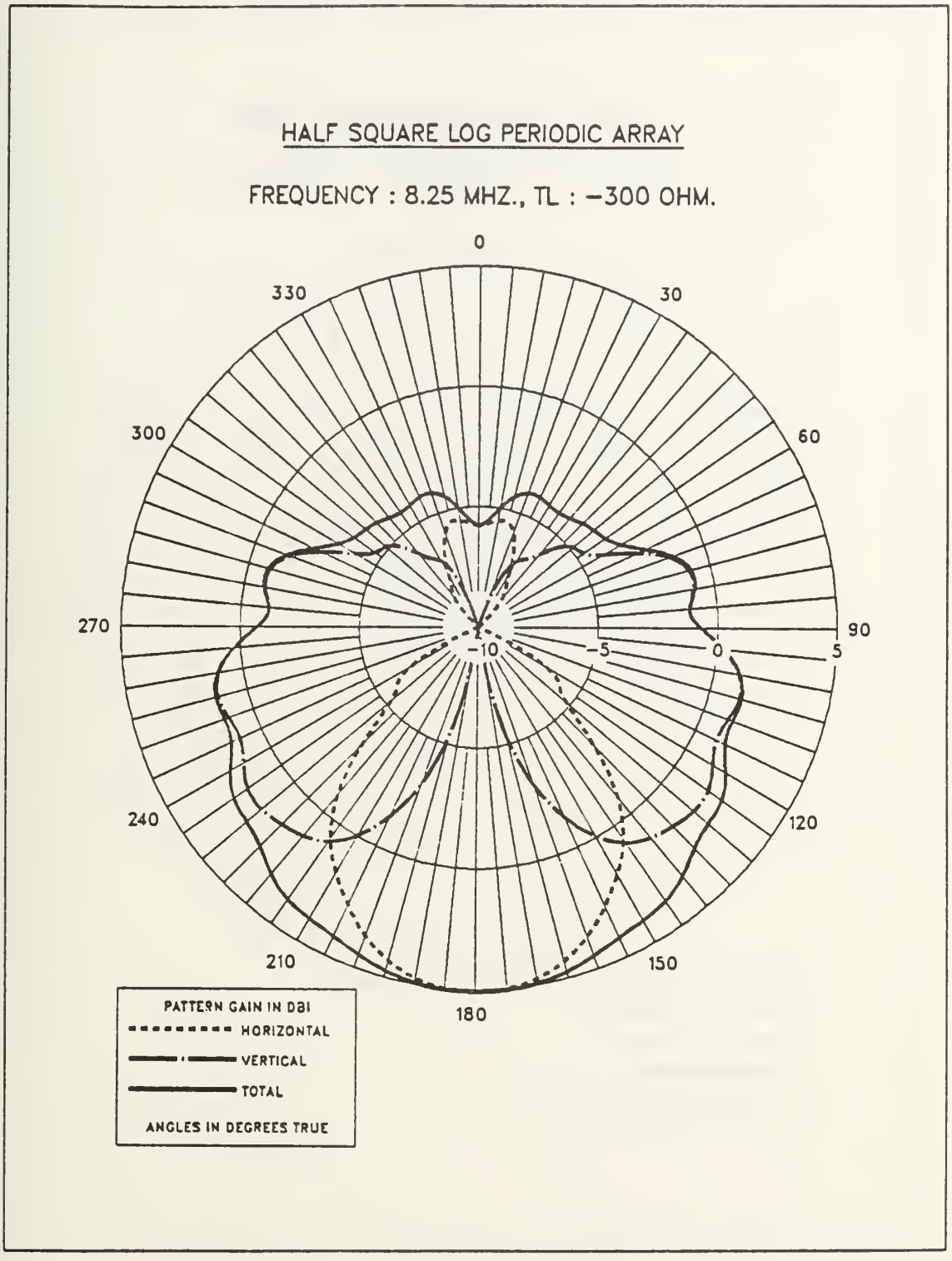

Figure C.26 Horizontal Pattern, Frequency: 8.25 MHz.

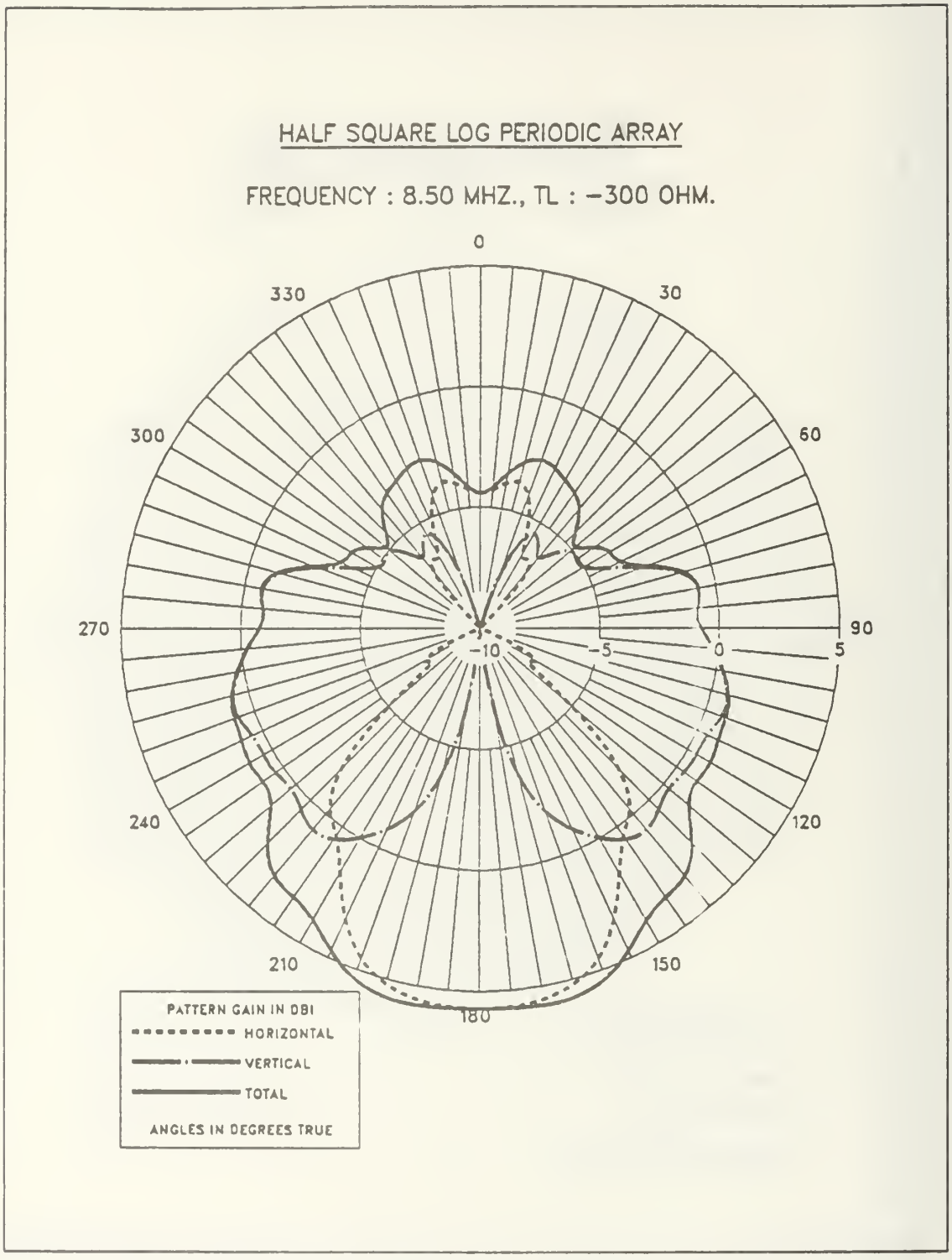

Figure C.27 Horizontal Pattern, Frequency: 8.5 MHz.

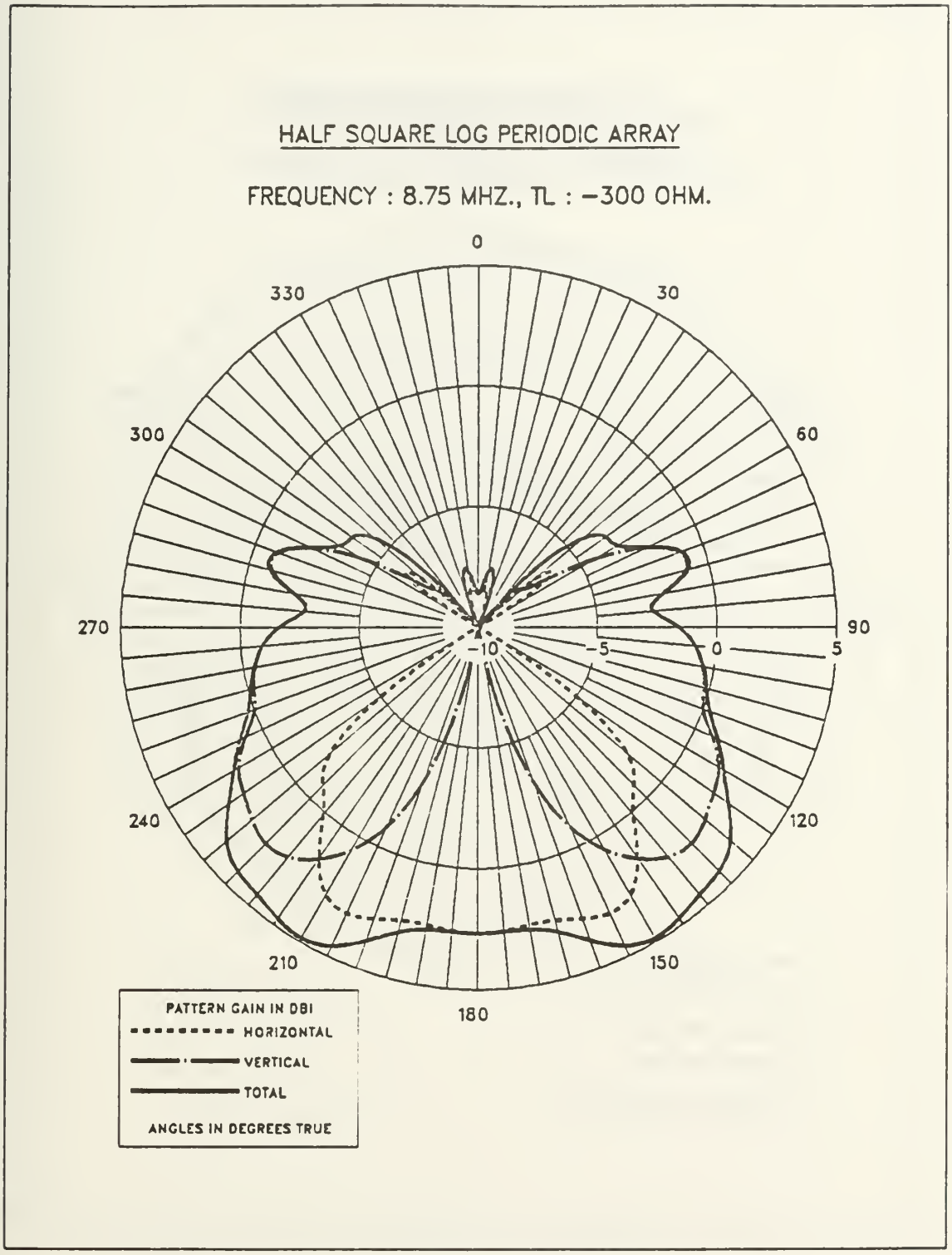

Figure C.28 Horizontal Pattern, Frequency: 8.75 MHz.

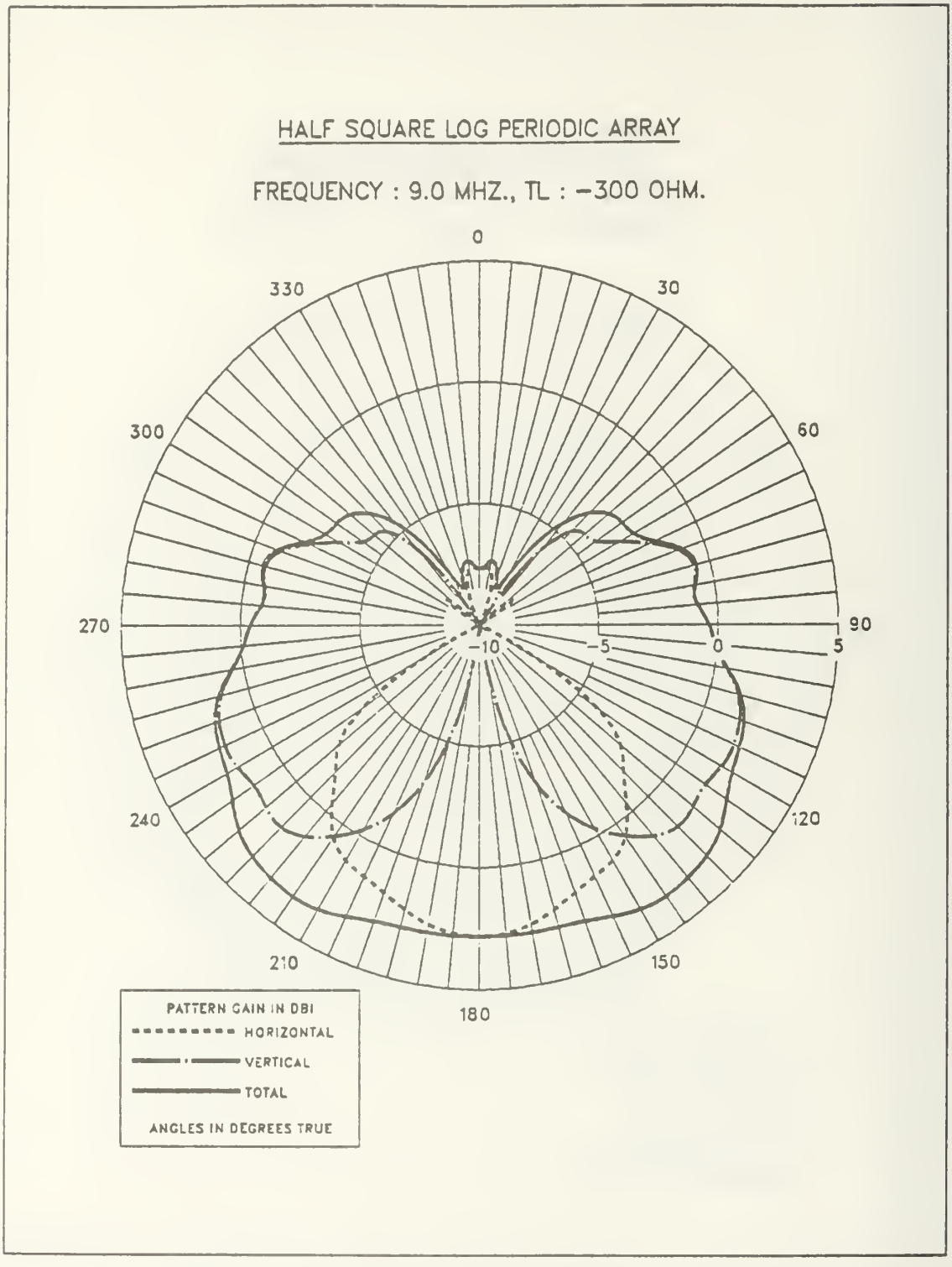

Figure C.29 Horizontal Pattern, Frequency: 9.0 MHz.

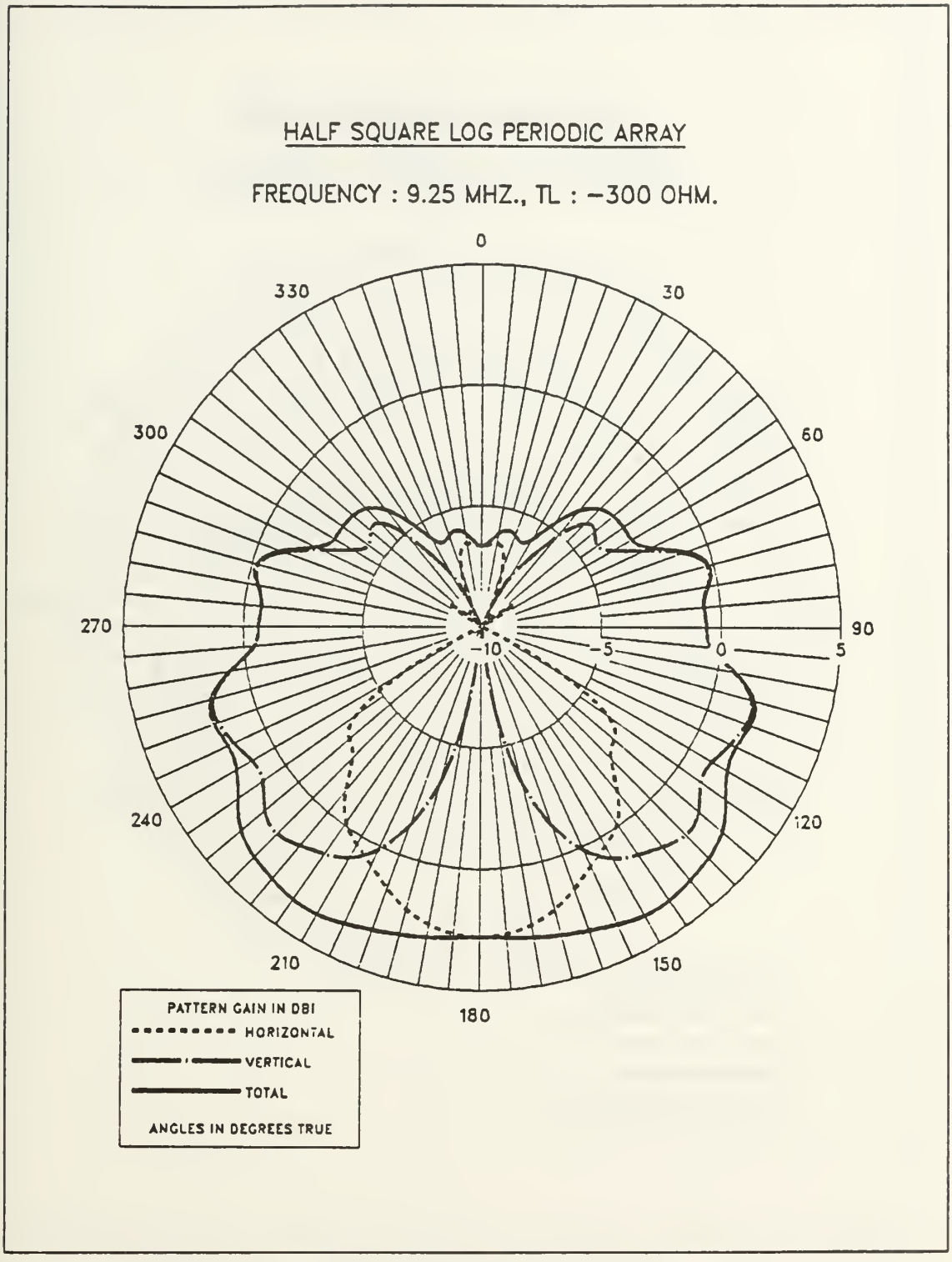

Figure C.30 Horizontal Pattern, Frequency: 9.25 MHz.

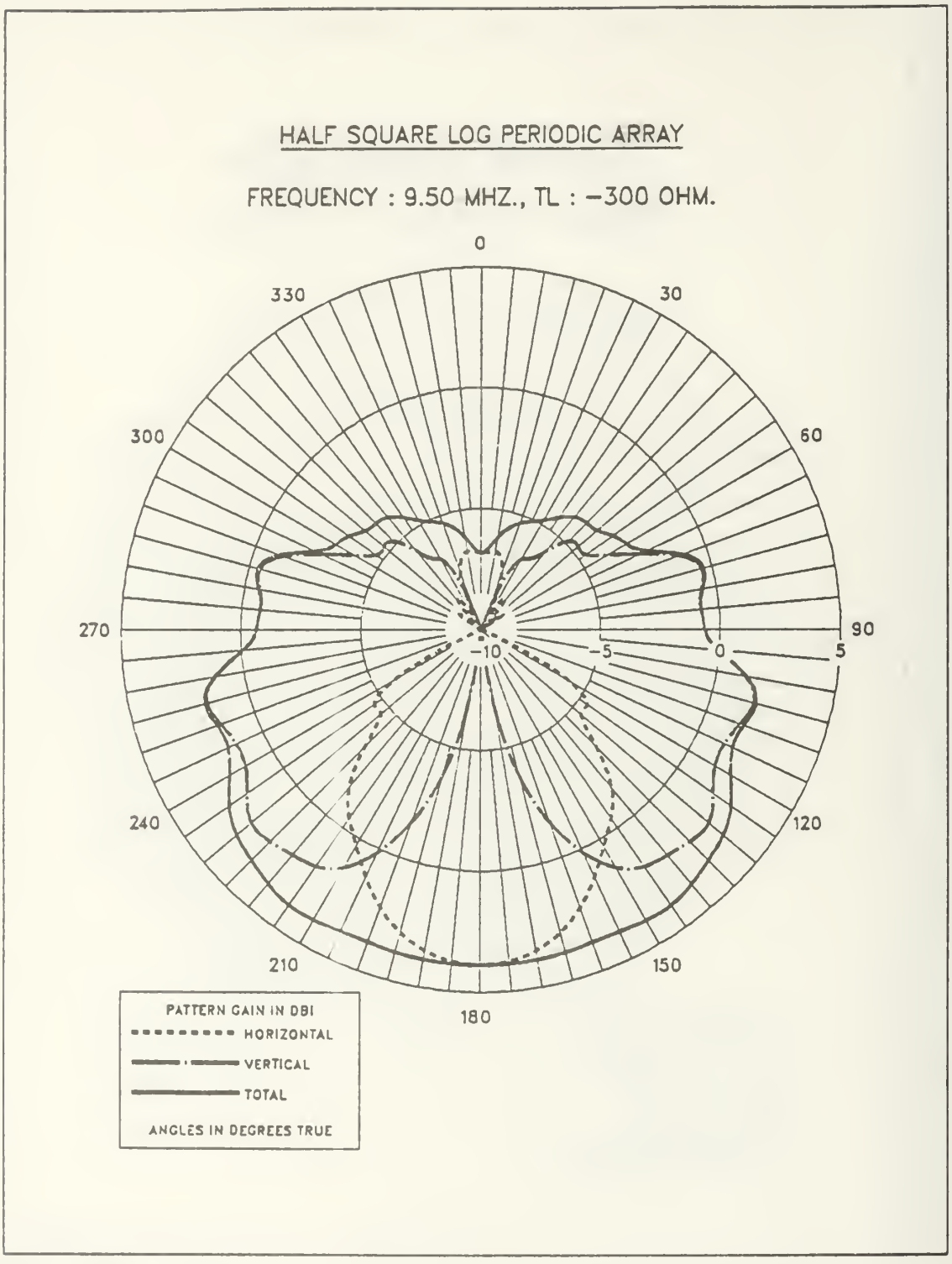

Figure C.31 Horizontal Pattern, Frequency: 9.5 MHz.

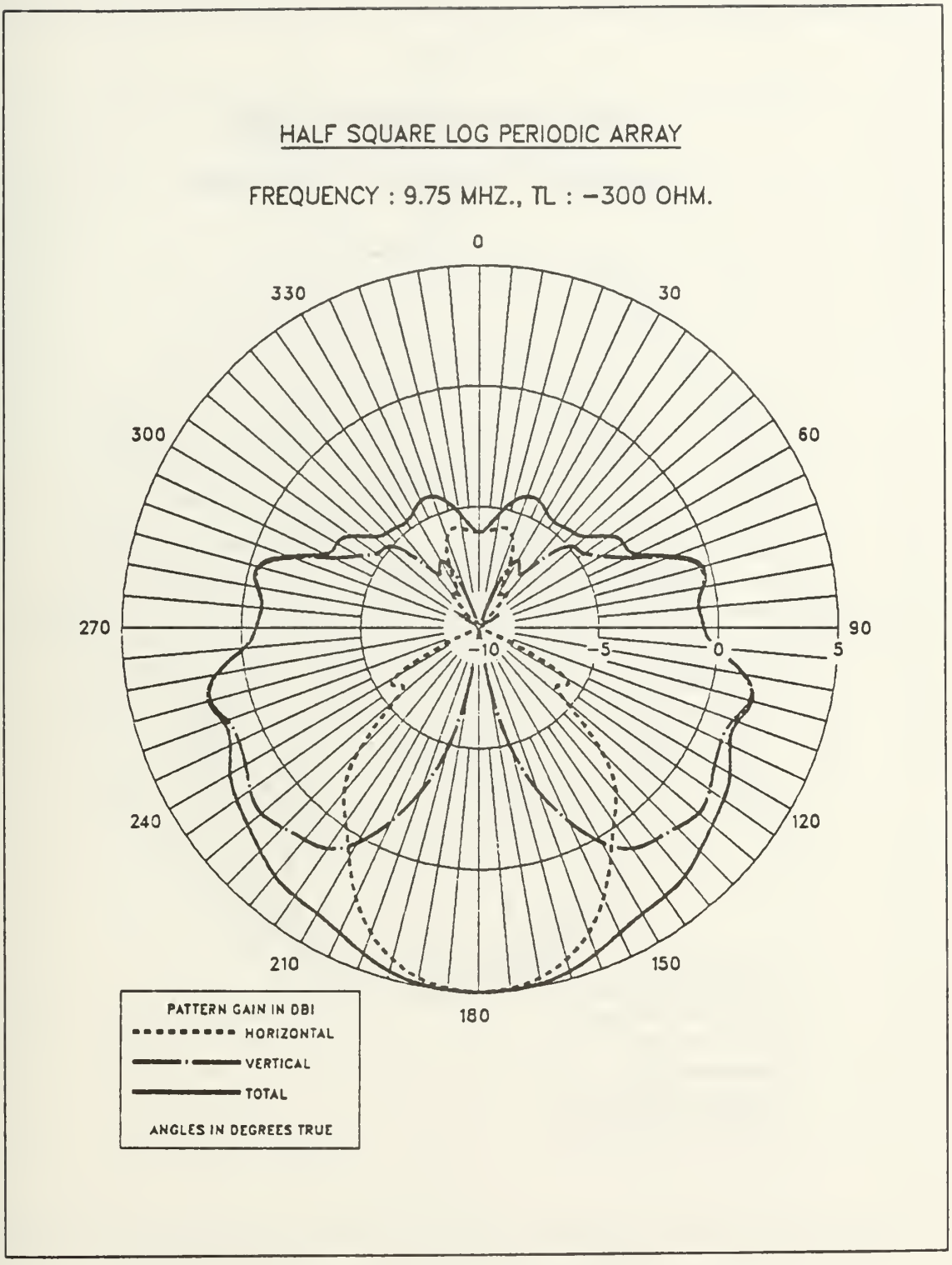

Figure C.32 Horizontal Pattern, Frequency: 9.75 MHz.

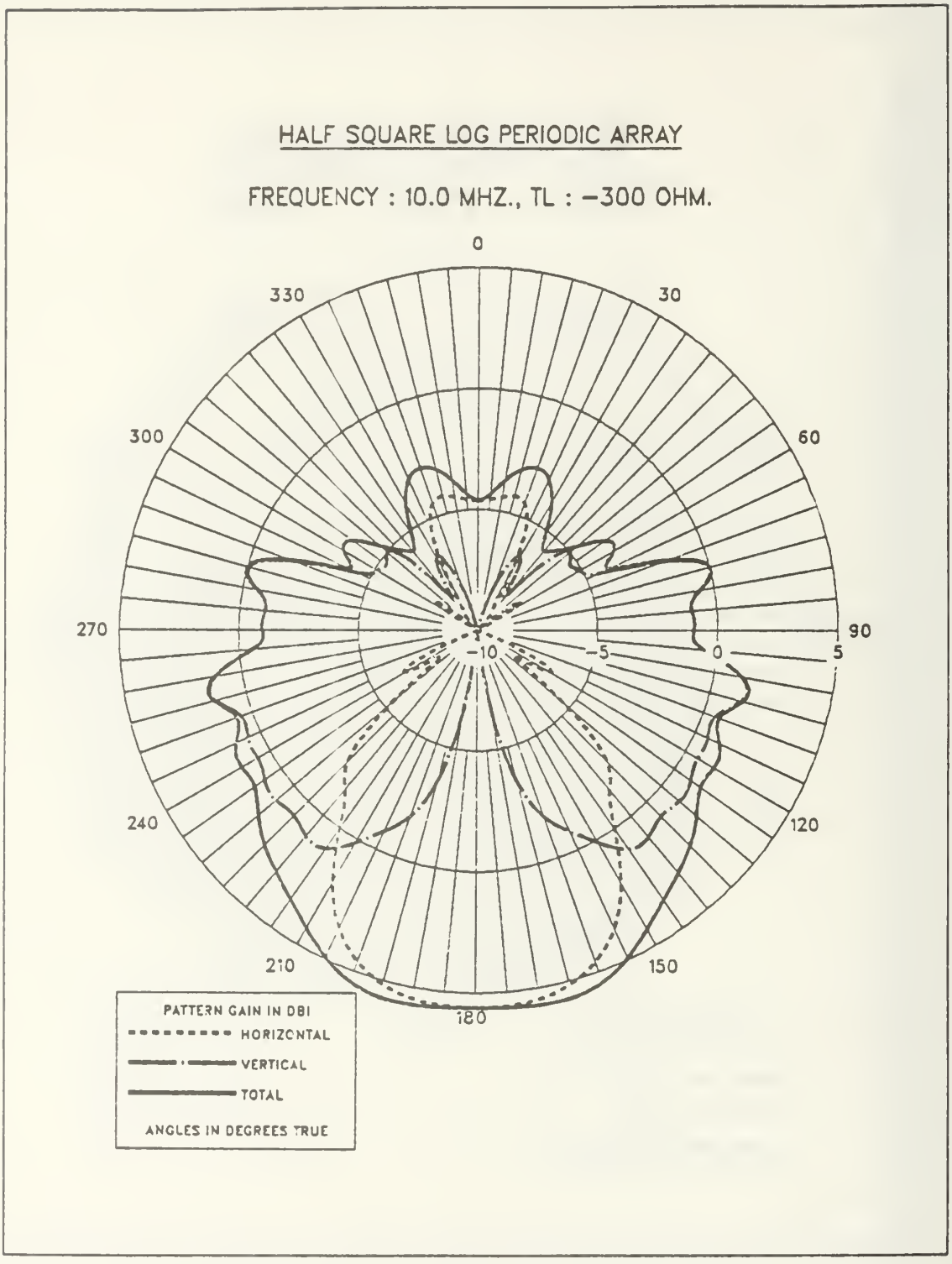

Figure C.33 Horizontal Pattern, Frequency: 10.0 MHz.

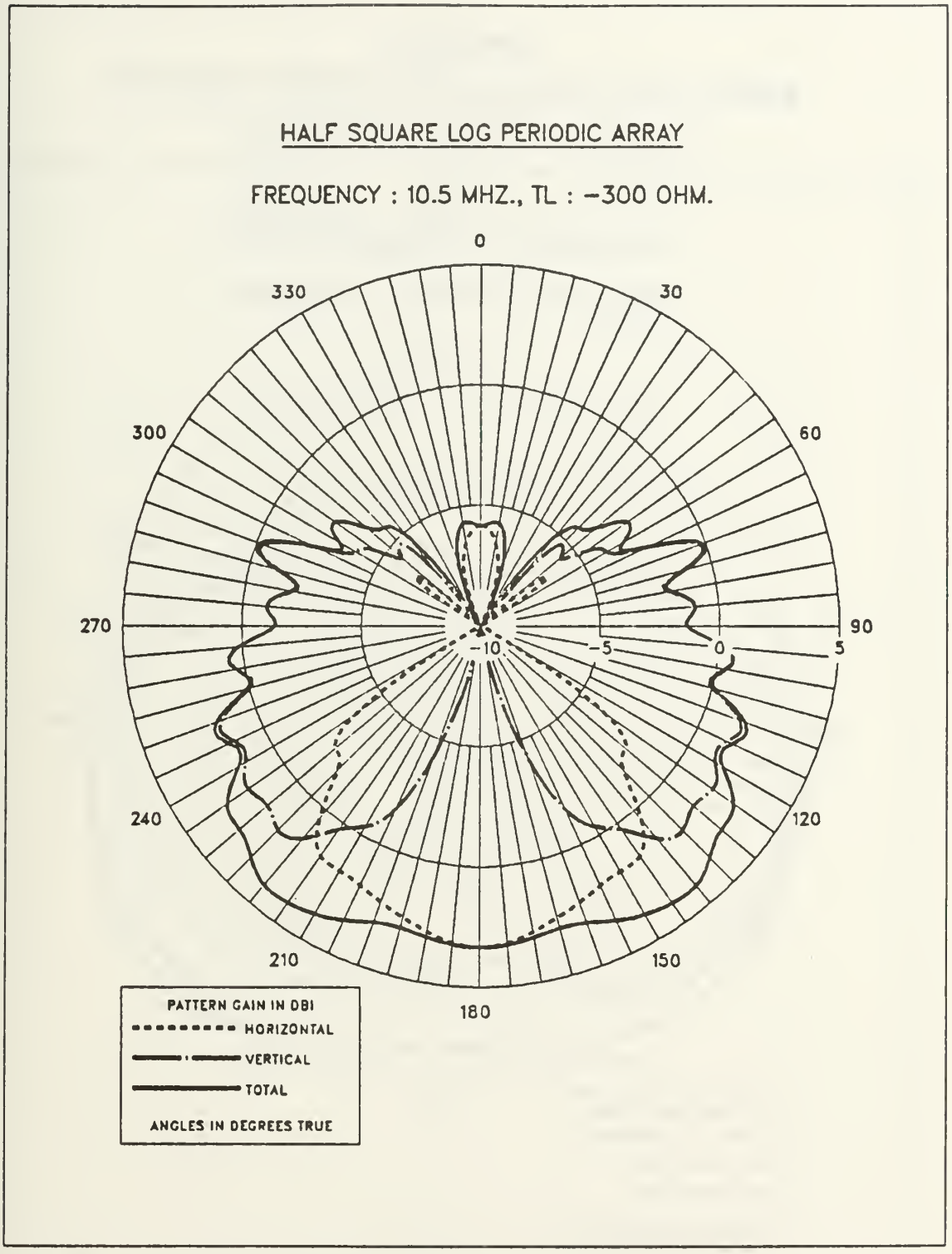

Figure C.34 Horizontal Pattern, Frequency: 10.5 MHz.

APPENDIX D
RADIATION PATTERNS OVER PERFECT GROUND

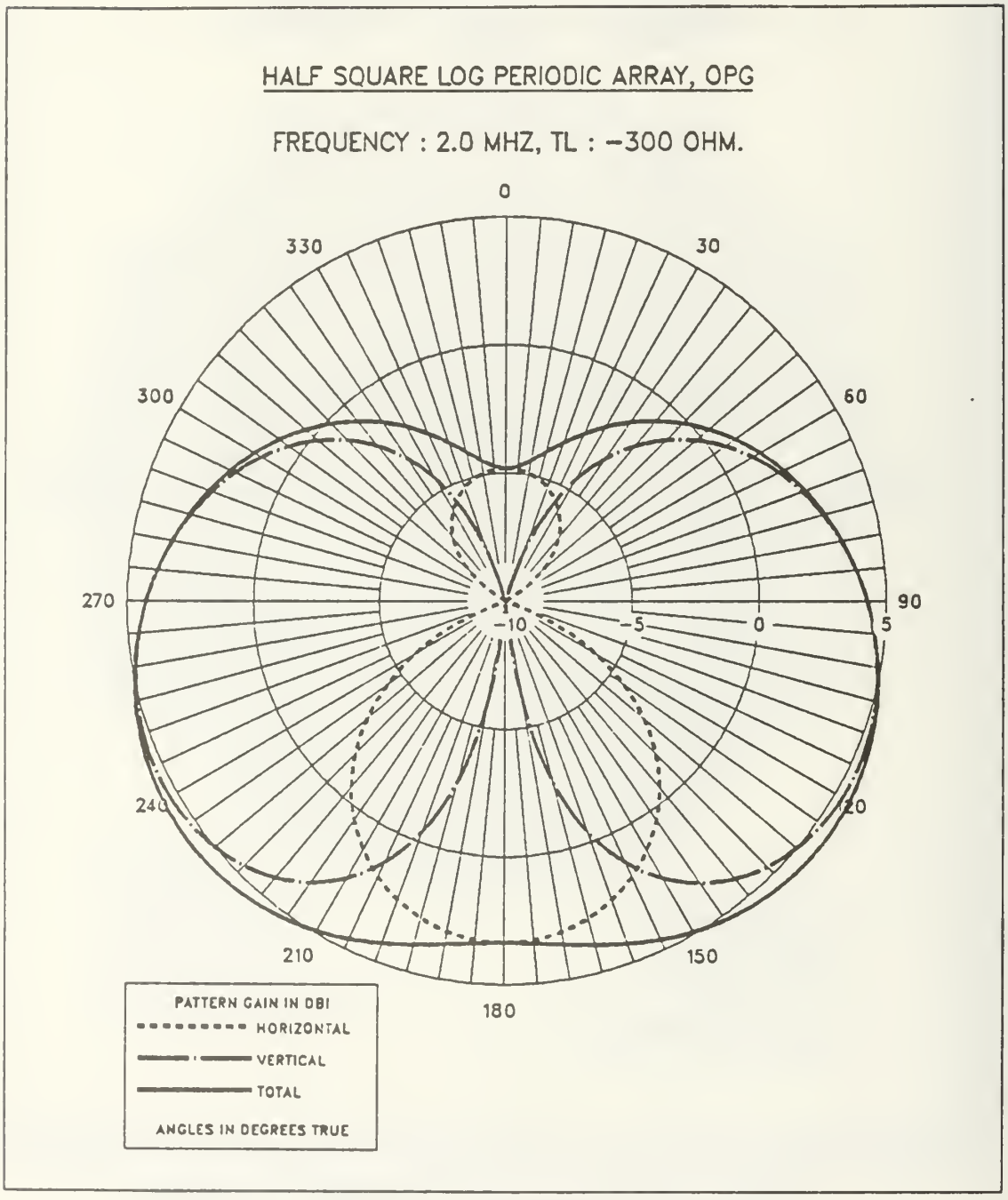

Figure D.1 Horizontal Pattern. Frequency: 2 MHz.

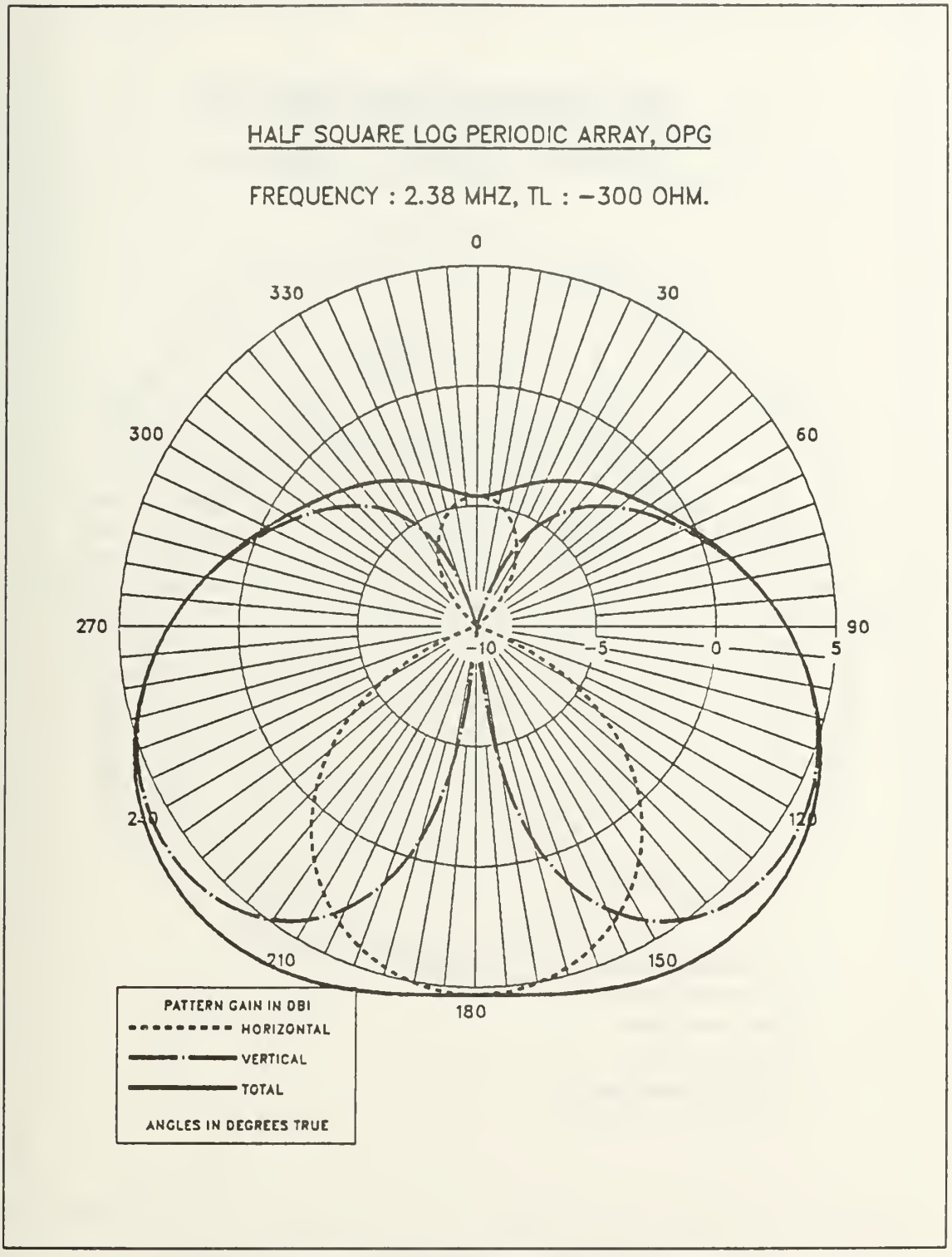

Figure D.2 Horizontal Pattern, Frequency: 2.38 MHz.

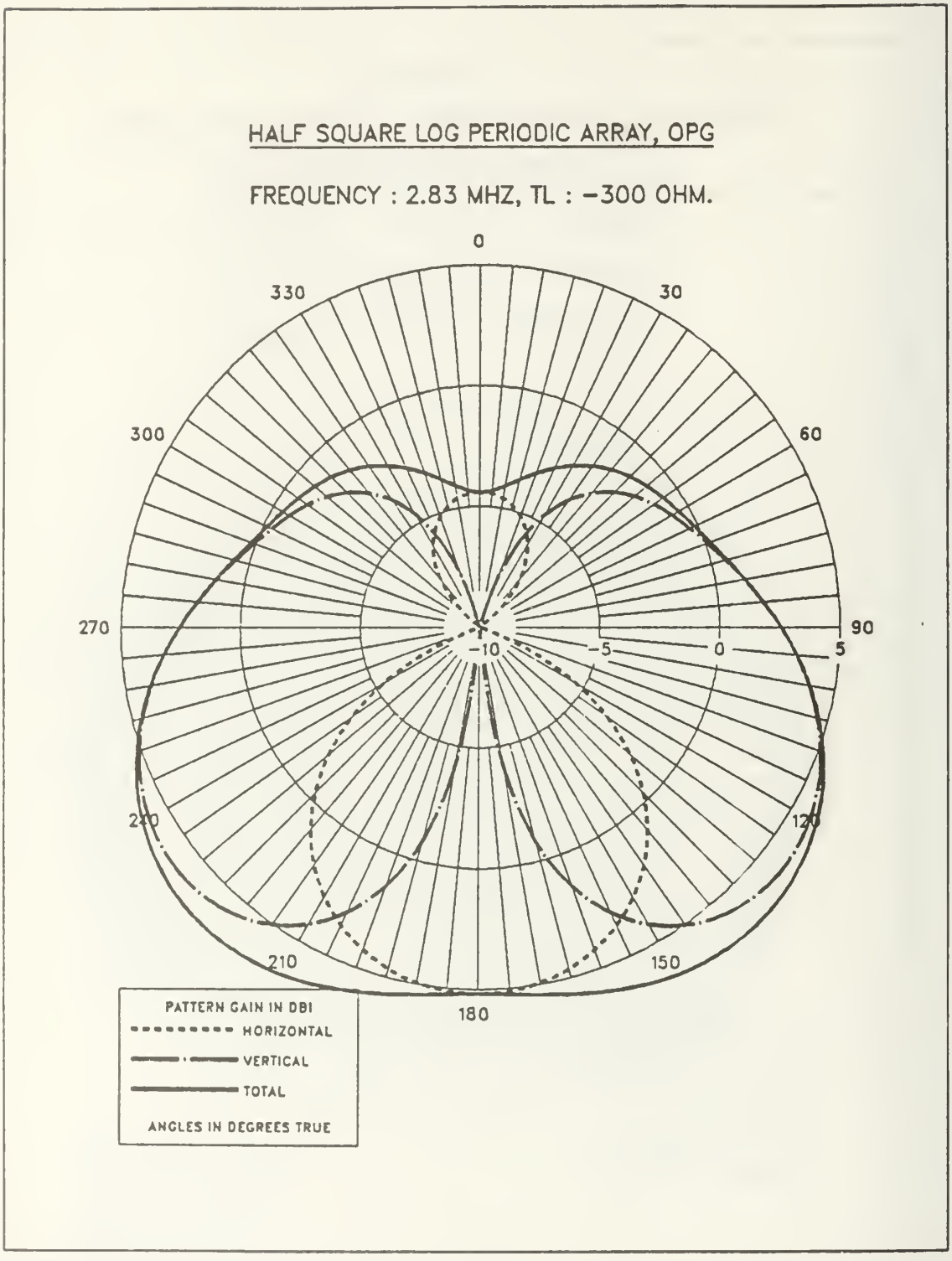

Figure D.3 Horizontal Pattern, Frequency: 2.83 MHz.

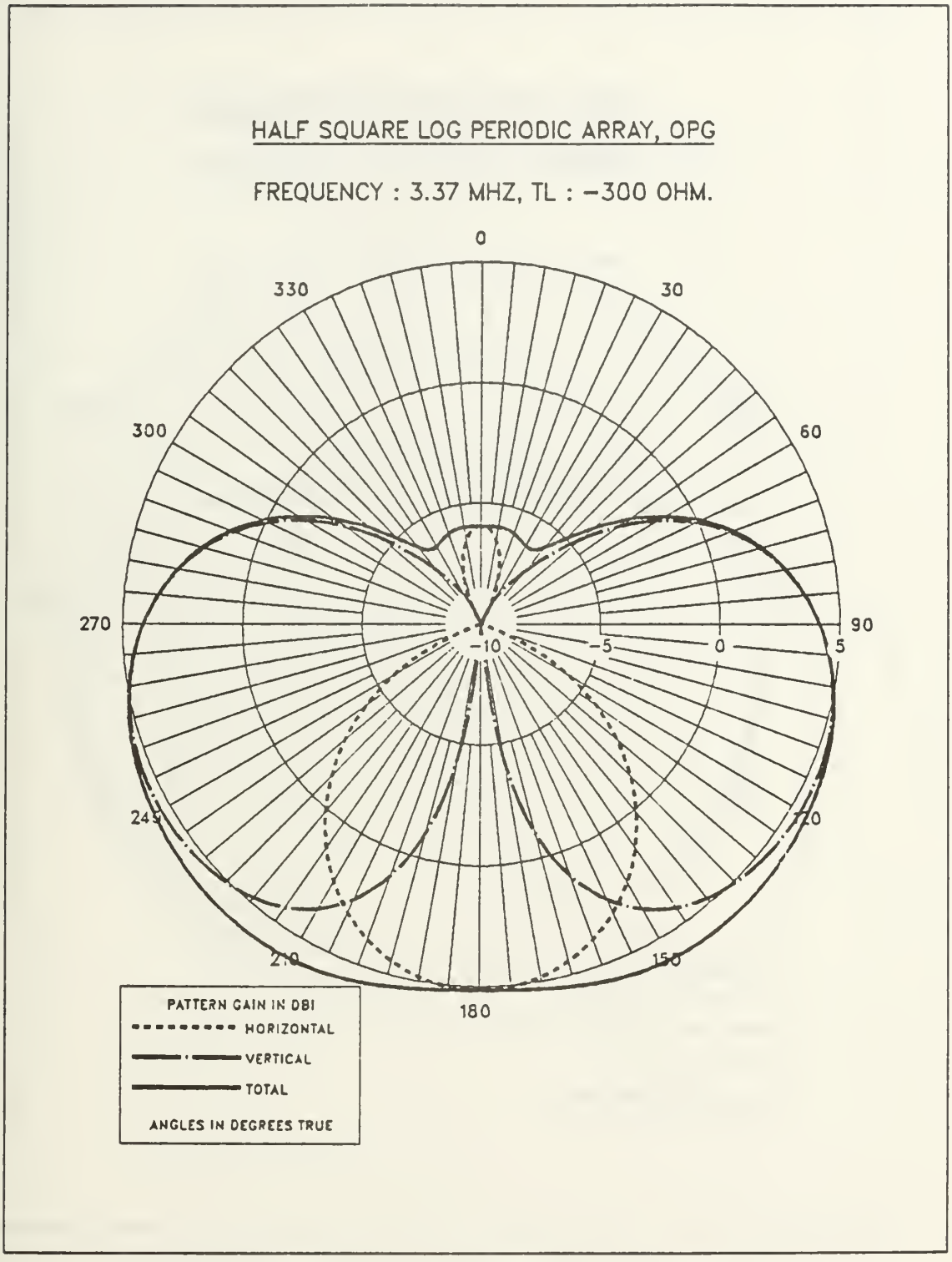

Figure D.4 Horizontal Pattern, Frequency: 3.37 MHz.

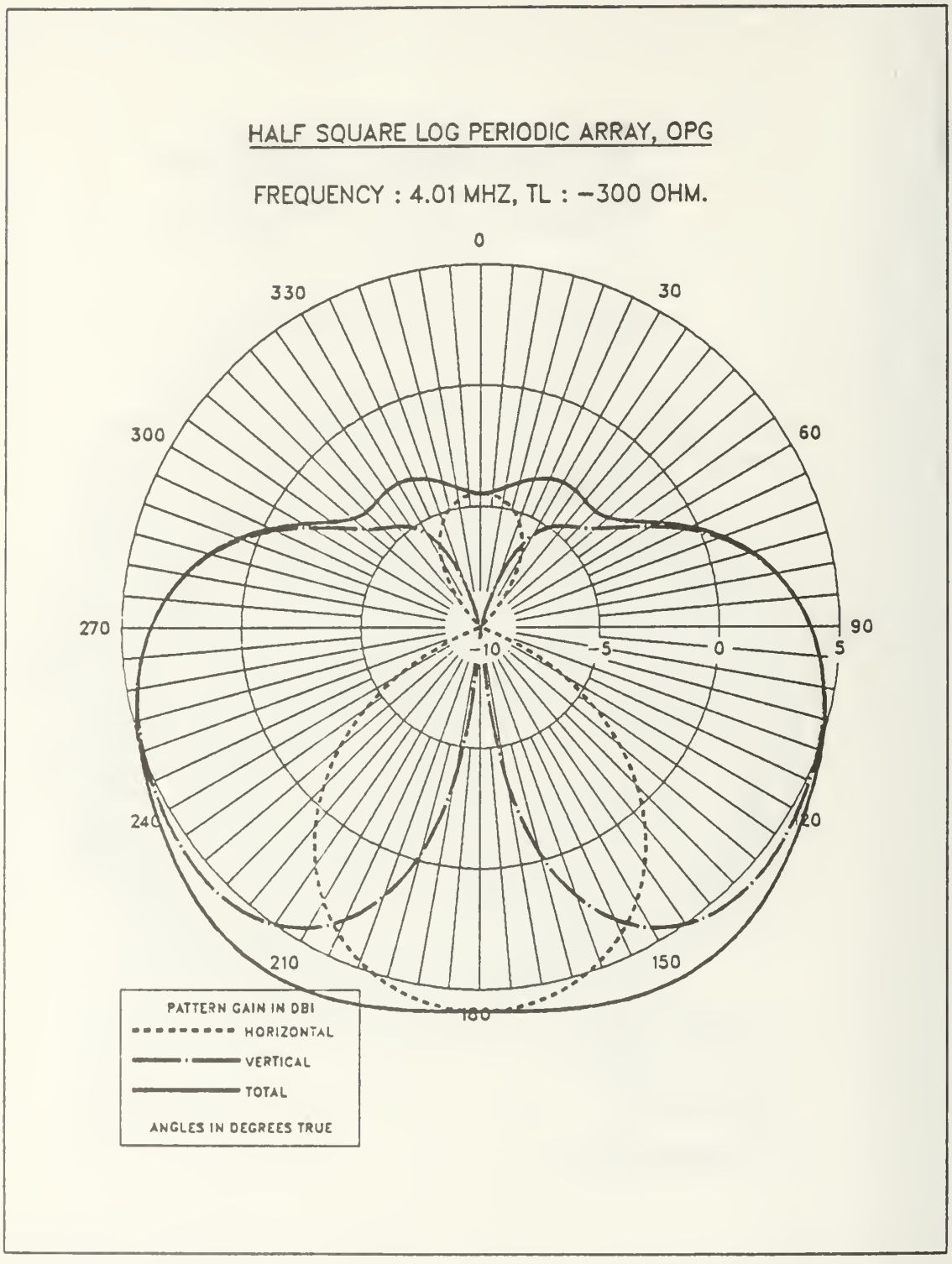

Figure D.5 Horizontal Pattern, Frequency: 4.07 MHz.

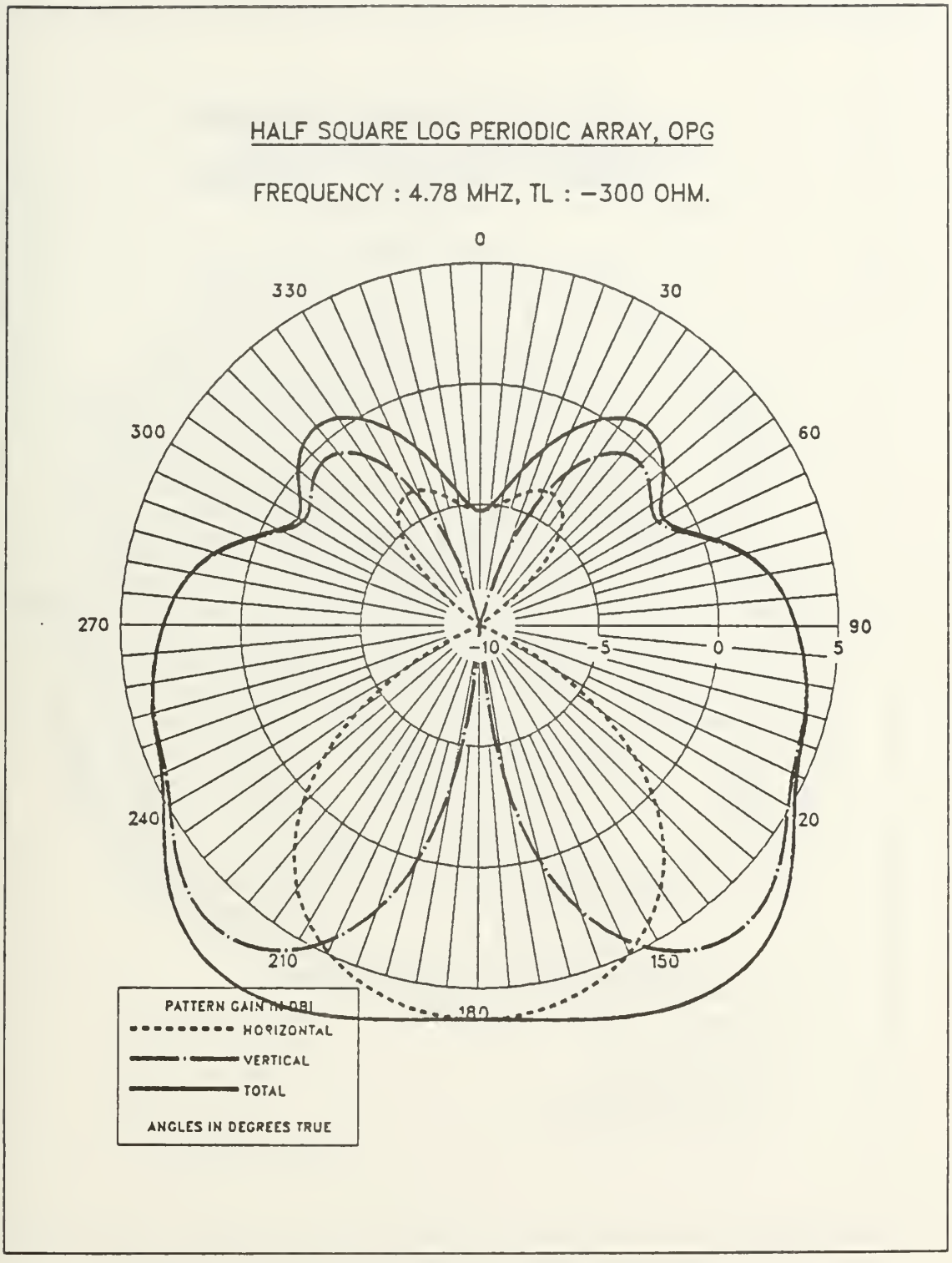

Figure D.6 Horizontal Pattern, Frequency: 4.78 MHz.

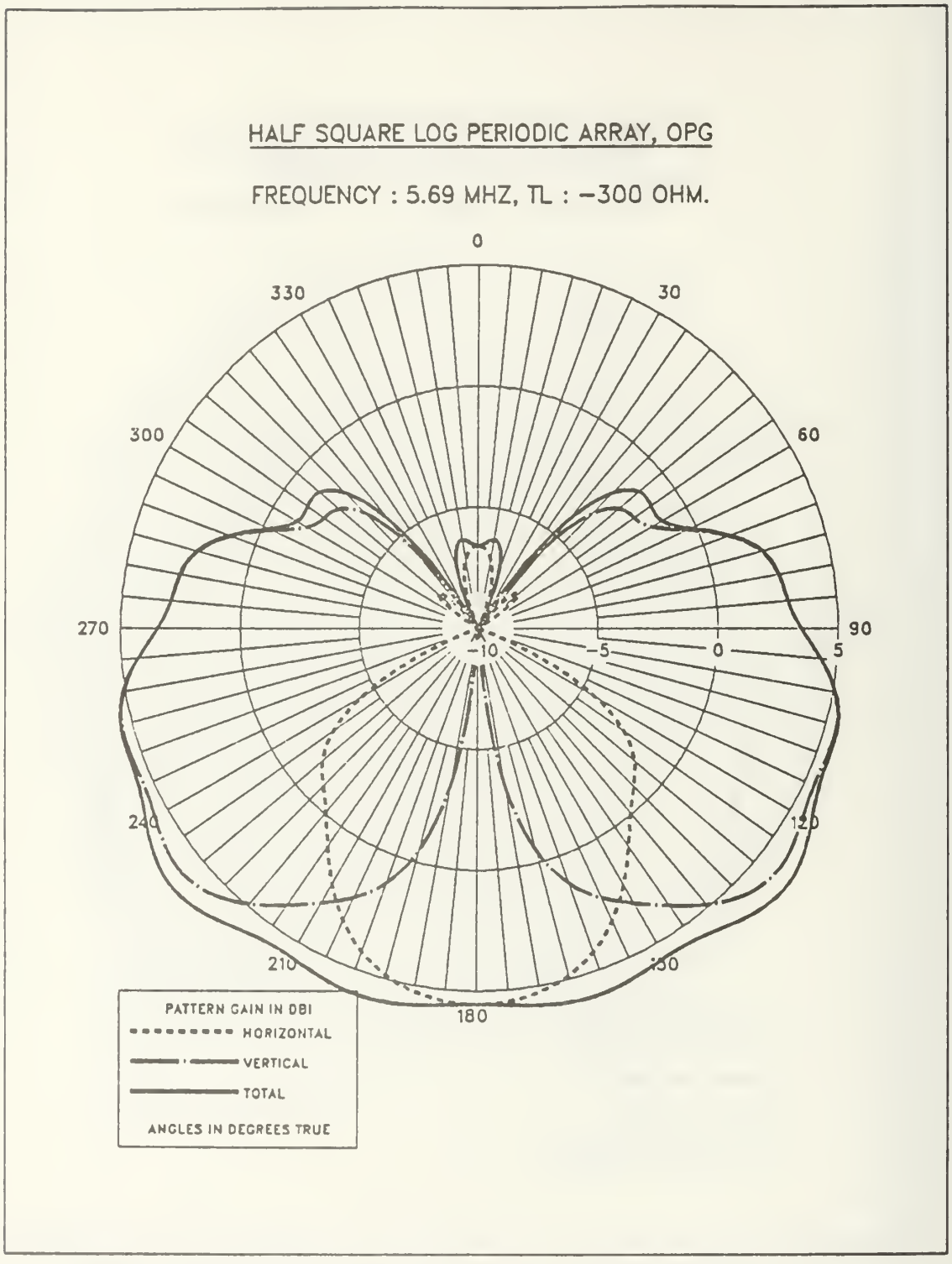

Figure D.7 Horizontal Pattern, Frequency: 5.69 MHz.

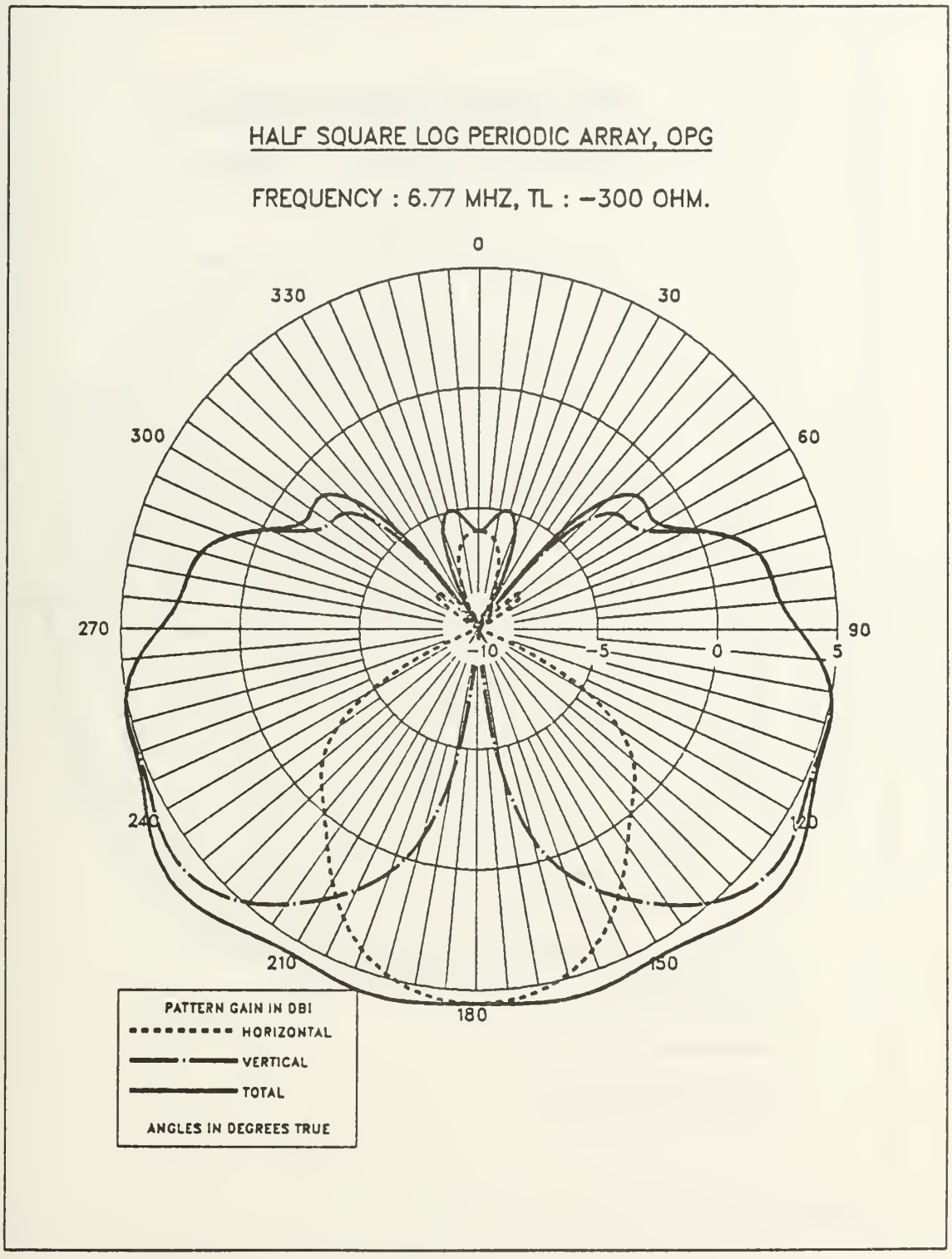

Figure D.8 Horizontal Pattern, Frequency: 6.77 MHz.

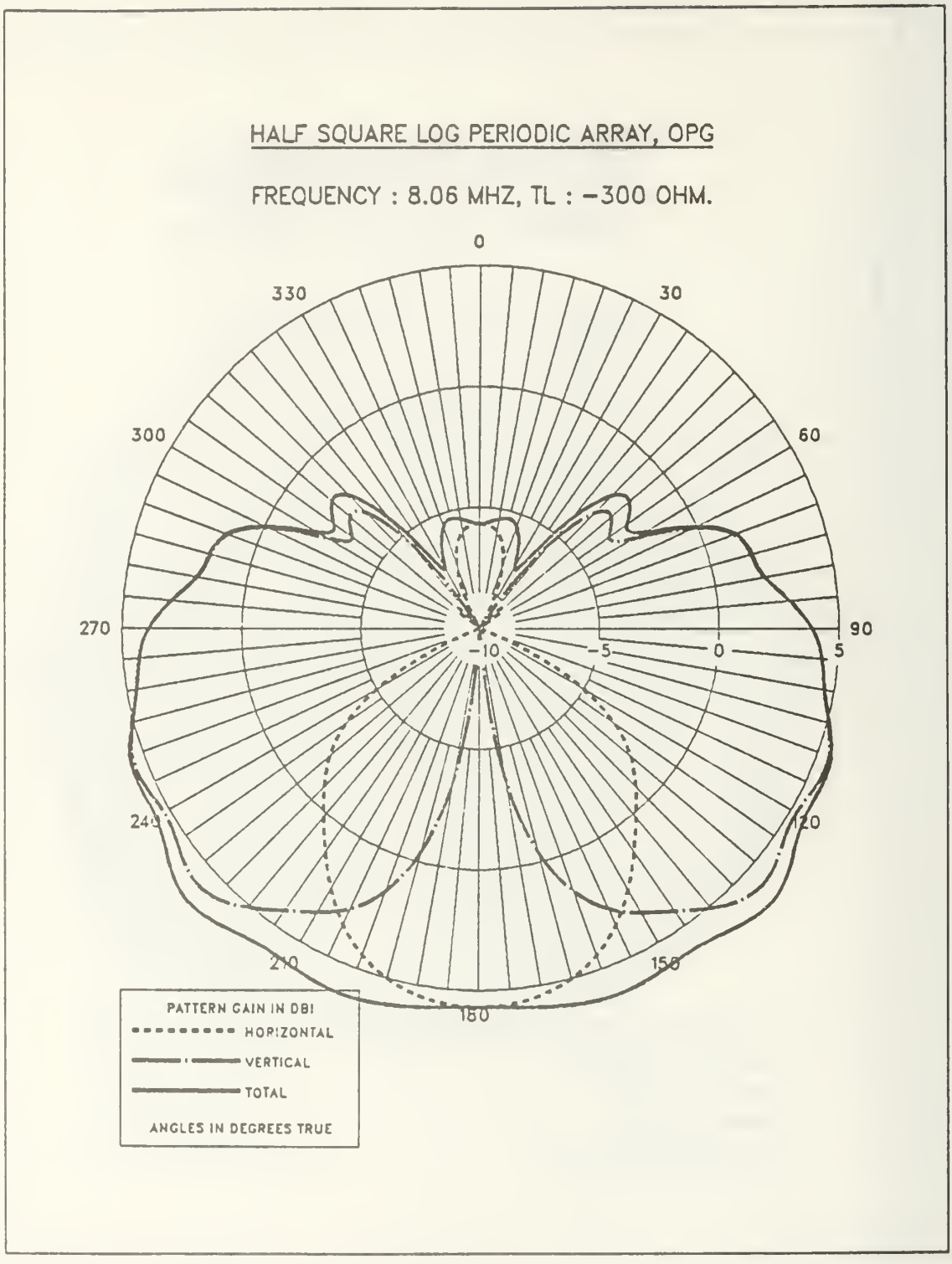

Figure D.9 Horizontal Pattern, Frequency: 8.06 MHz.

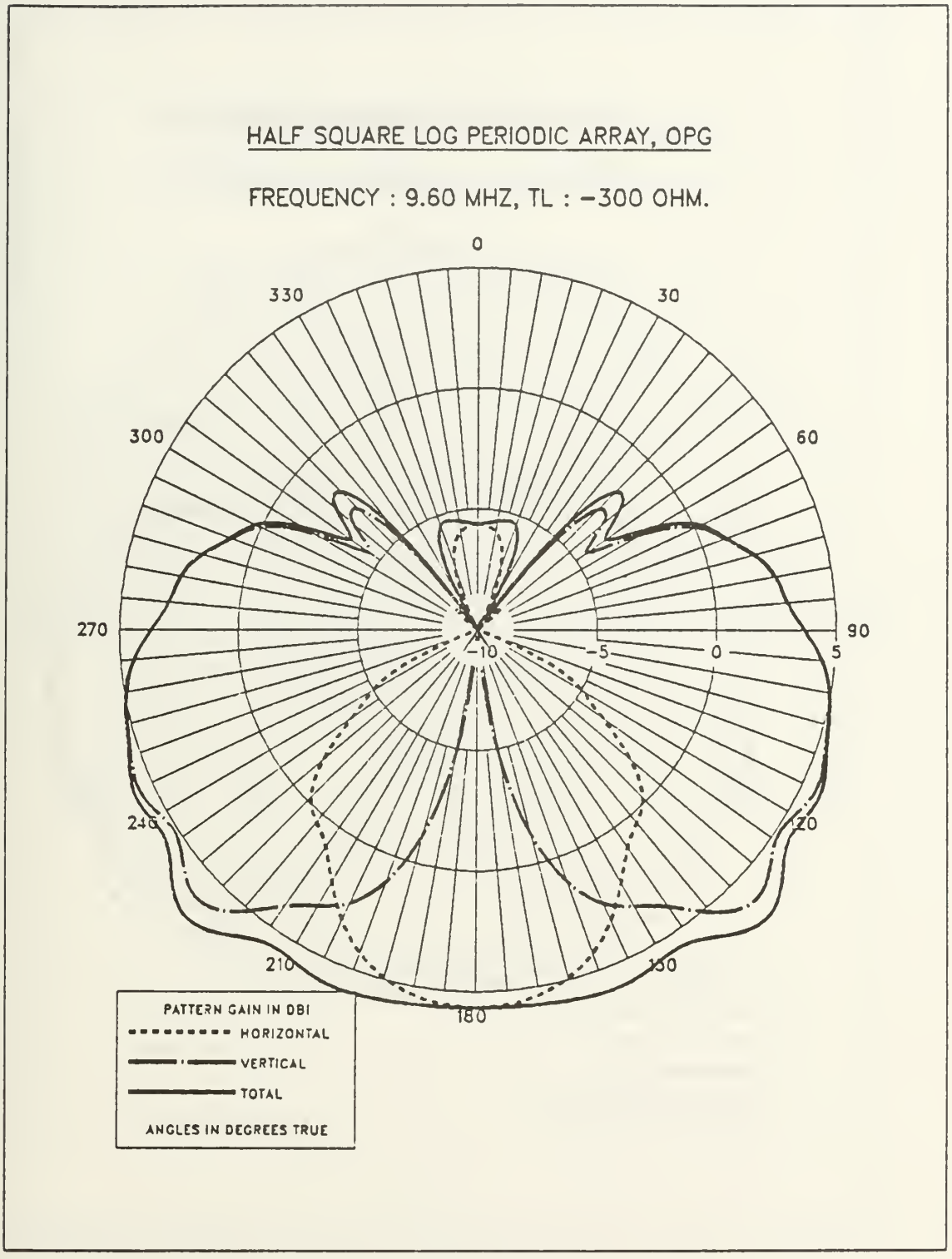

Figure D.10 Horizontal Pattern, Frequency: 9.60 MHz.

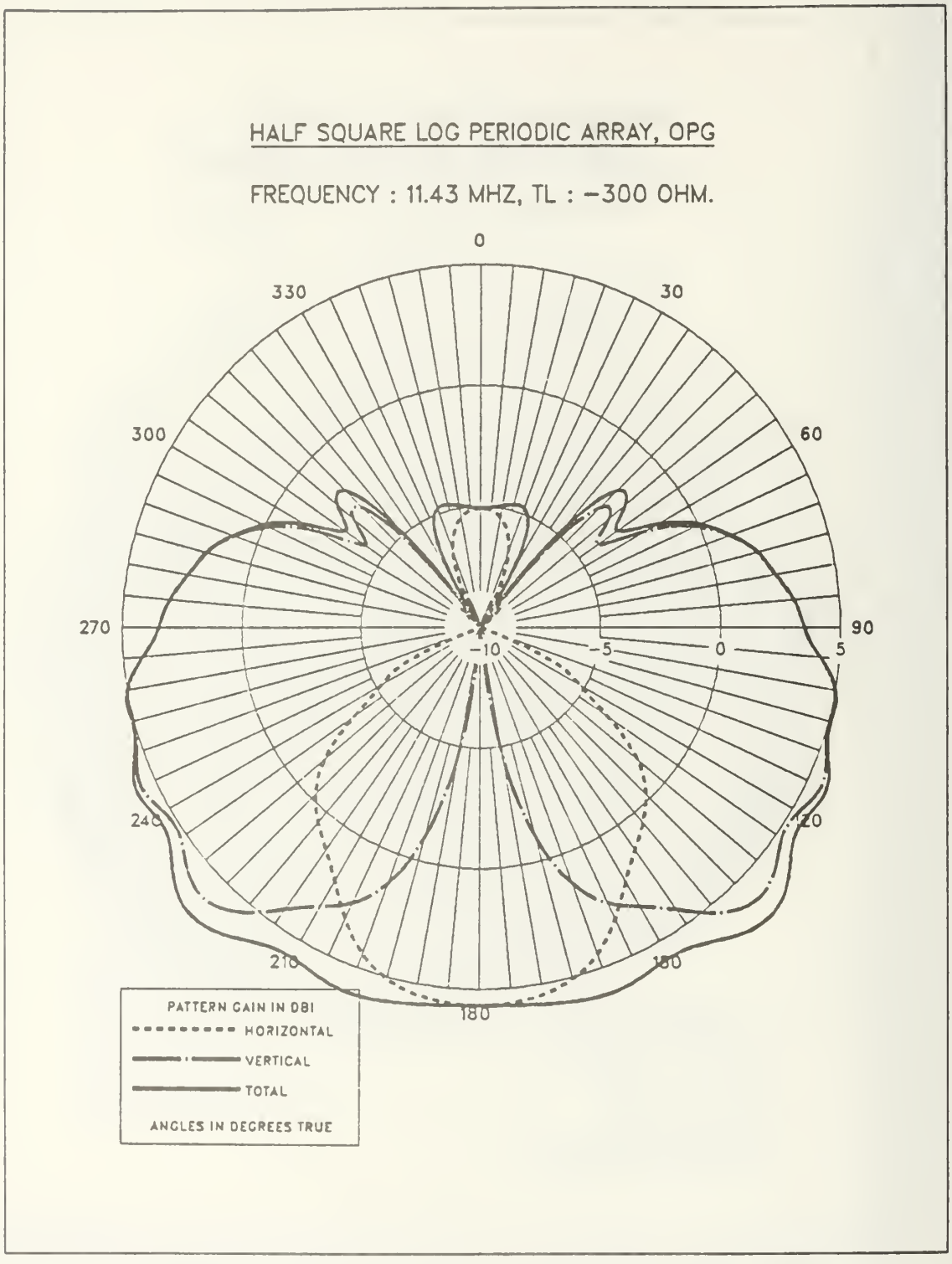

Figure D.11 Horizontal Pattern, Frequency: 11.43 MHz.

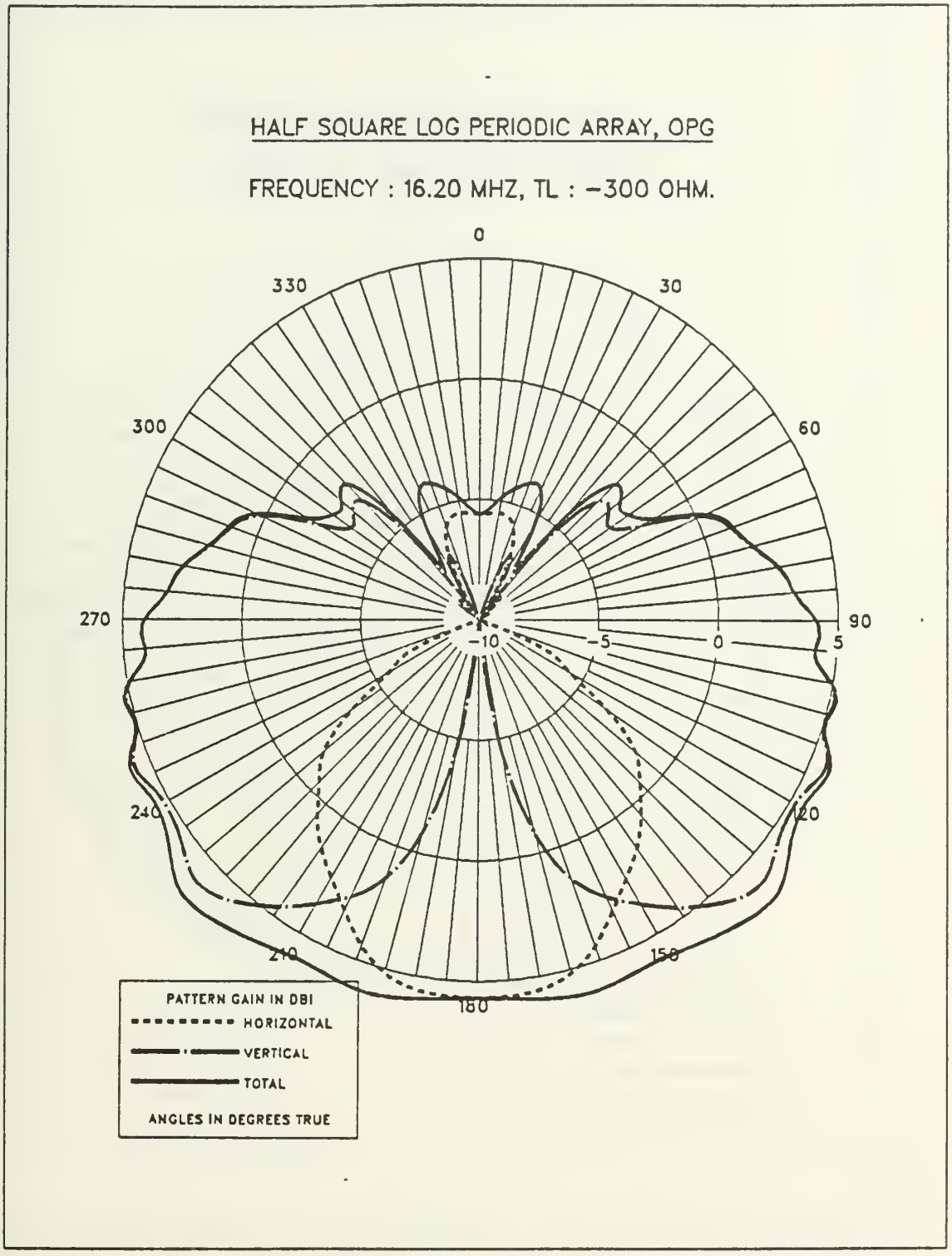

Figure D.12 Horizontal Pattern, Frequency: 16.20 MHz.

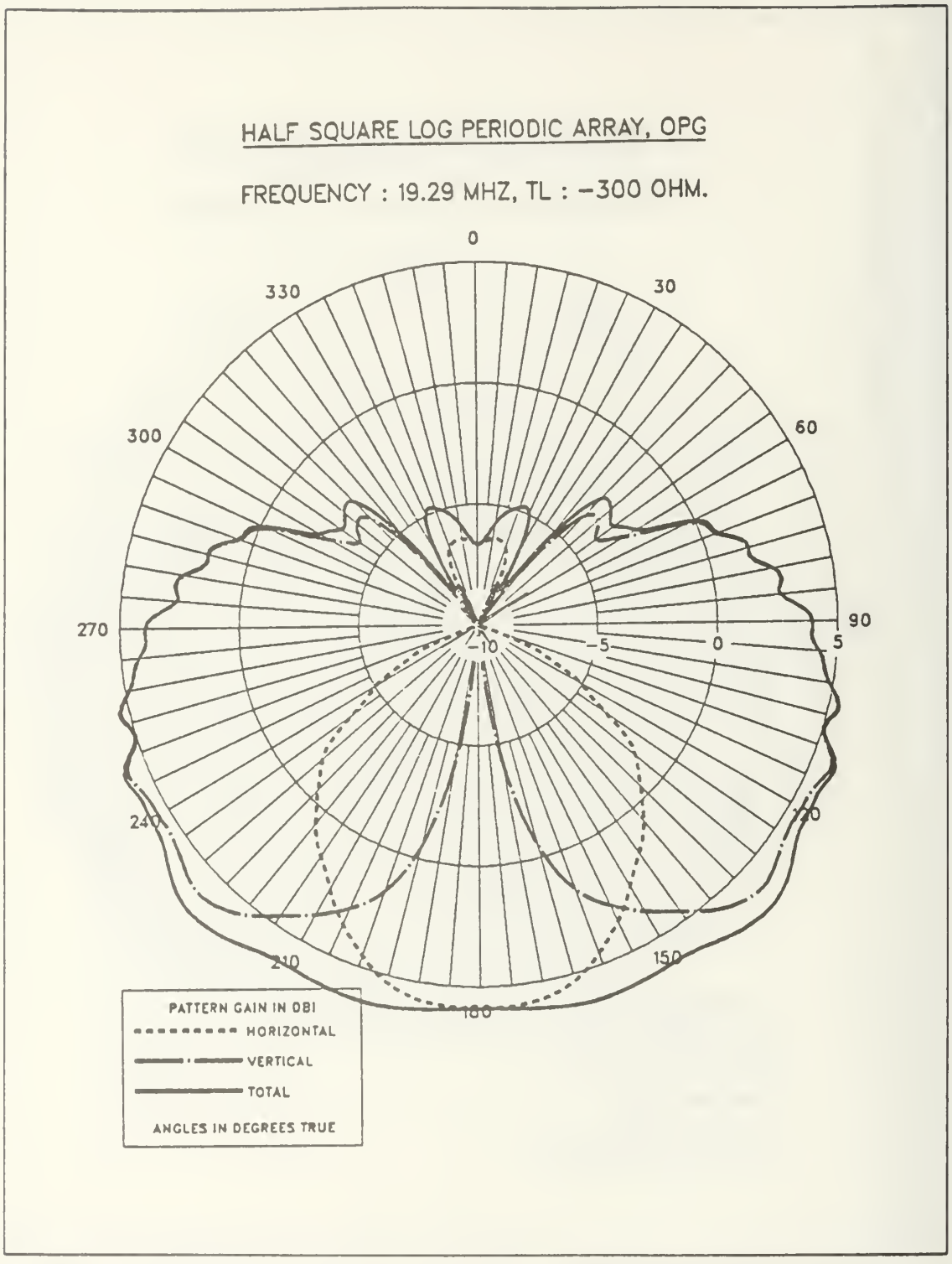

Figure D.13 Horizontal Pattern, Frequency: 19.29 MHz.

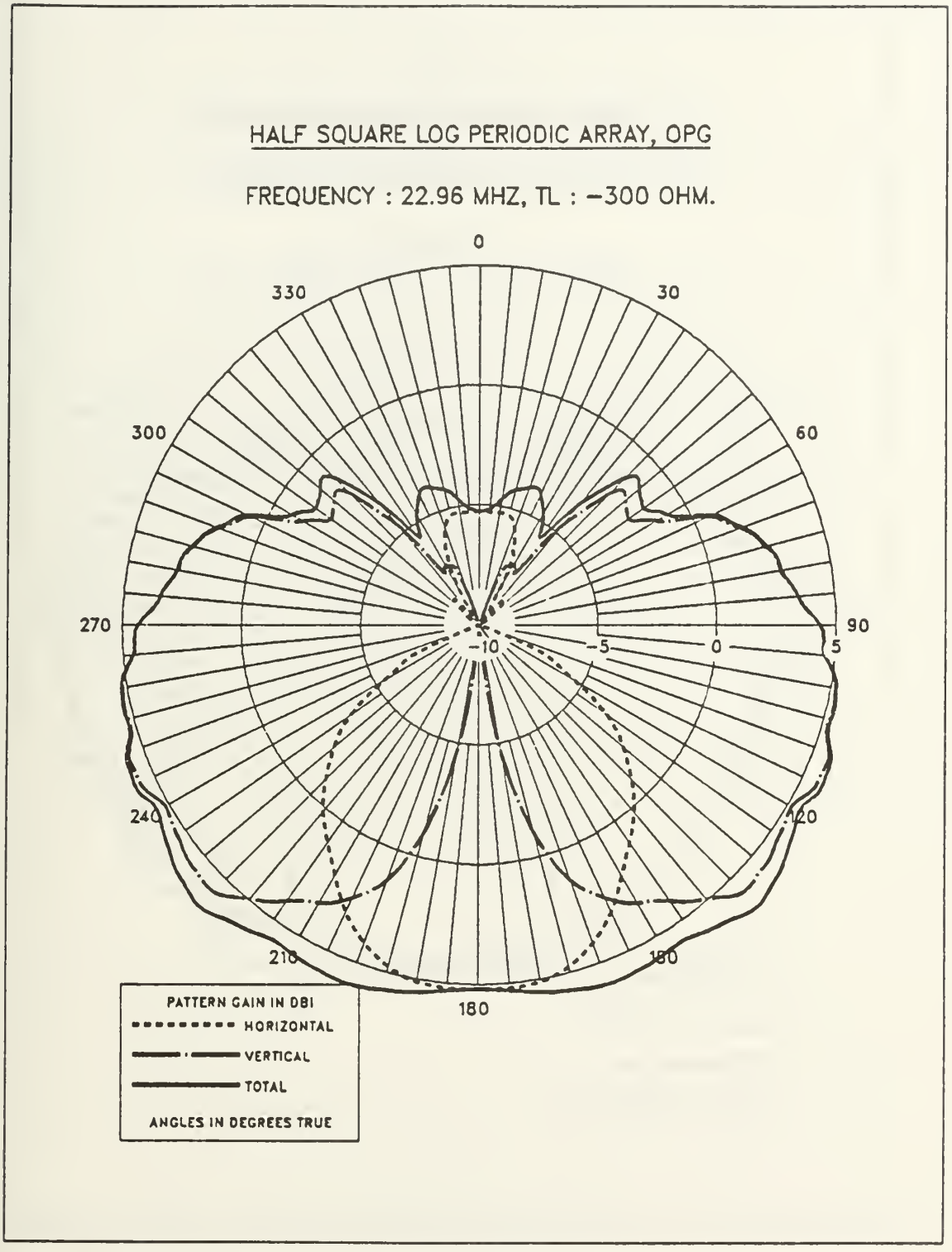

Figure D.14 Horizontal Pattern, Frequency: 22.96 MHz.

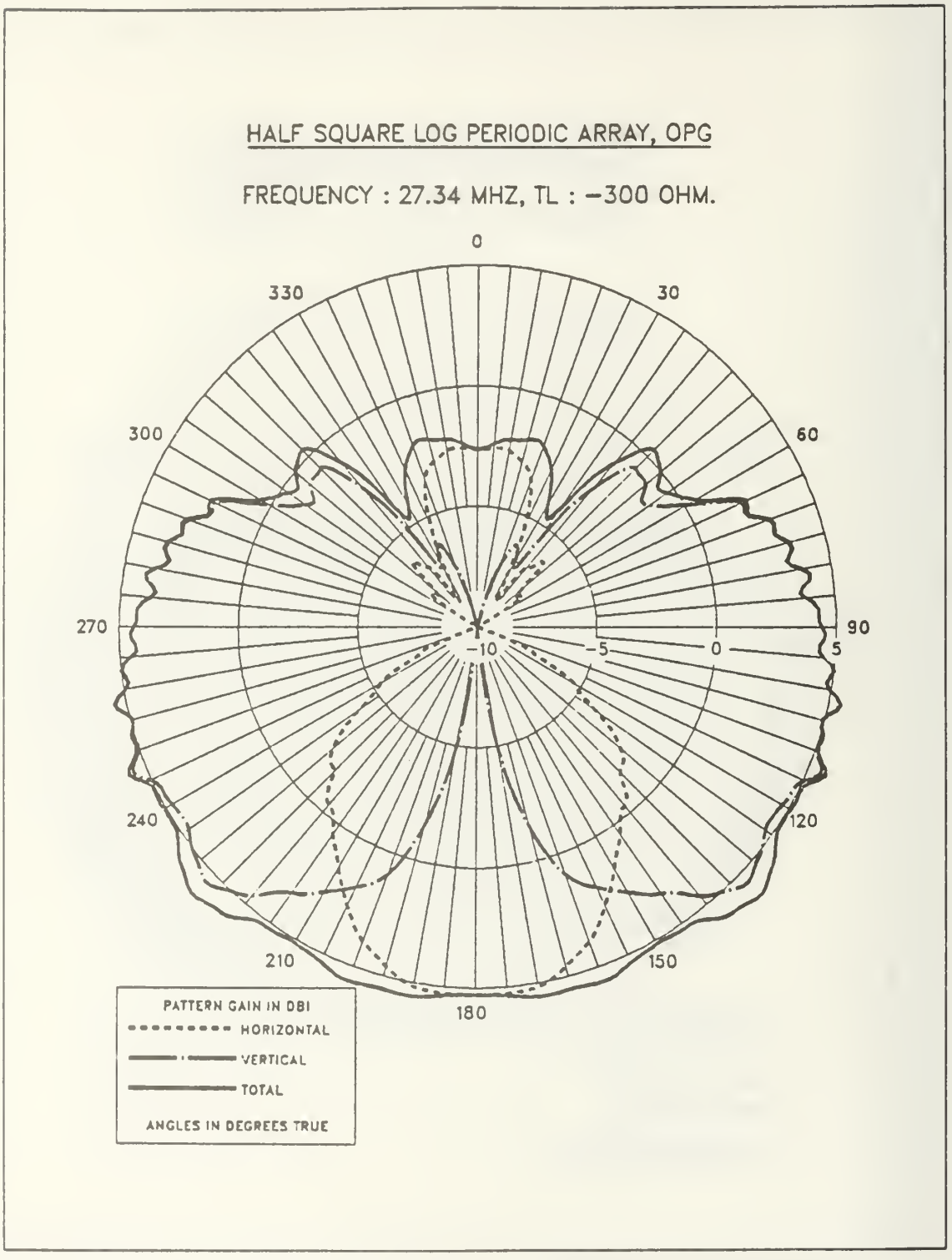

Figure D.15 Horizontal Pattern, Frequency: 27.34 MHz.

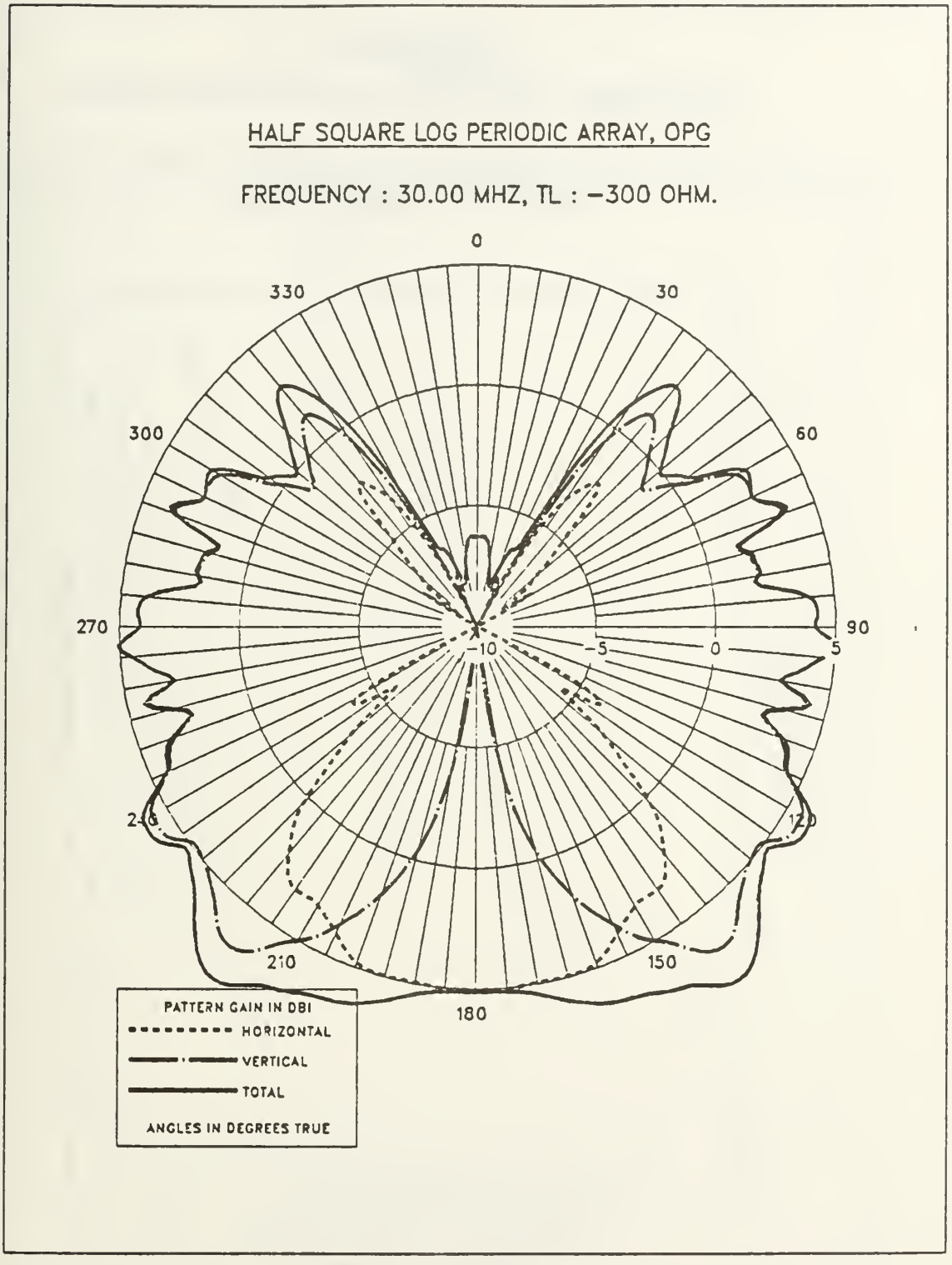

Figure D.16 Horizontal Pattern, Frequency: 30.0 MHz.

APPENDIX E
AMPLITUDE AND PHASE PLOTS IN FREE SPACE

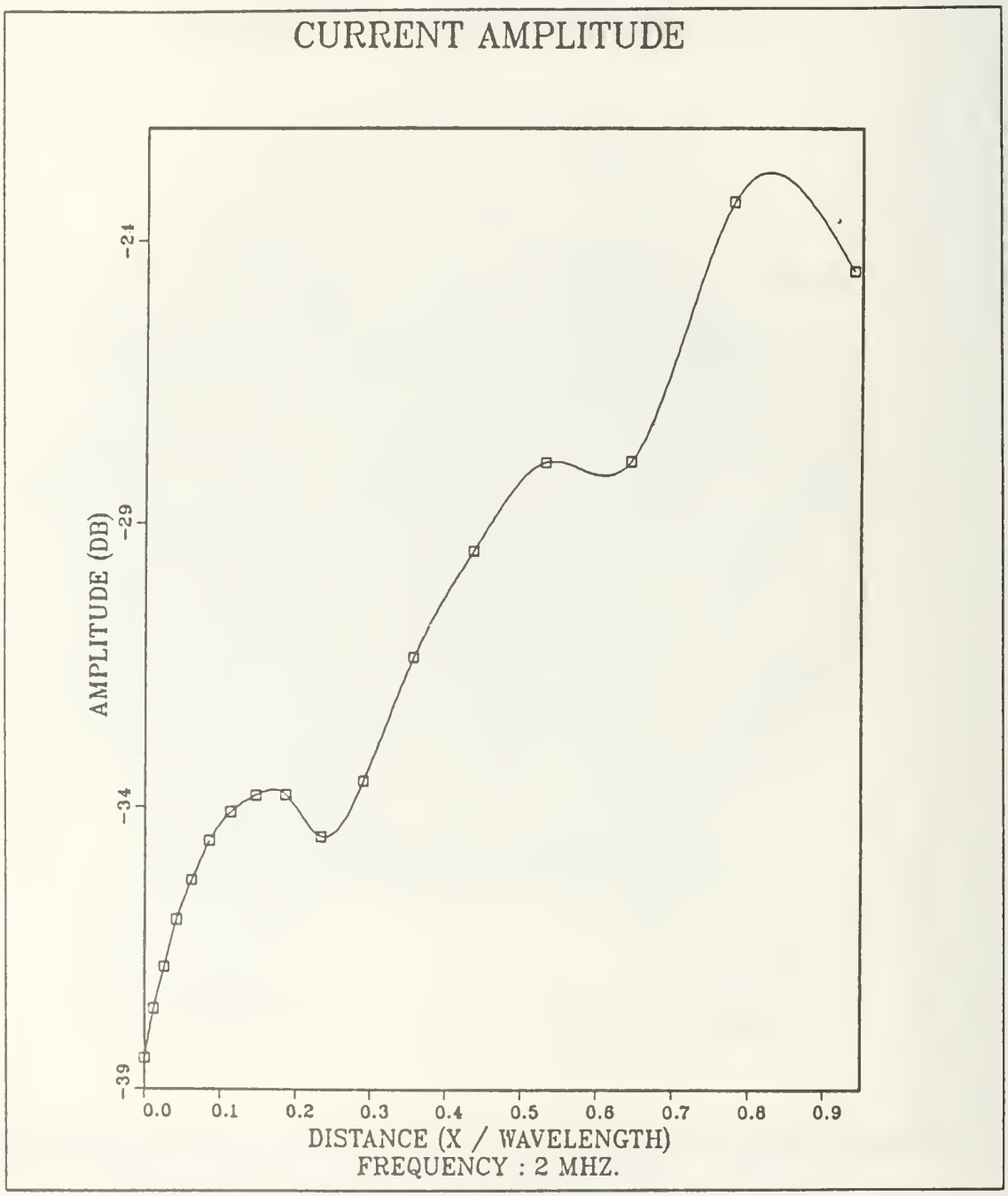

Figure E.1 Current Amplitude, Frequency : 2 MHz.

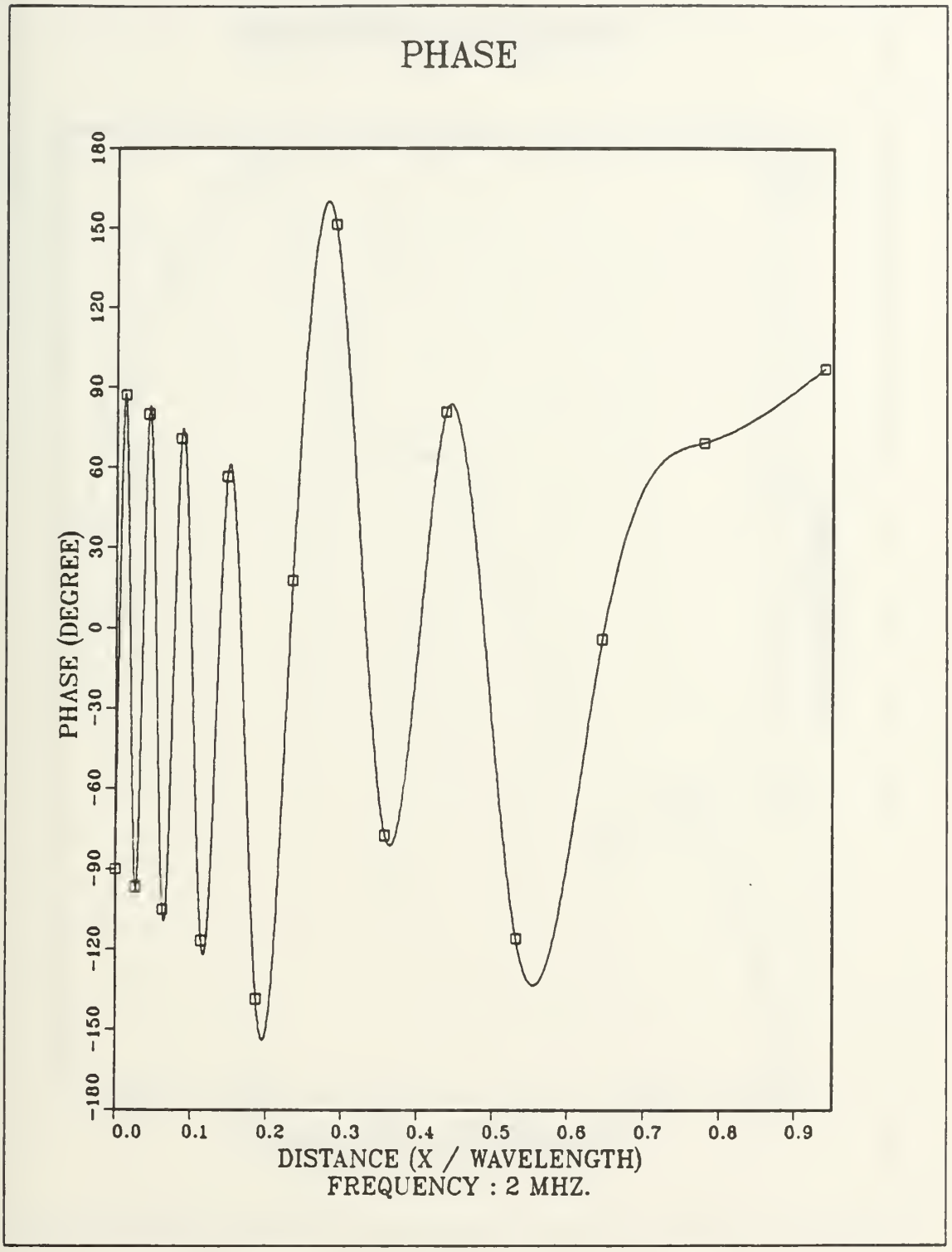

Figure E.2 Current Phase, Frequency : 2 MHz.

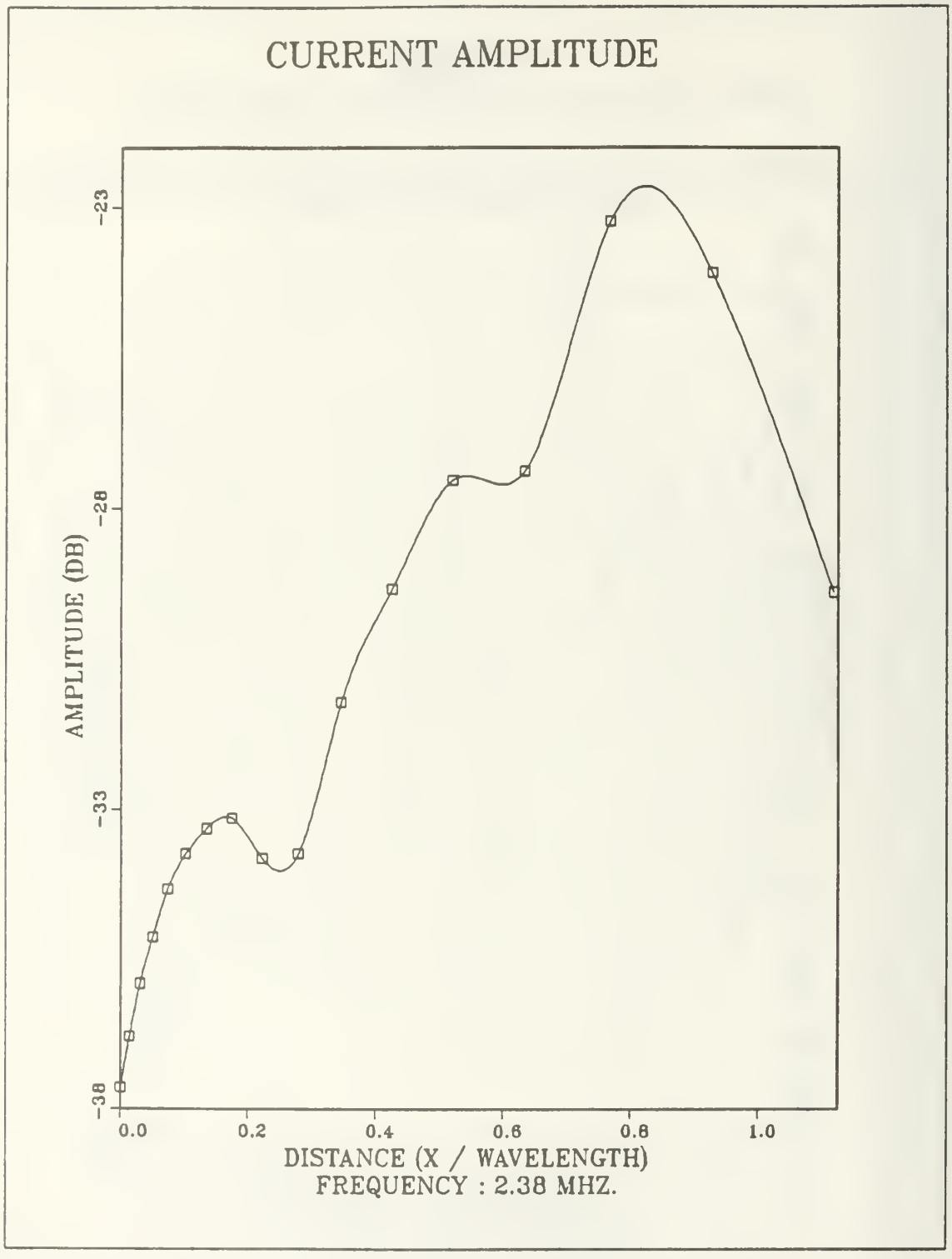

Figure E.3 Current Amplitude, Frequency : 2.38 MHz.

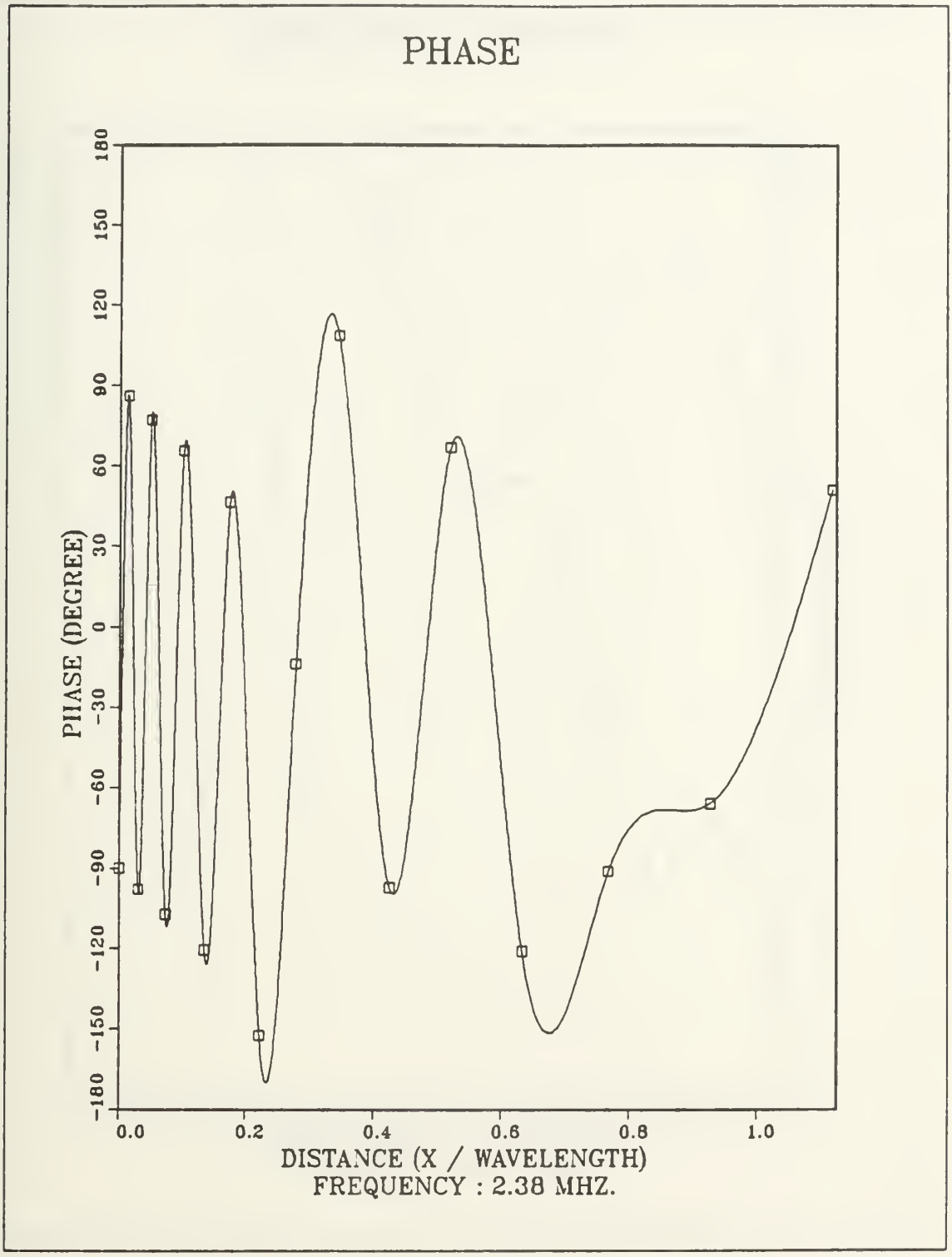

Figure E.4 Current Phase, Frequency : 2.38 MHz.

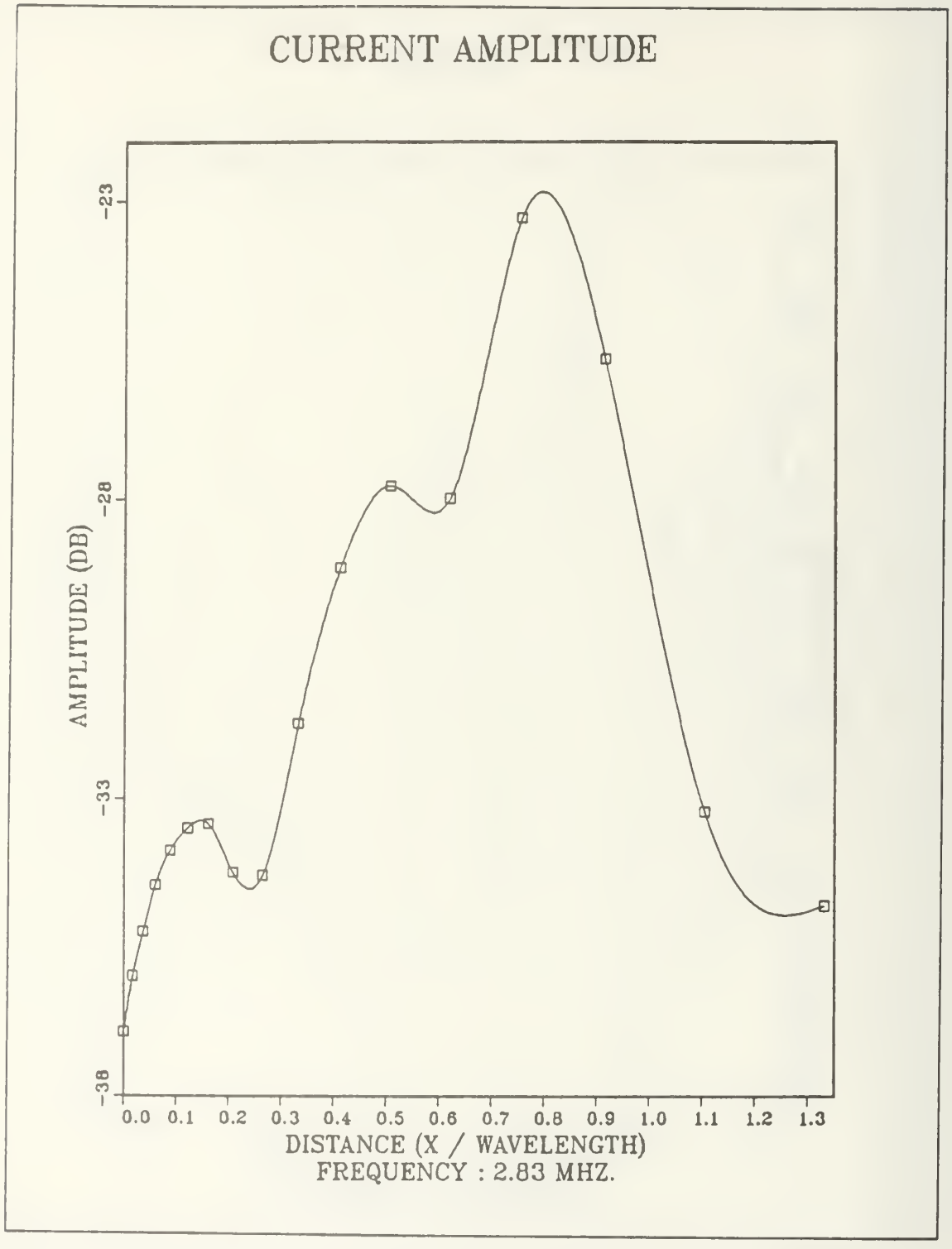

Figure E.5 Current Amplitude, Frequency : 2.83 MHz.

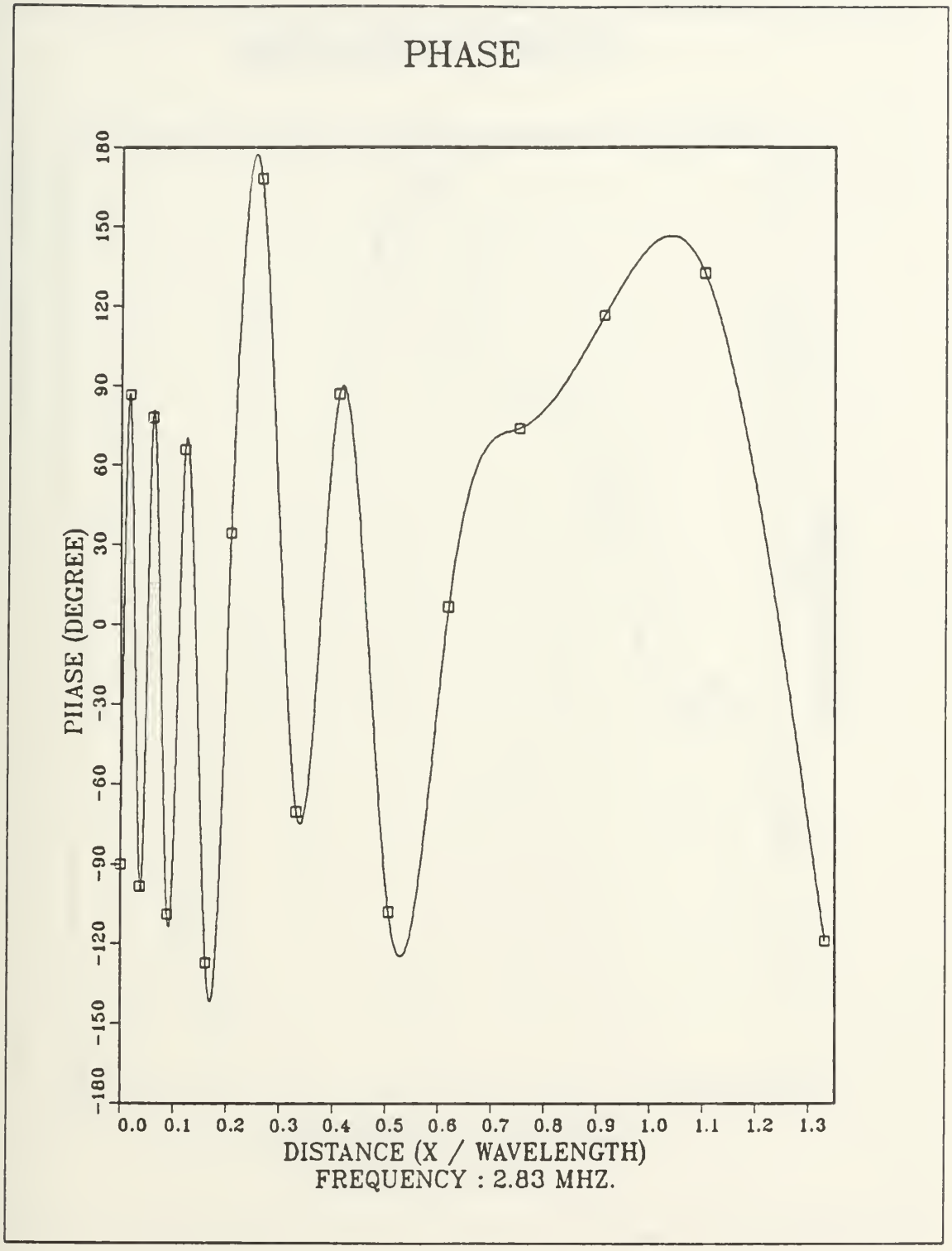

Figure E.6 Current Phase, Frequency : 2.83 MHz.

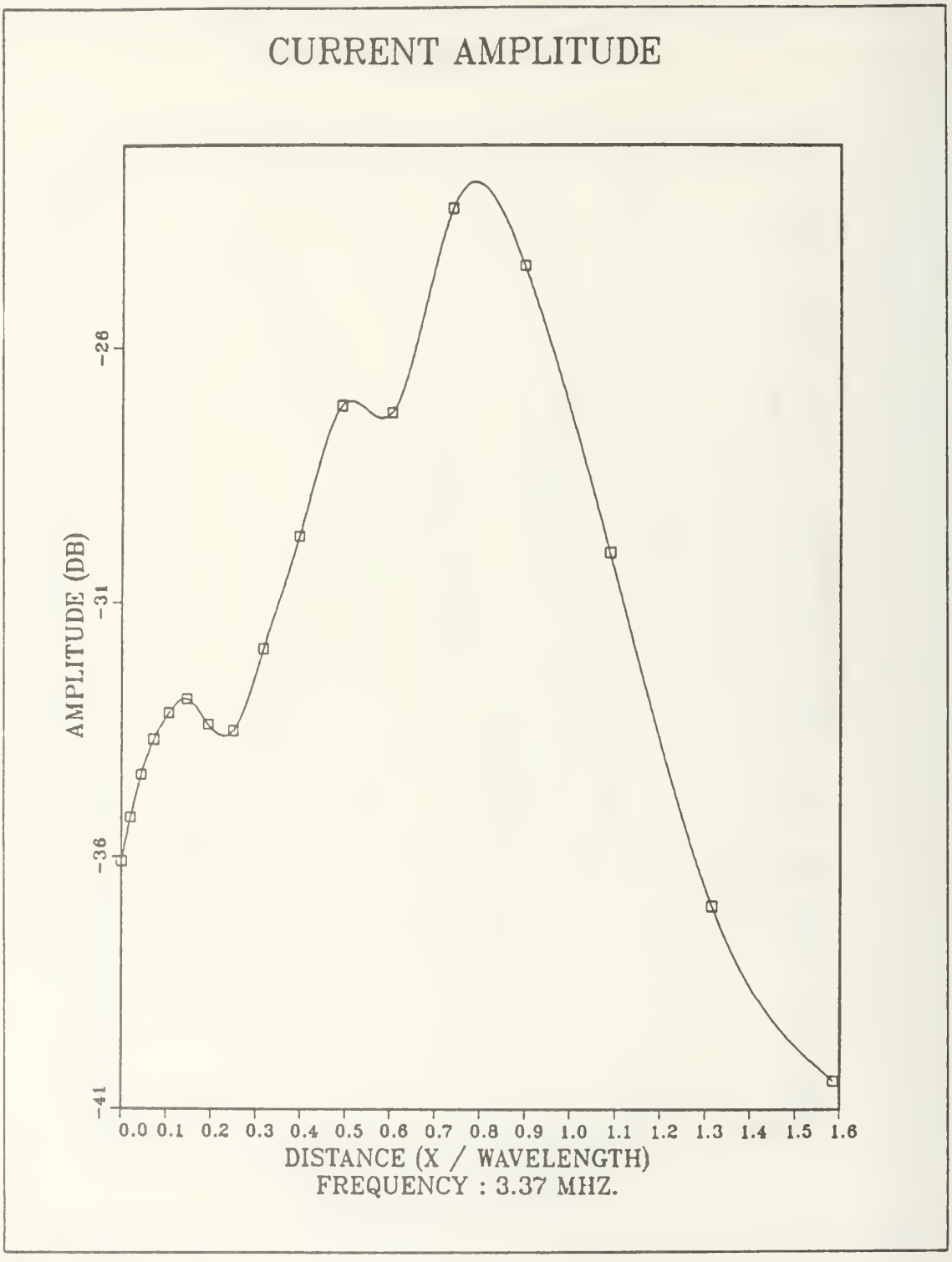

Figure E.7 Current Amplitude, Frequency : 3.37 MHz.

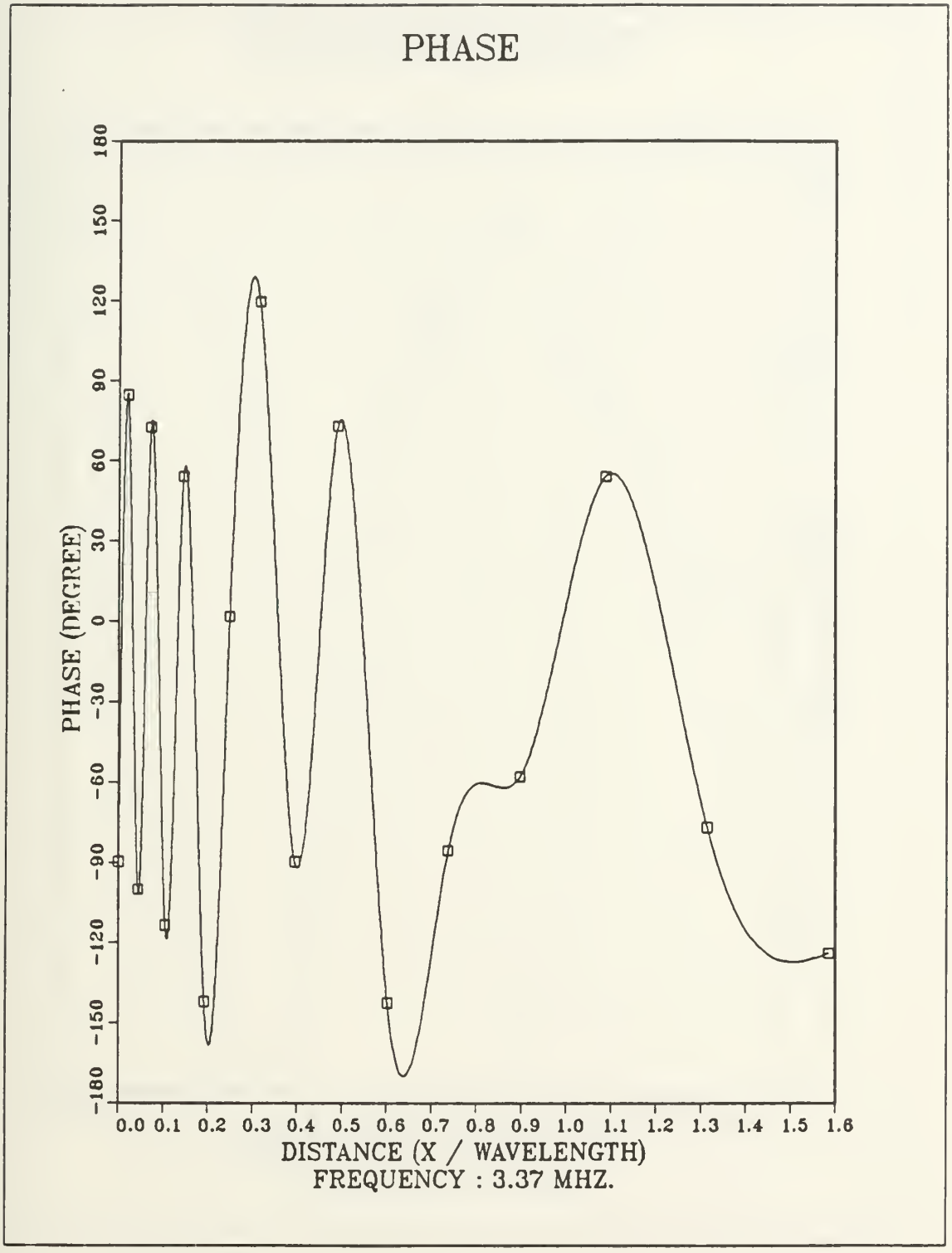

Figure E.8 Current Phase, Frequency : 3.37 MHz.

Figure E.9 Current Amplitude, Frequency : 4.01 MHz.

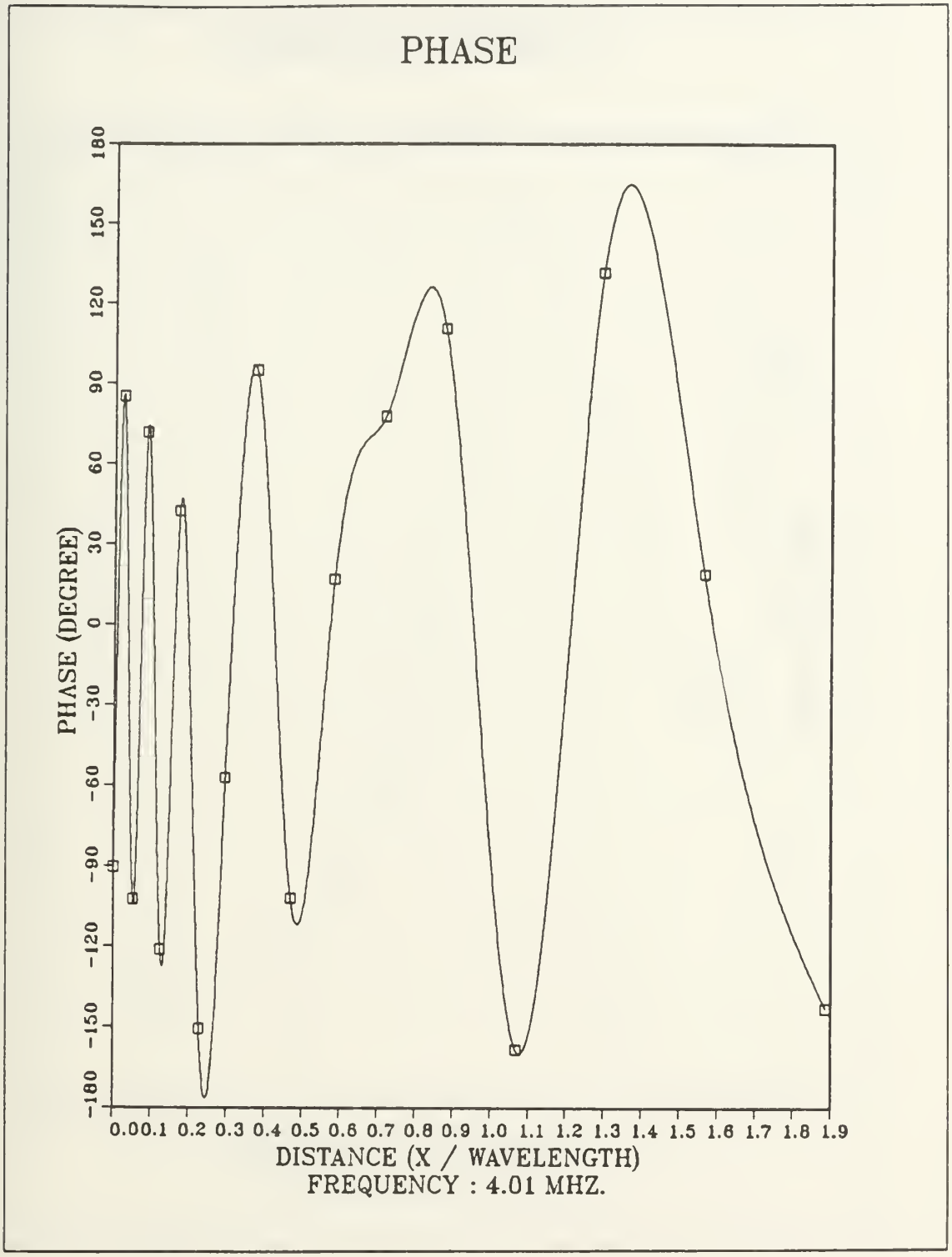

Figure E.10 Current Phase, Frequency : 4.01.

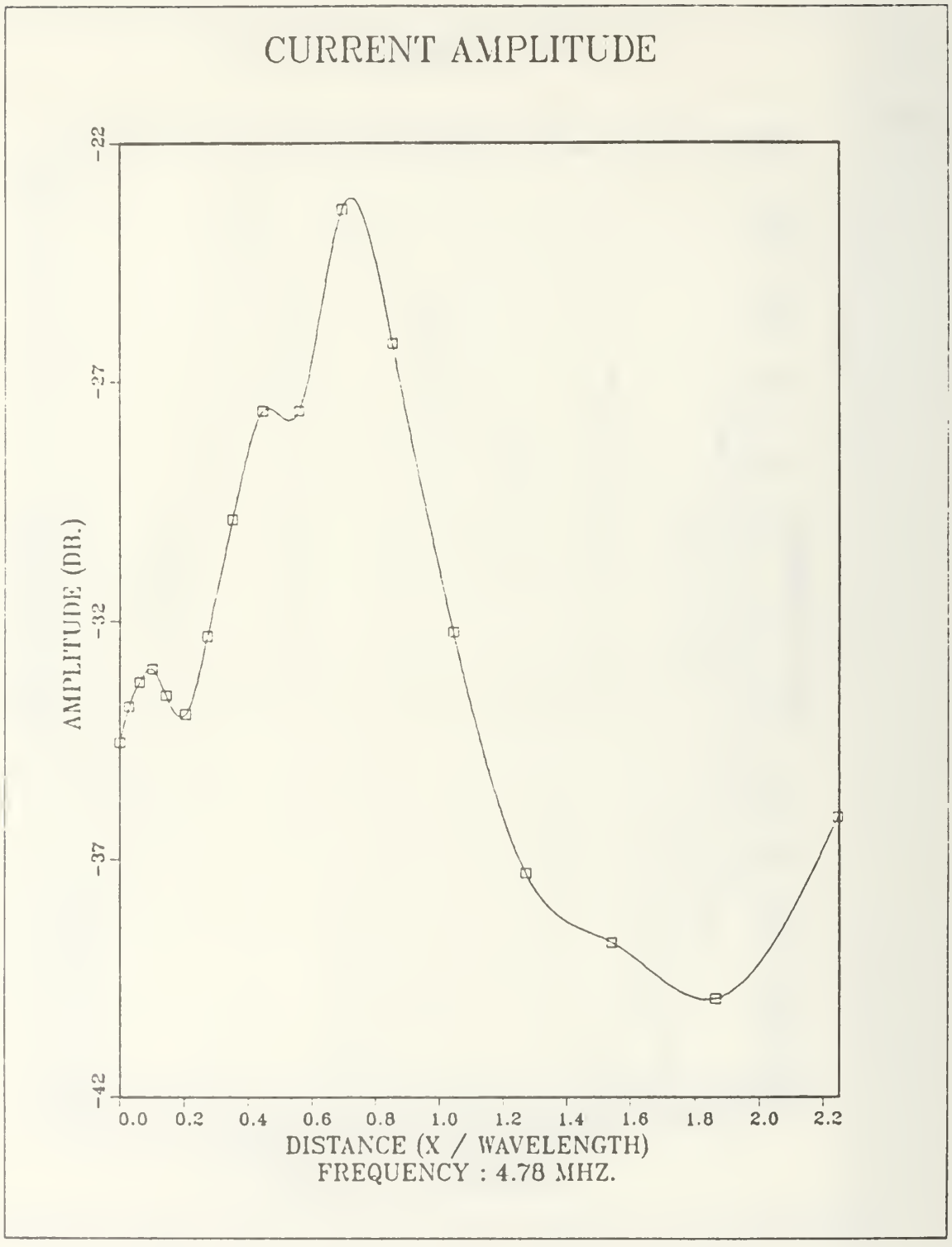

Figure E.11 Current Amplitude, Frequency : 4.78 MHz.

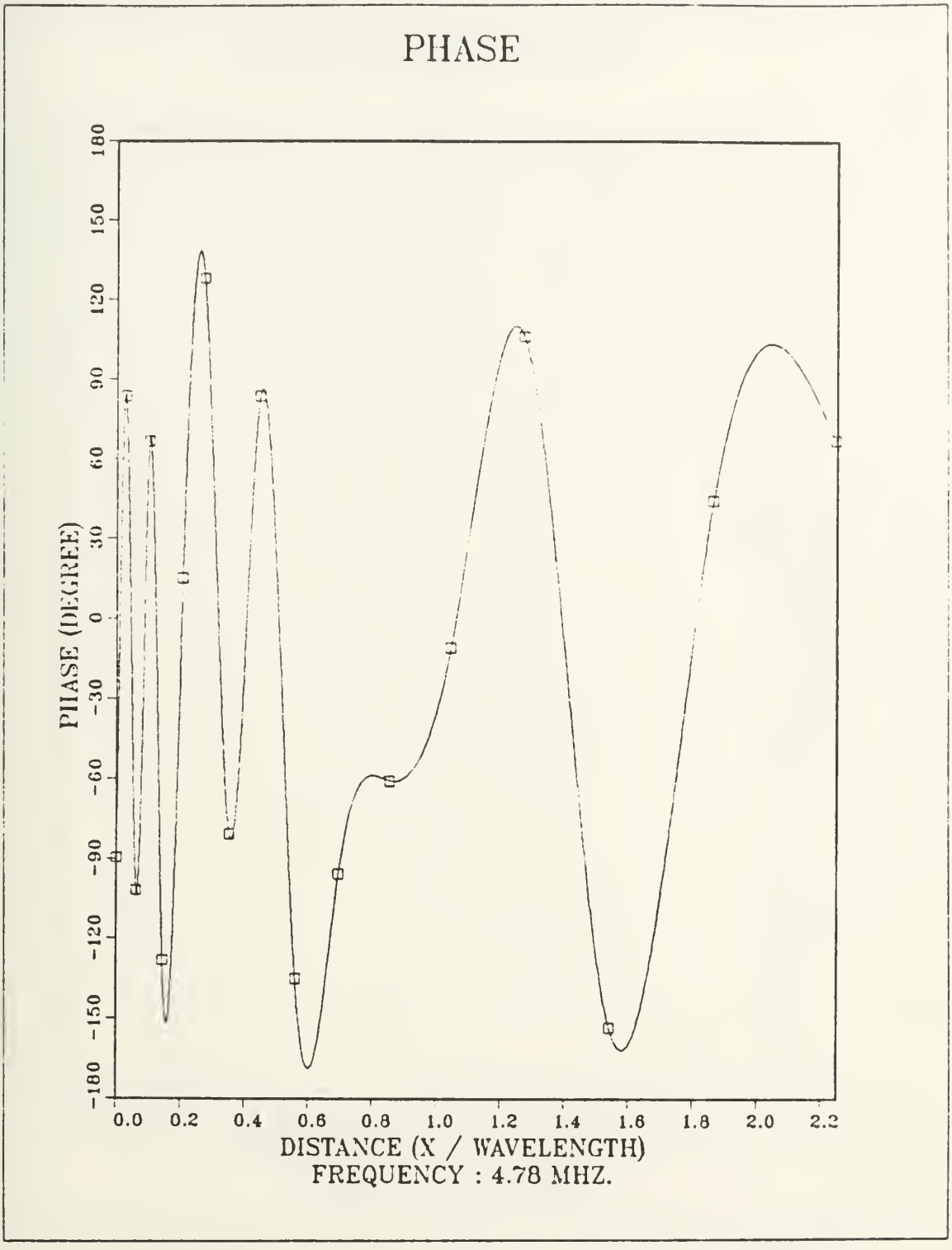

Figure E.12 Current Phase, Frequency : 4.78 MHz.

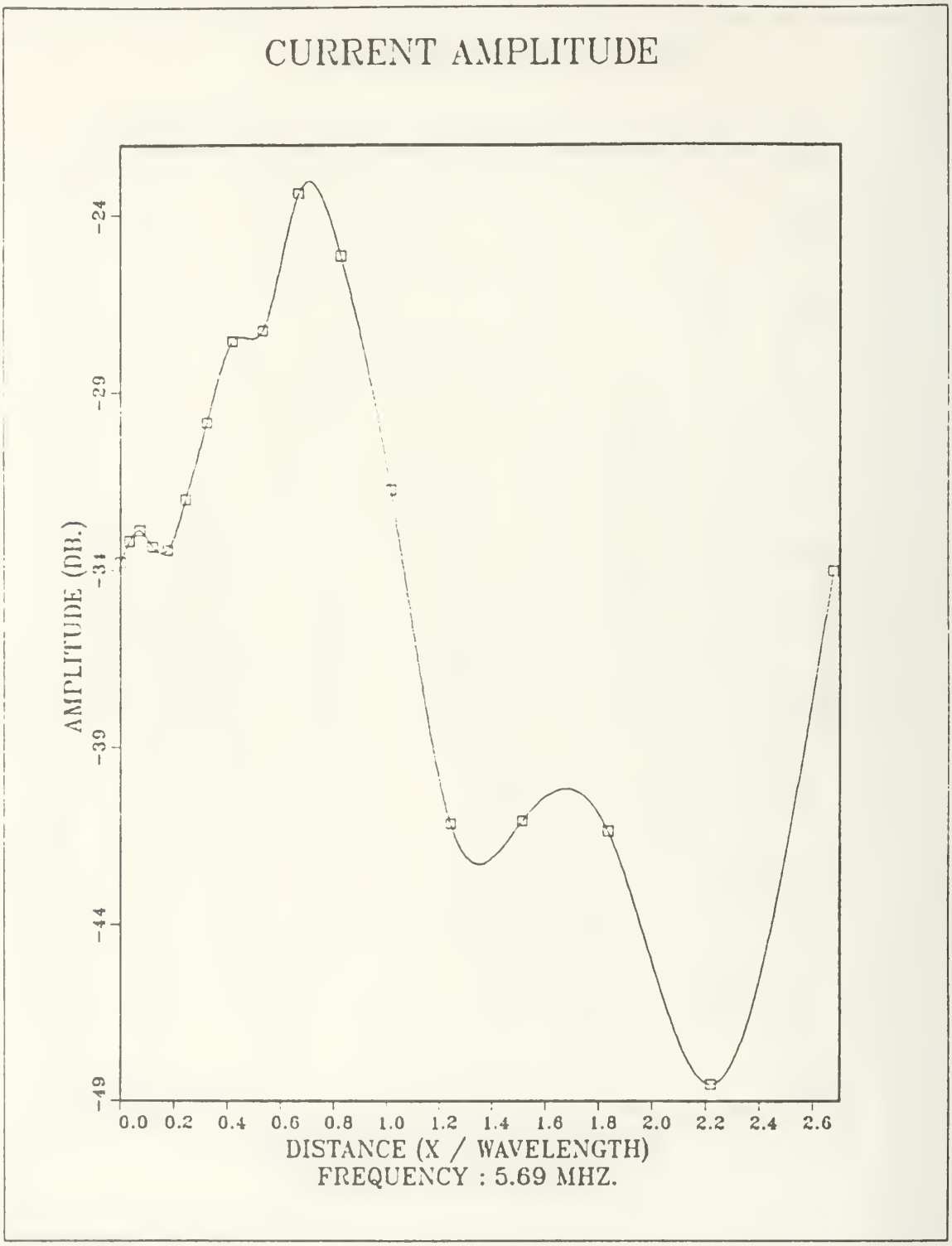

Figure E.13 Current Amplitude, Frequency : 5.69 MHz.

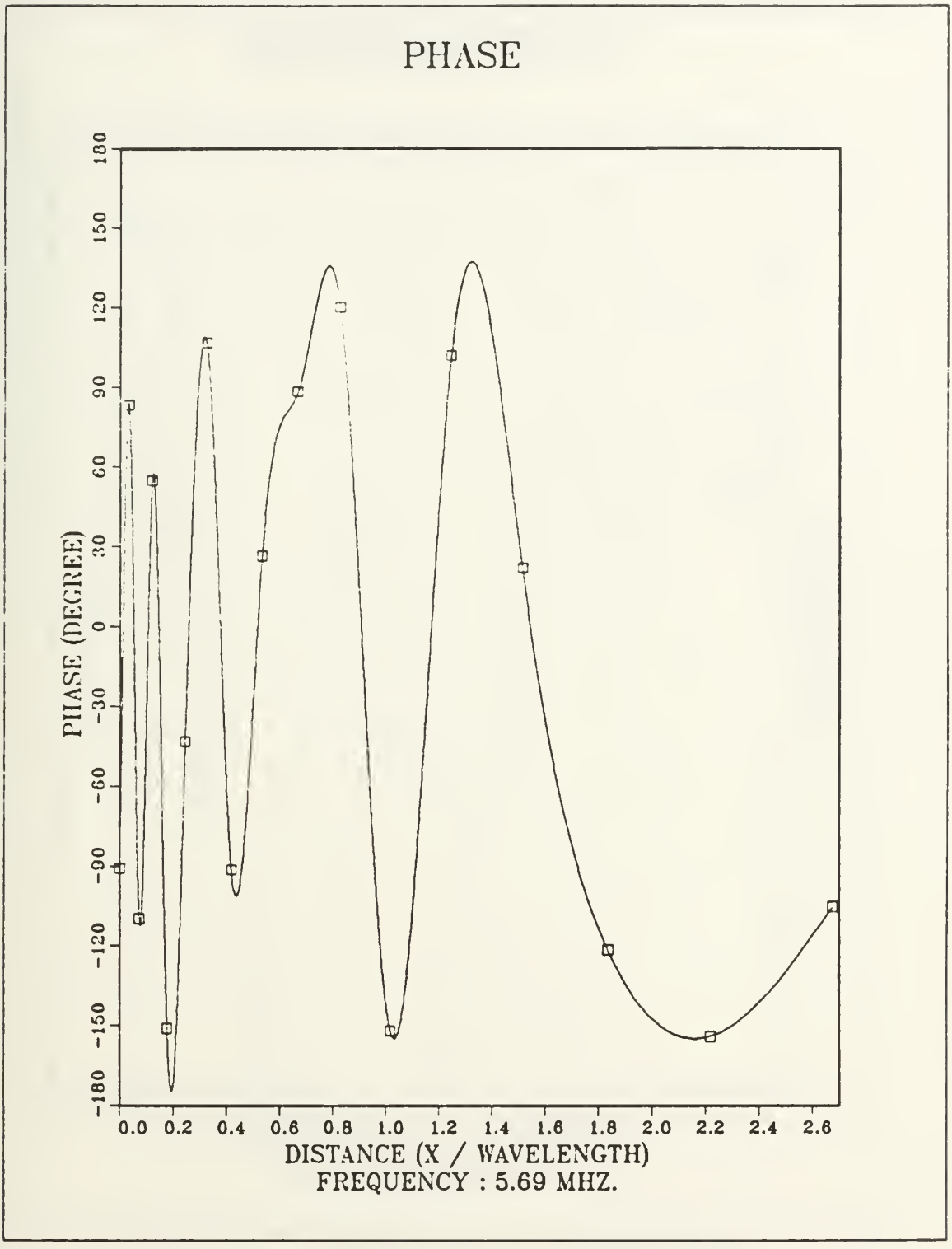

Figure E.14 Current Phase, Frequency : 5.69 MHz.

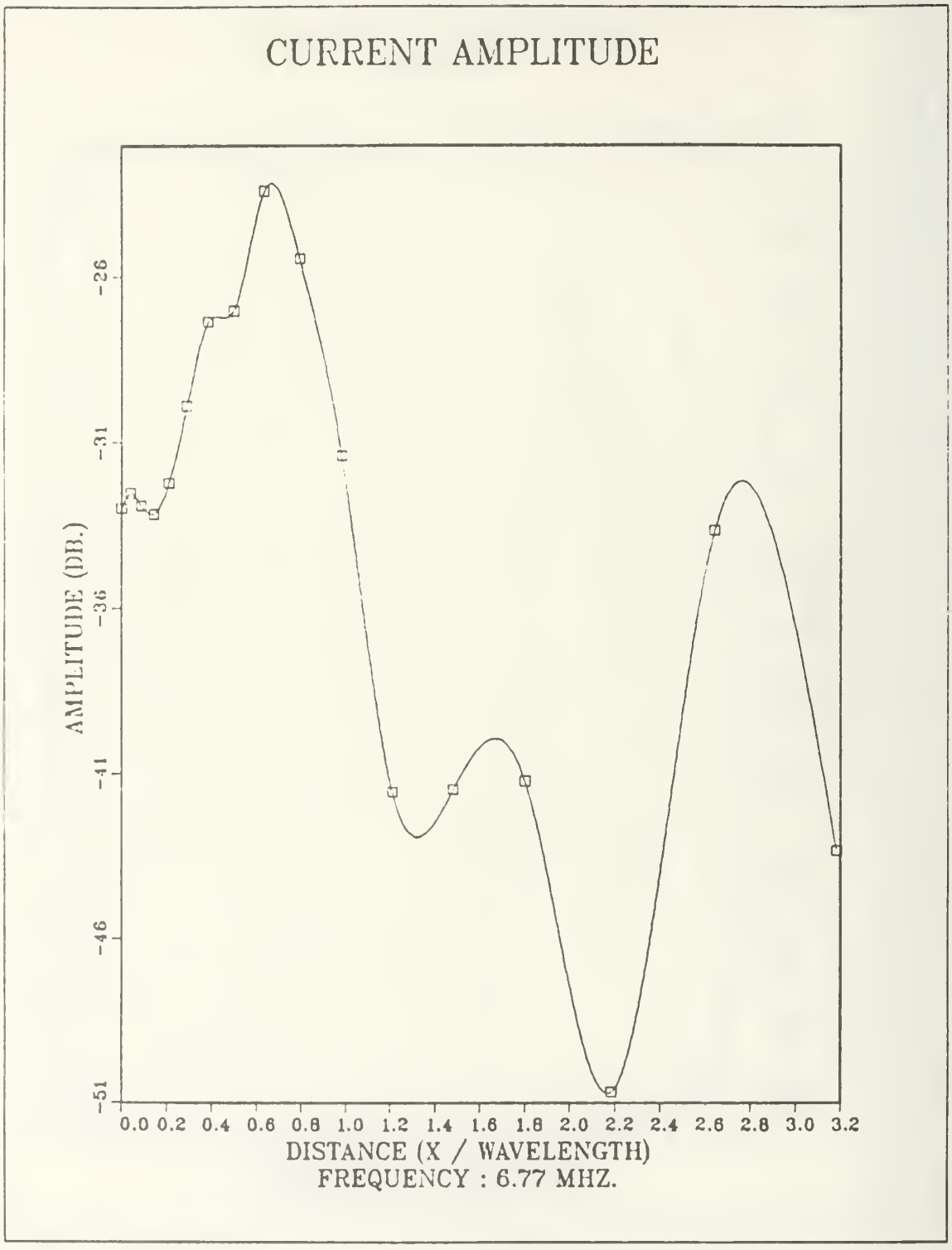

Figure E.15 Current Amplitude, Frequency : 6.77 MHz.

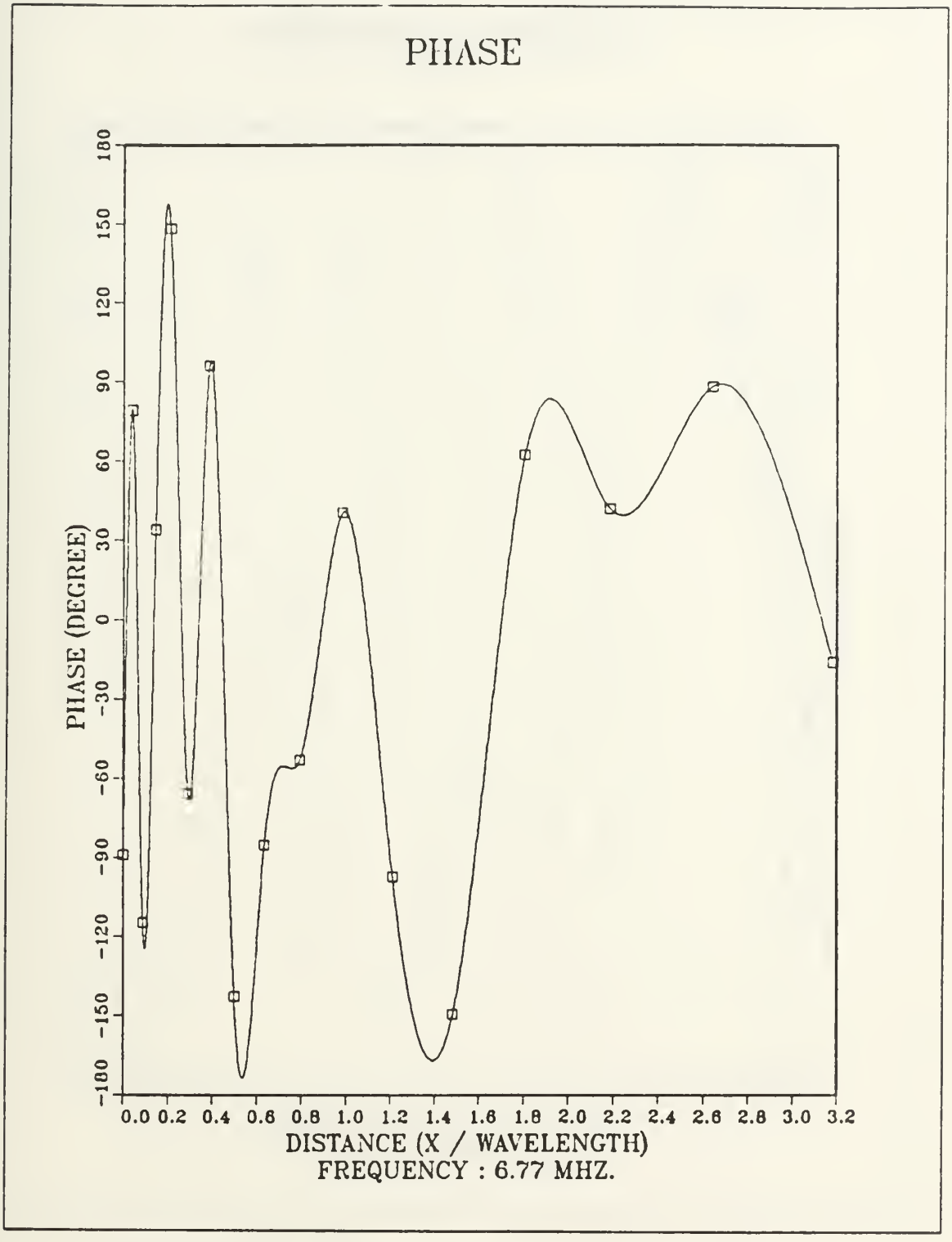

Figure E.16 Current Phase, Frequency : 6.77 MHz.

Figure E.17 Current Amplitude, Frequency : 8.06 MHz.

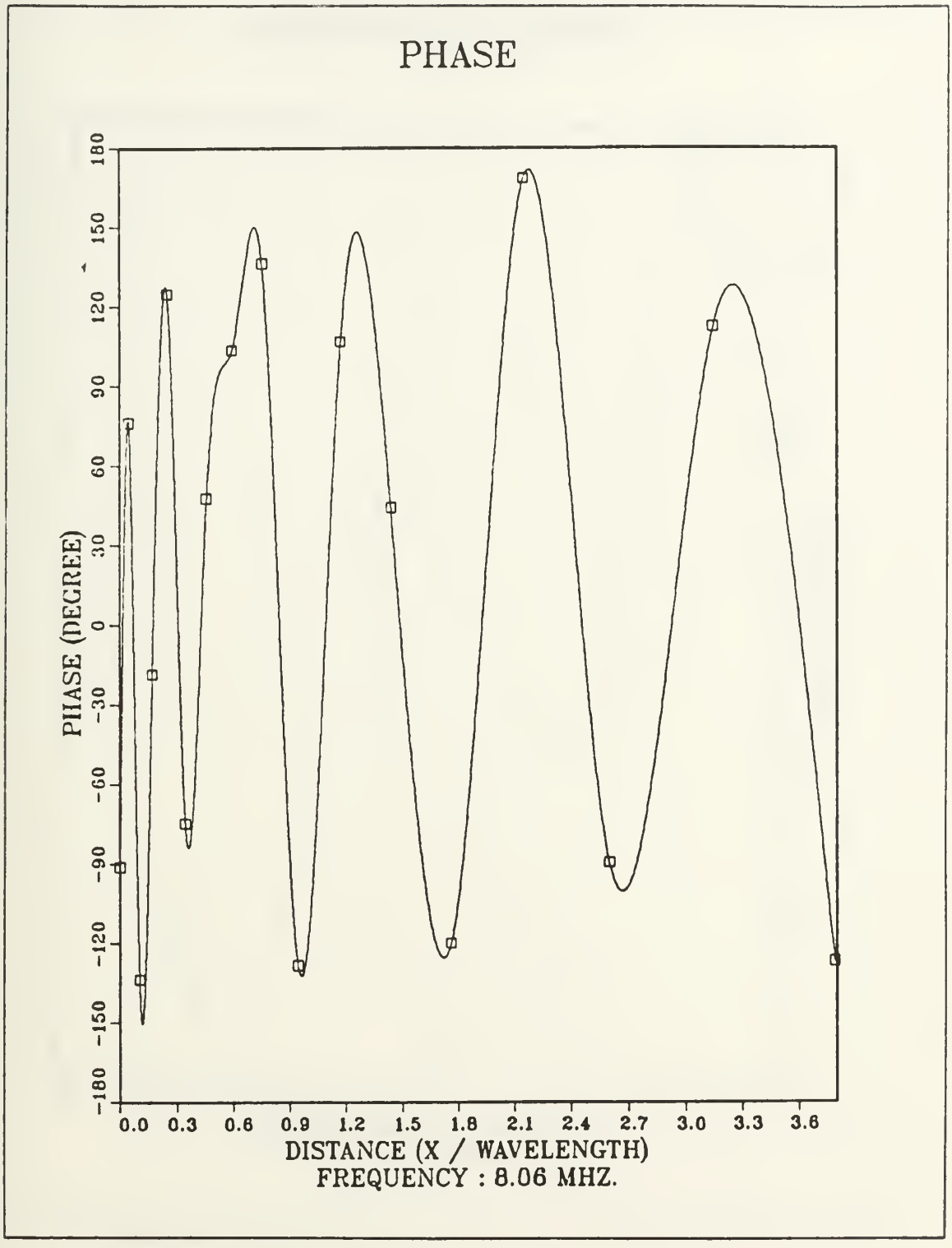

Figure E.18 Current Phase, Frequency : 8.06 MHz.

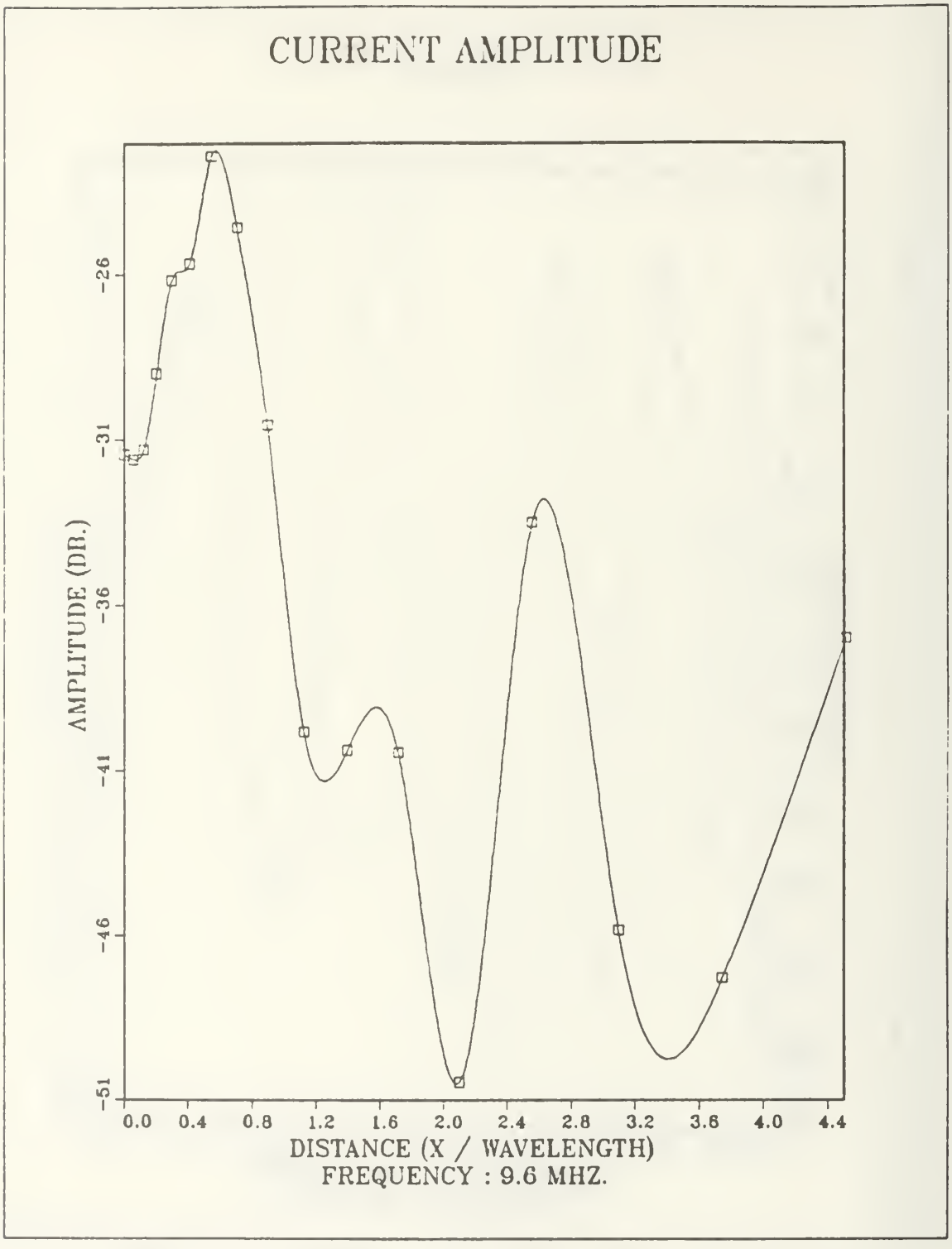

Figure E.19 Current Amplitude, Frequency : 9.6 MHz.

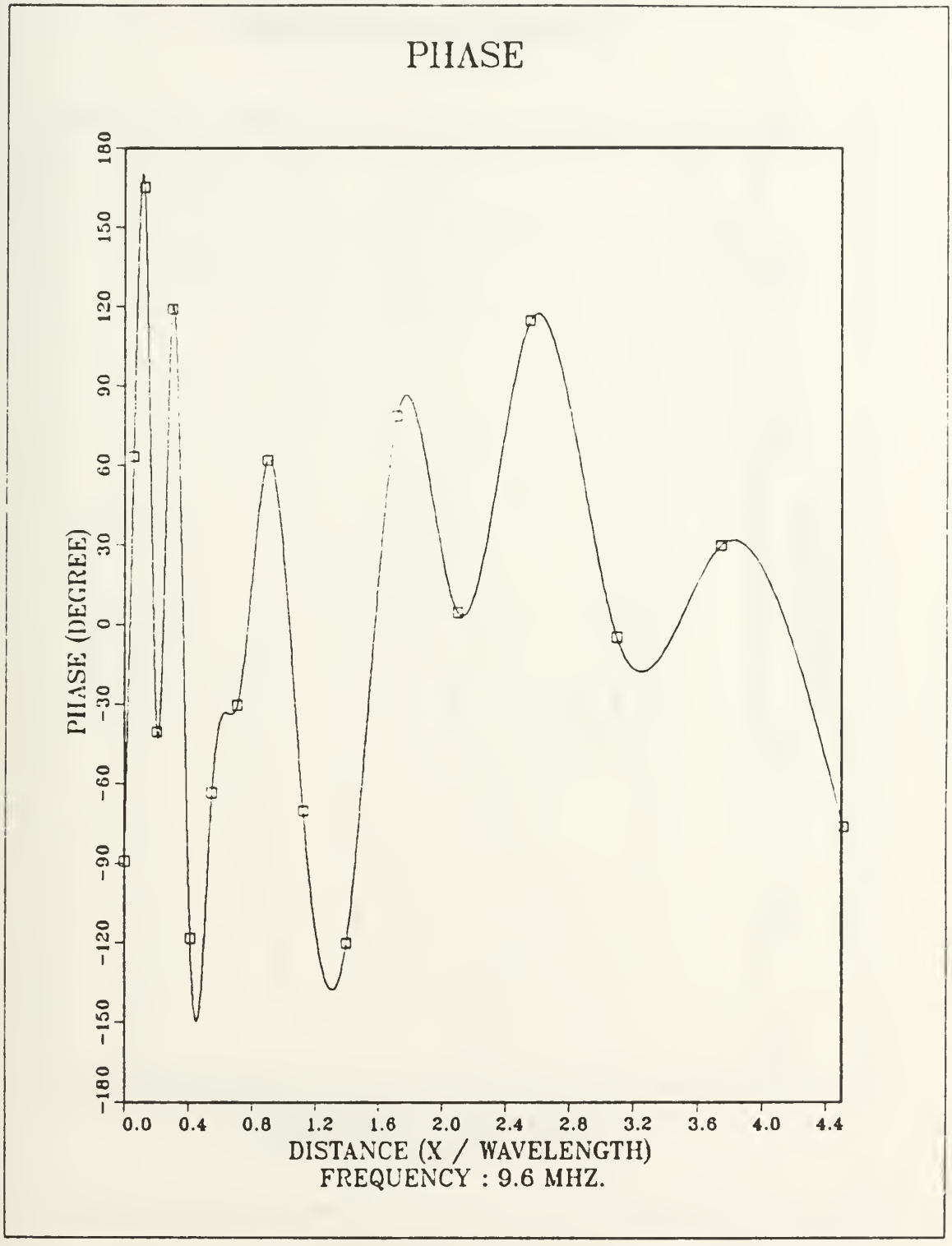

Figure E.20 Current Phase, Frequency : 9.6 MHz.

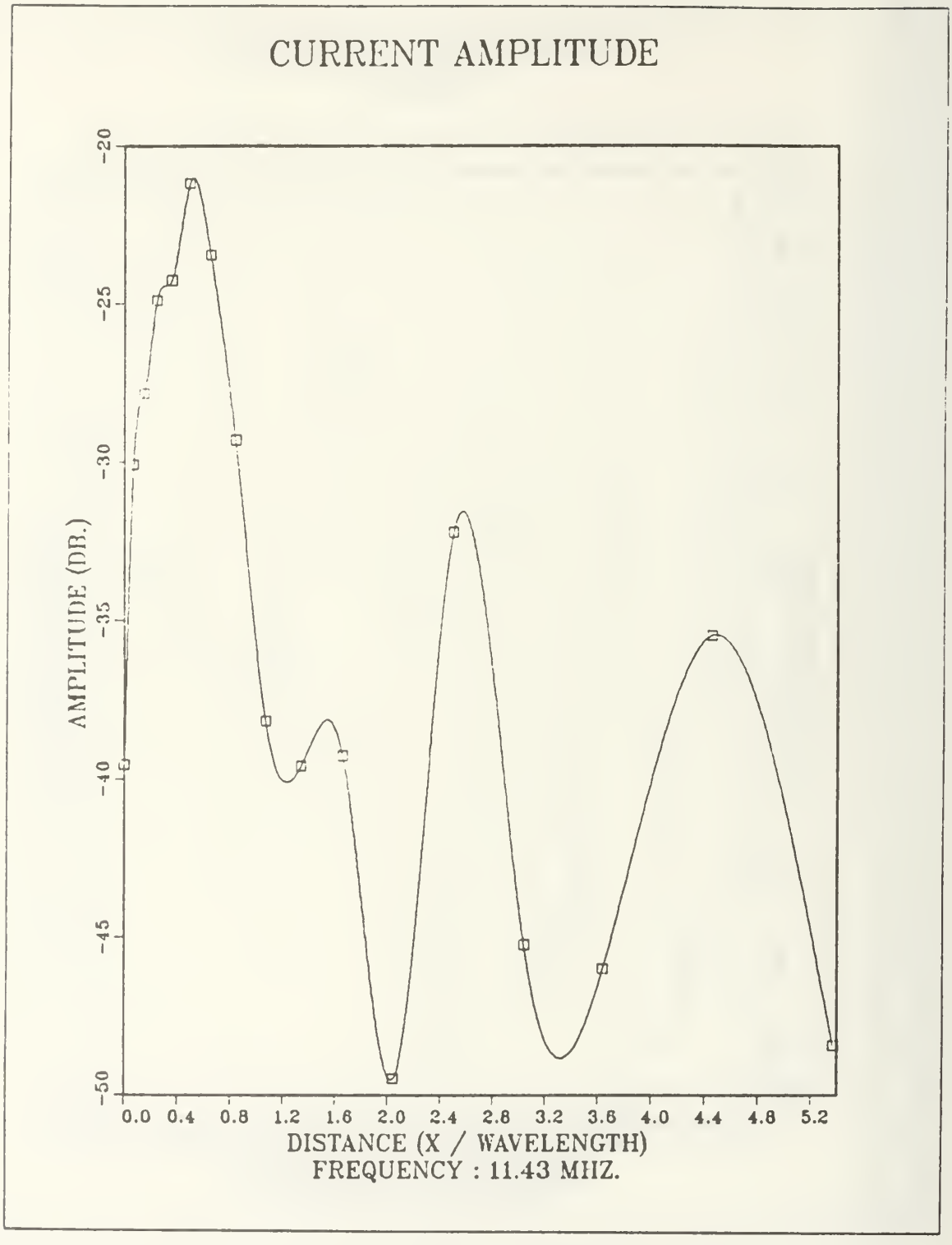

Figure E.21 Current Amplitude, Frequency : 11.43 MHz.

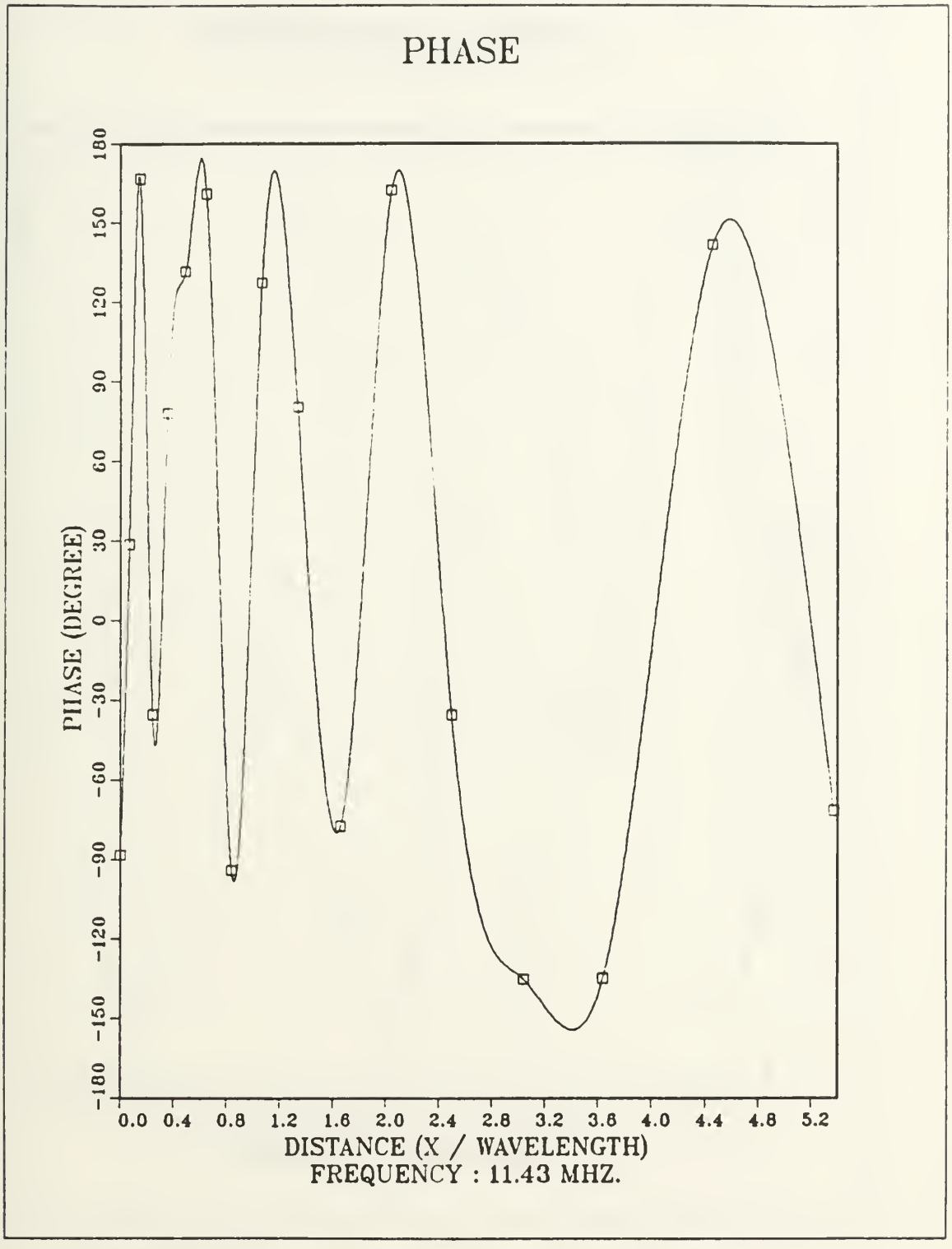

Figure E.22 Current Phase, Frequency : 11.43 MHz.

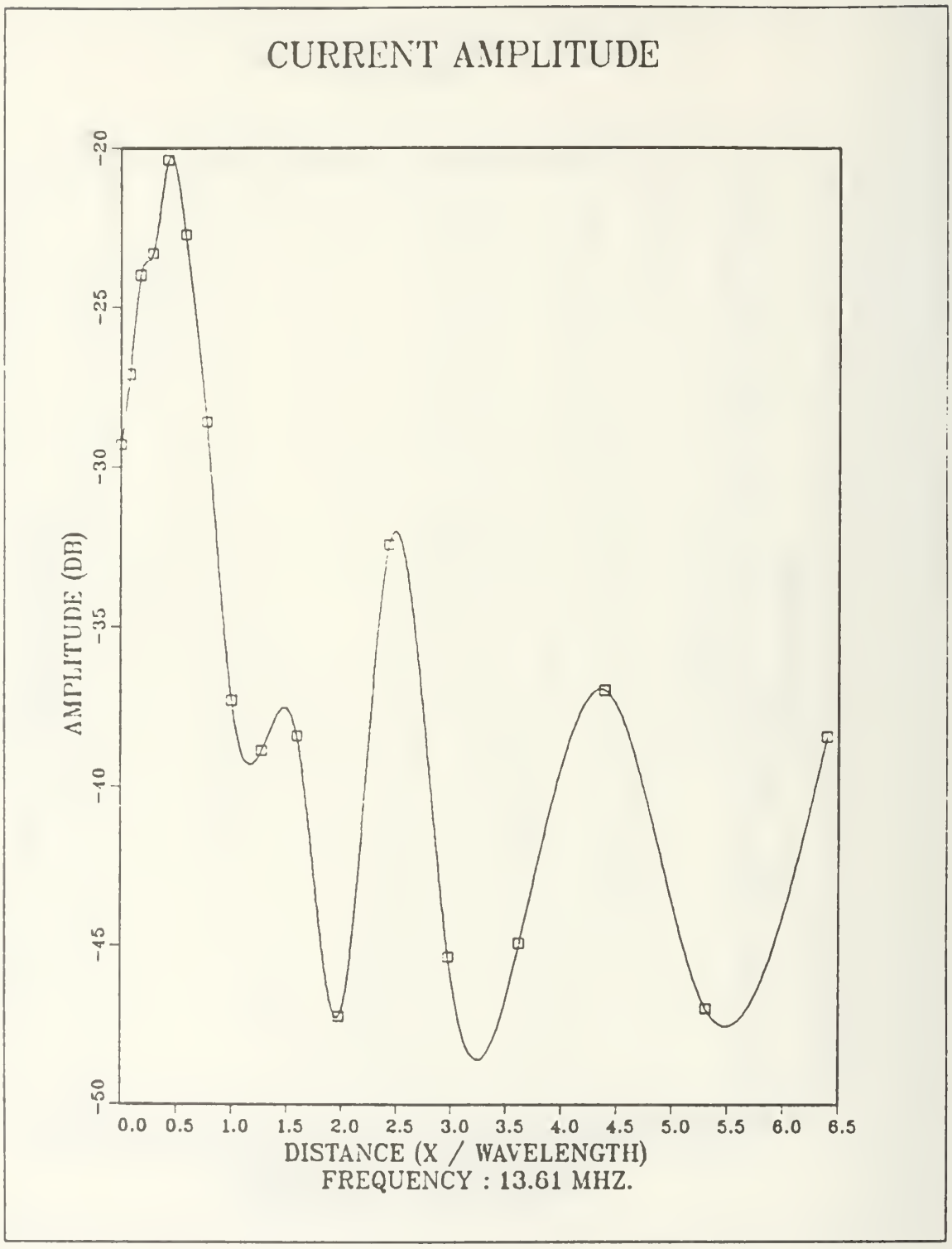

Figure E.23 Current Amplitude, Frequency : 13.61 MHz.

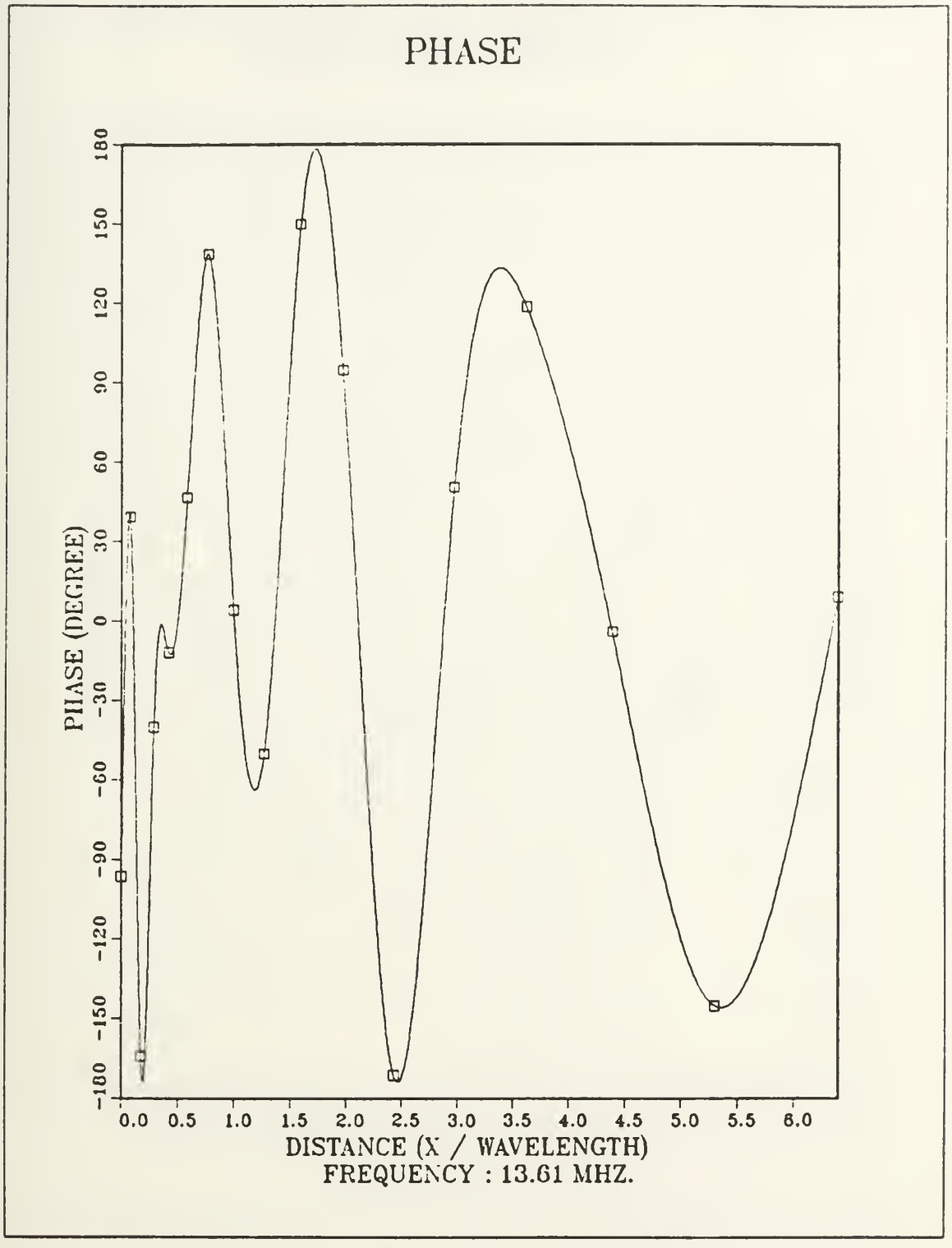

Figure E.24 Current Phase, Frequency : 13.61 MHz.

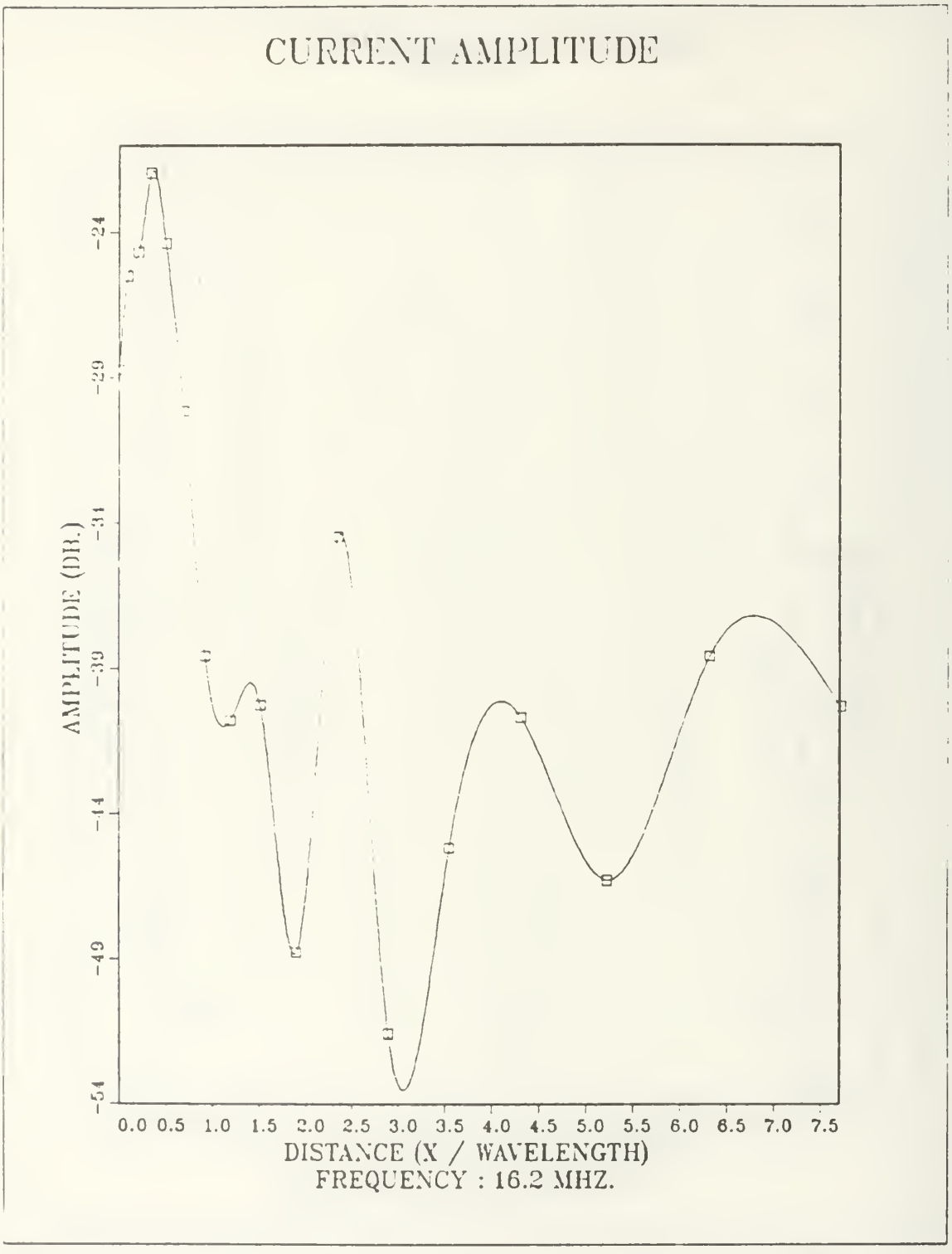

Figure E.25 Current Amplitude, Frequency : 16.2 MHz.

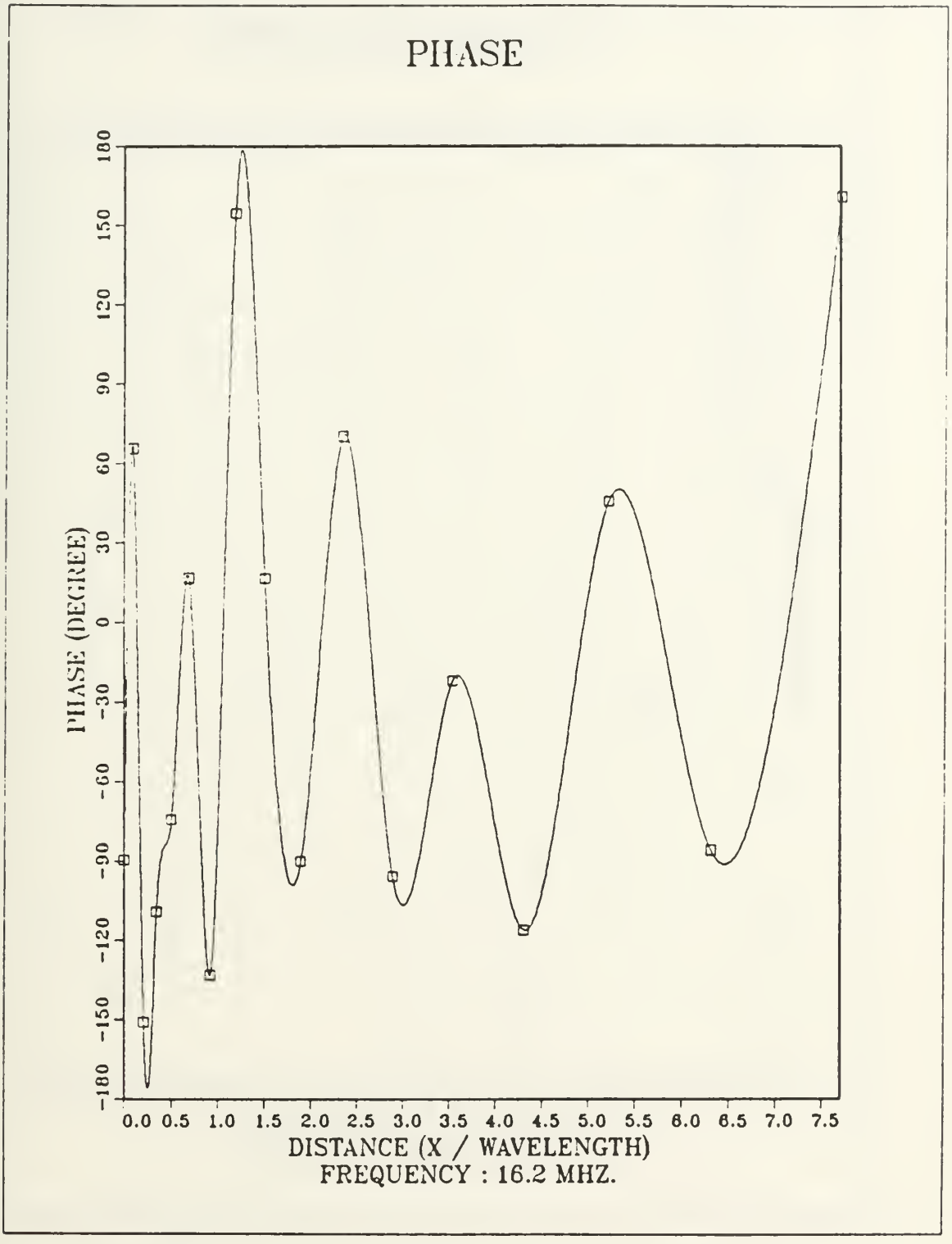

Figure E.26 Current Phase, Frequency : 16.2 MHz.

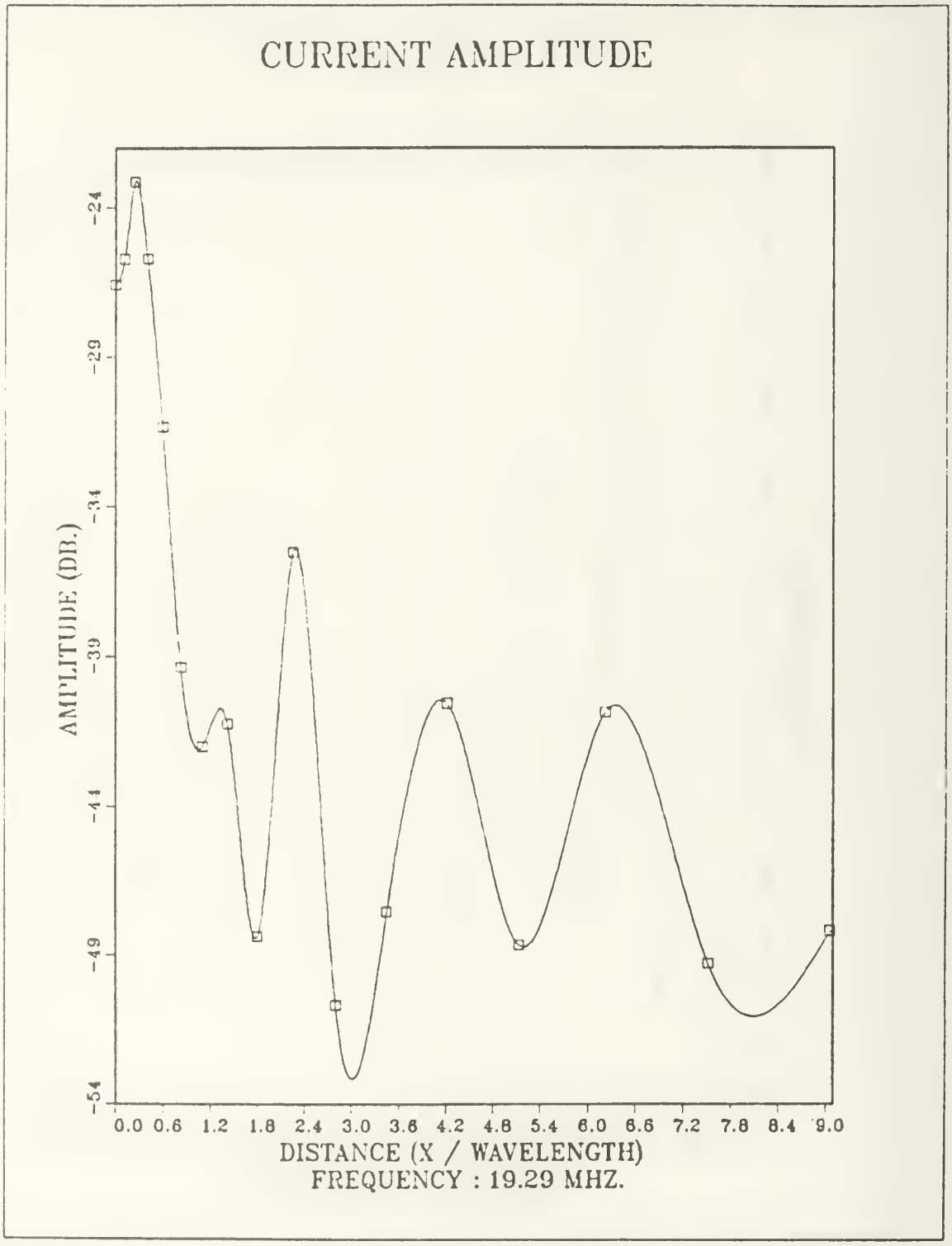

Figure E.27 Current Amplitude, Frequency : 19.29 MHz.

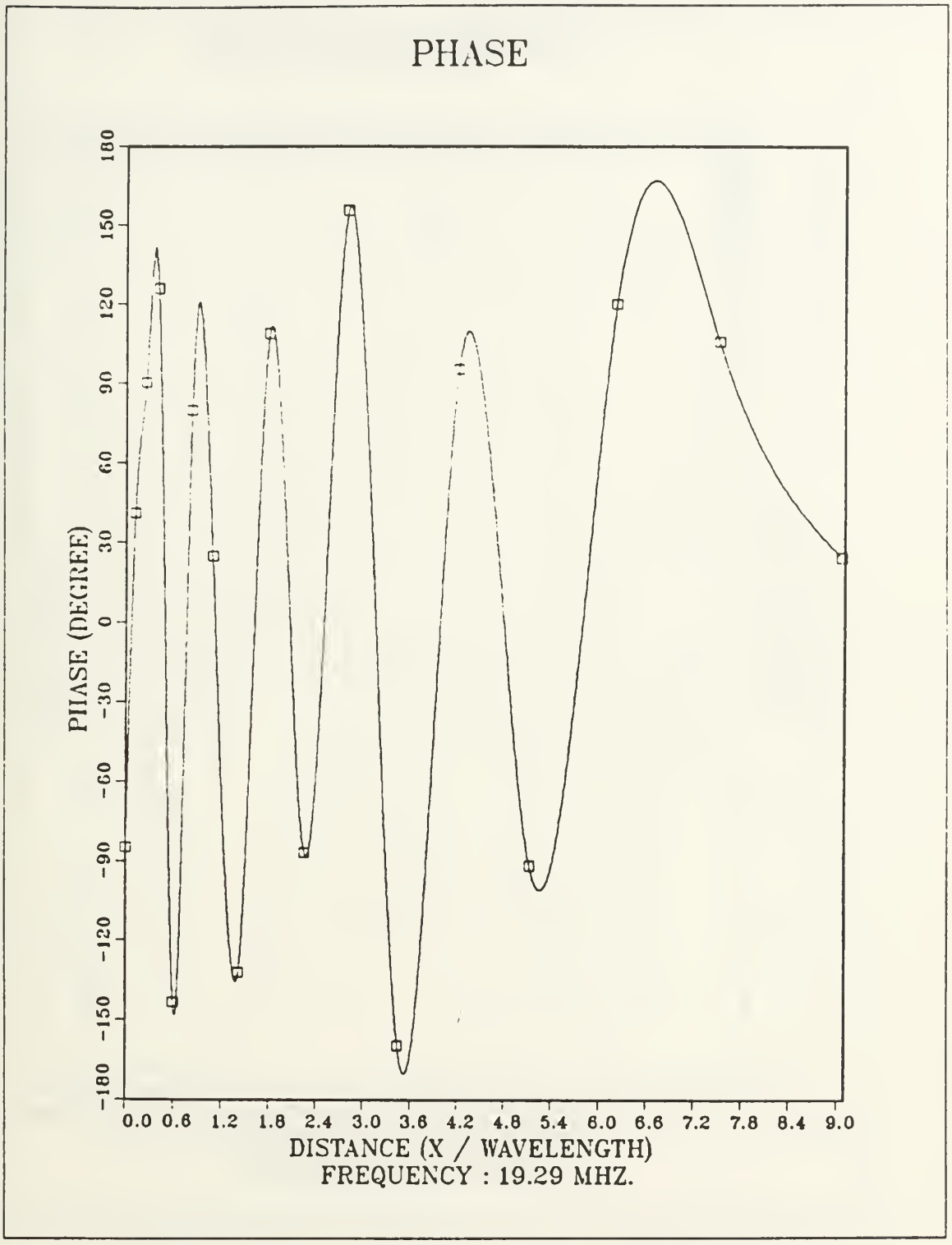

Figure E.28 Current Phase, Frequency : 19.29 MHz.

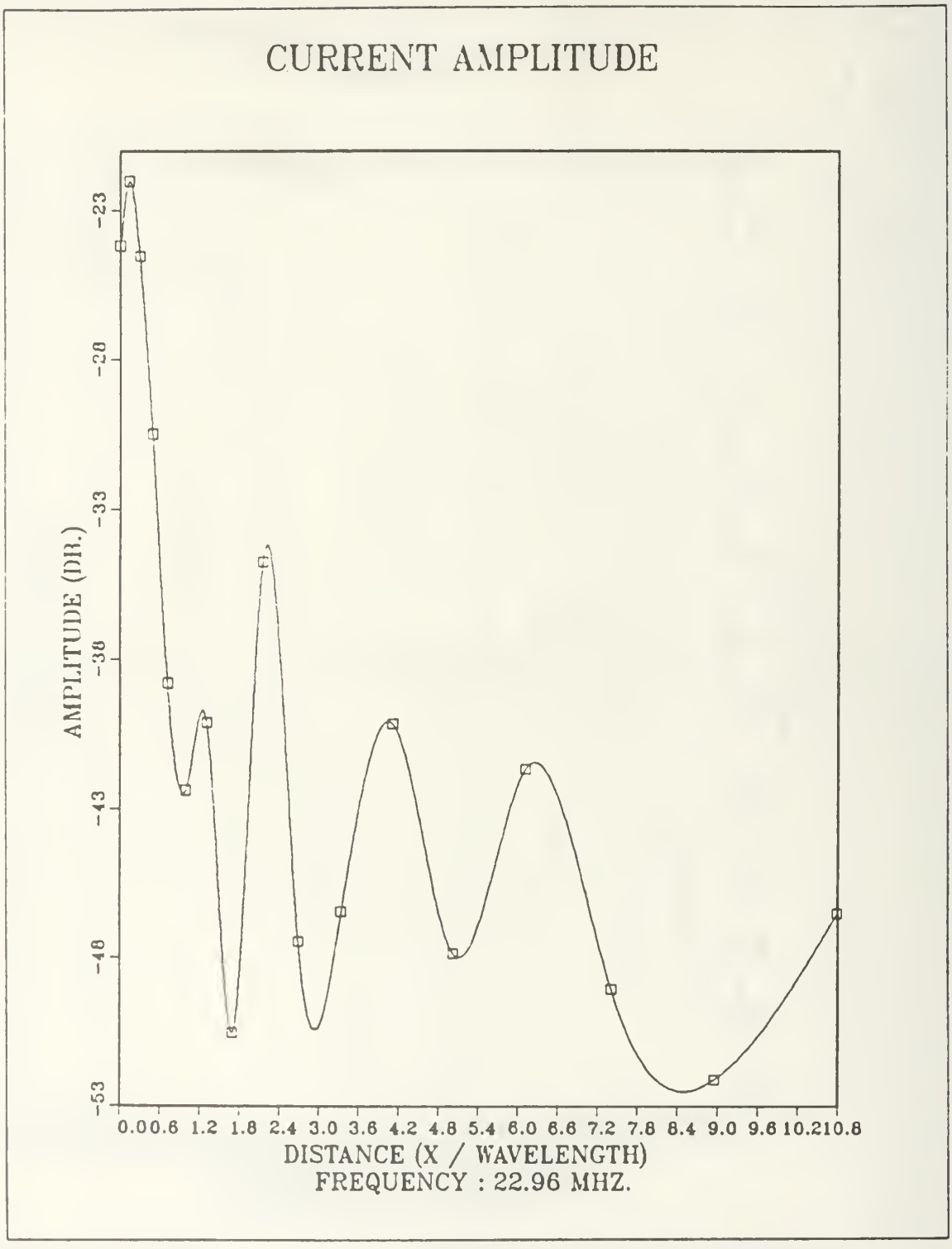

Figure E.29 Current Amplitude, Frequency : 22.96 MHz.

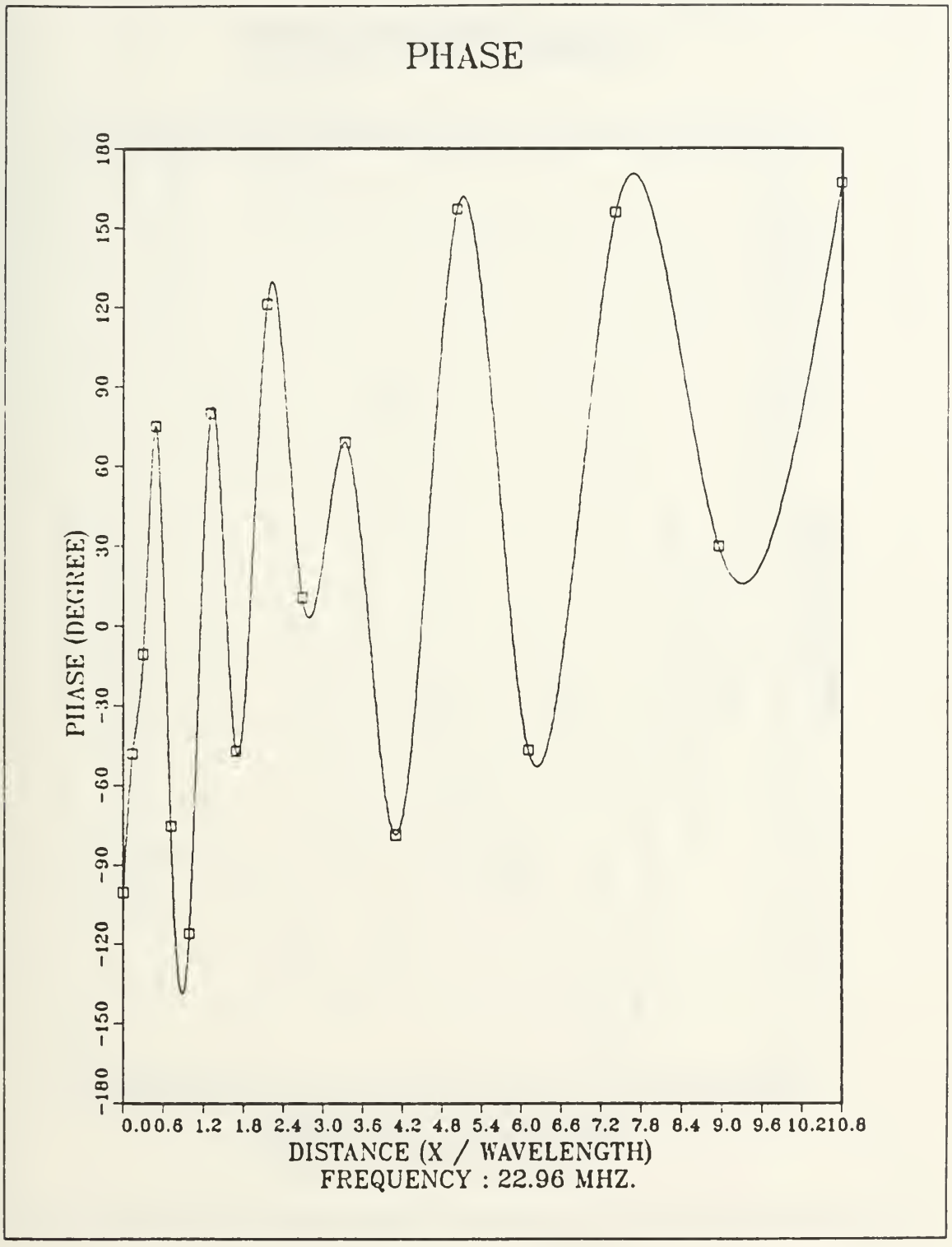

Figure E.30 Current Phase, Frequency : 22.96 MHz.

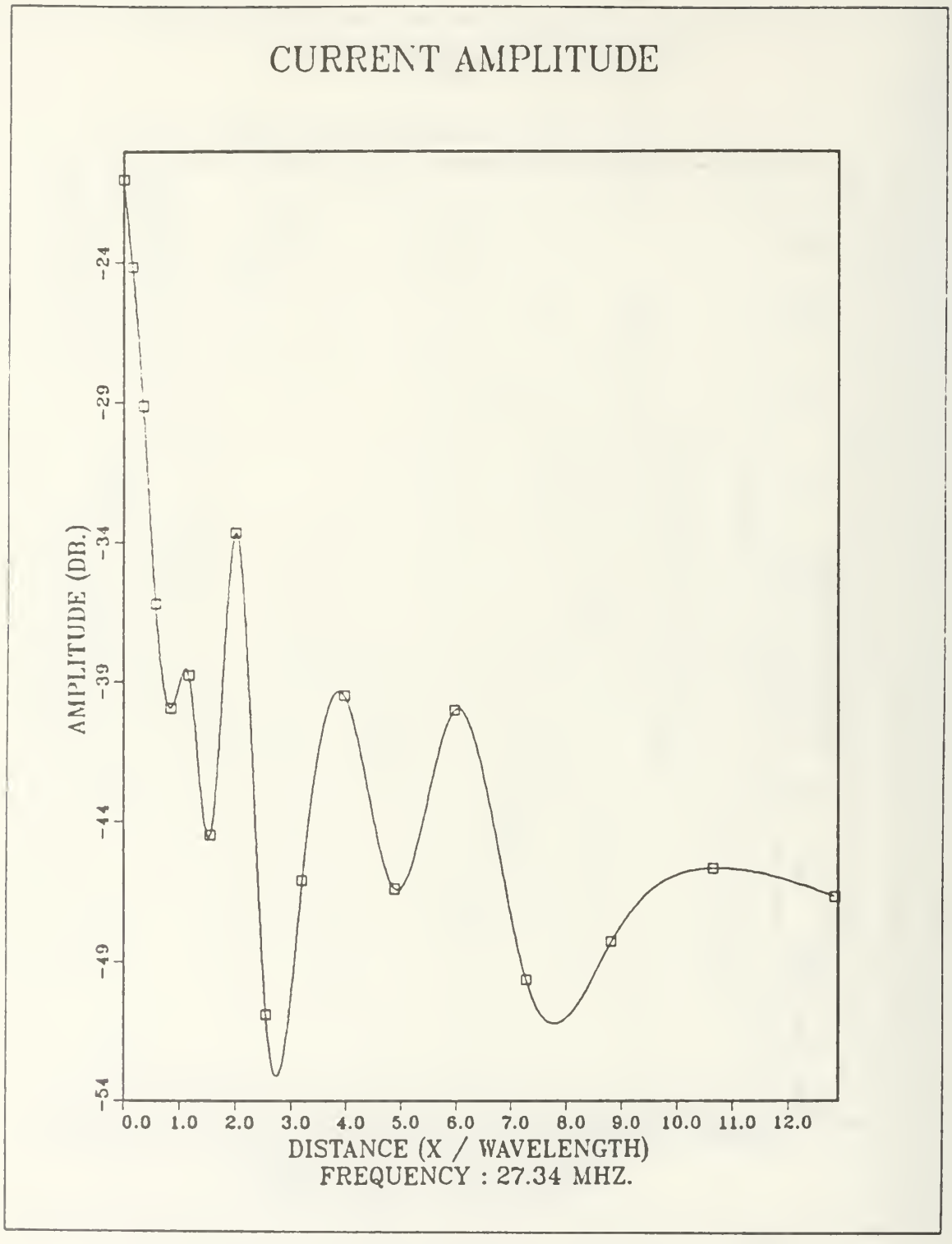

Figure E.31 Current Amplitude, Frequency : 27.34 MHz.

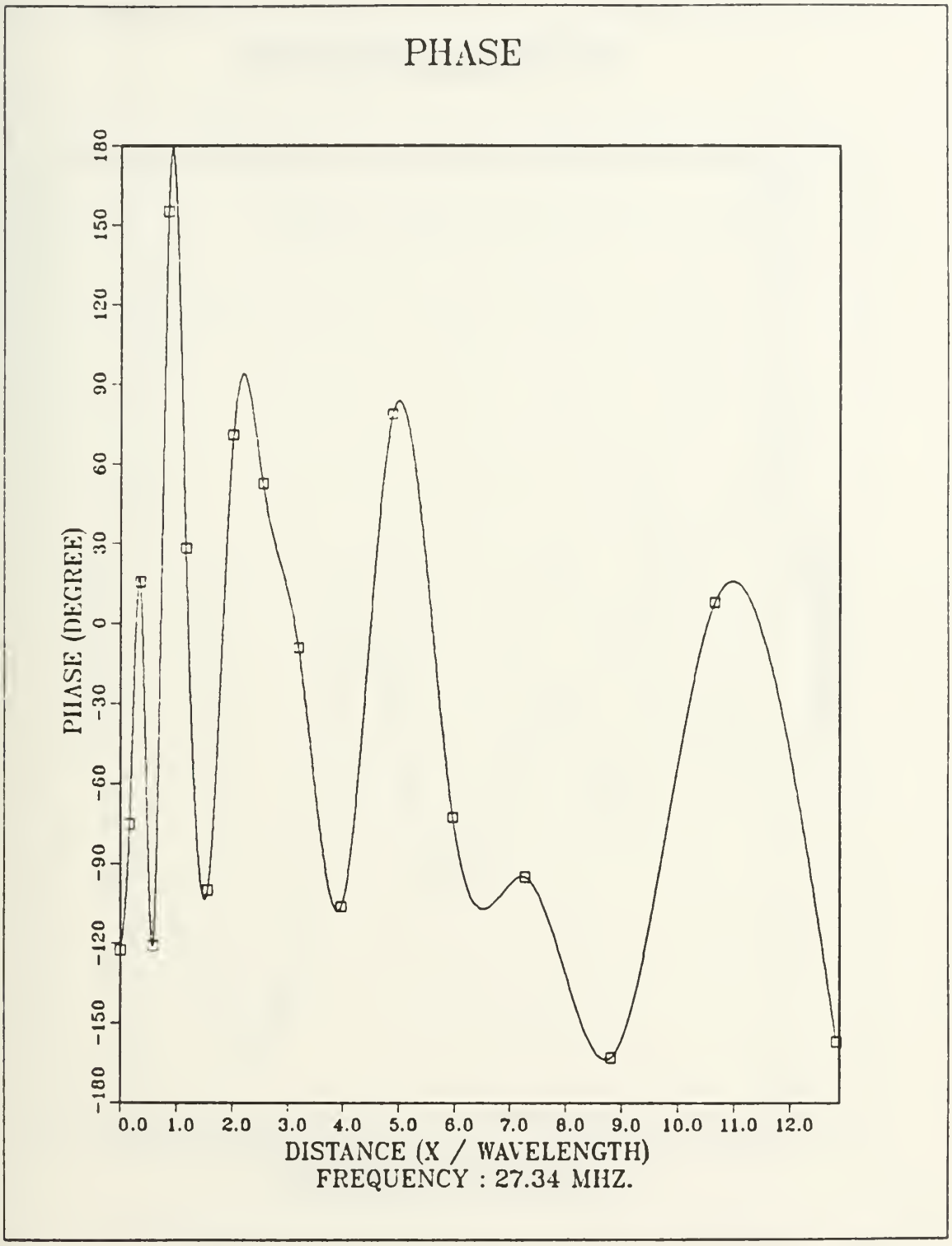

Figure E.32 Current Phase, Frequency : 27.34 MHz.

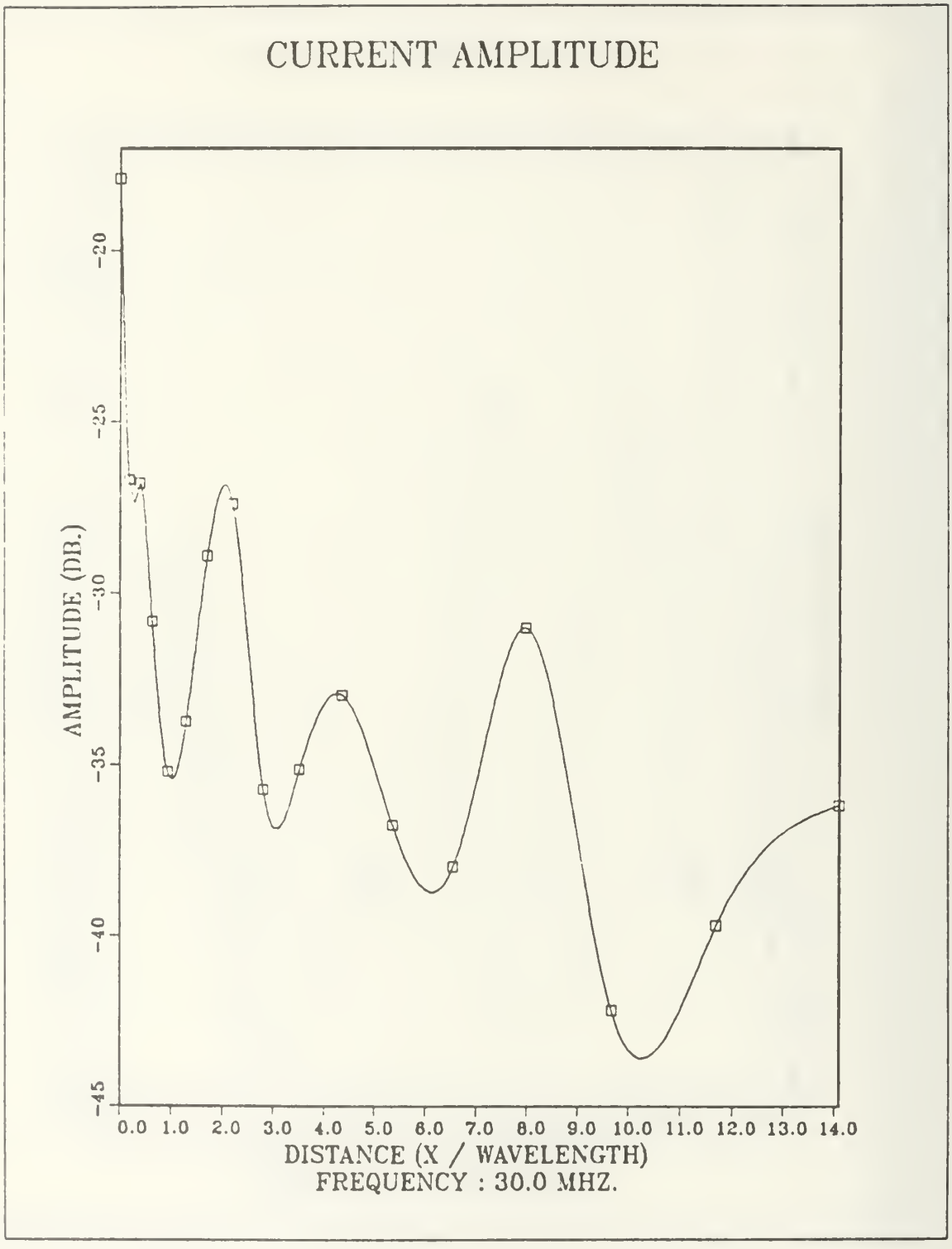

Figure E.33 Current Amplitude, Frequency : 30.0 MHz.

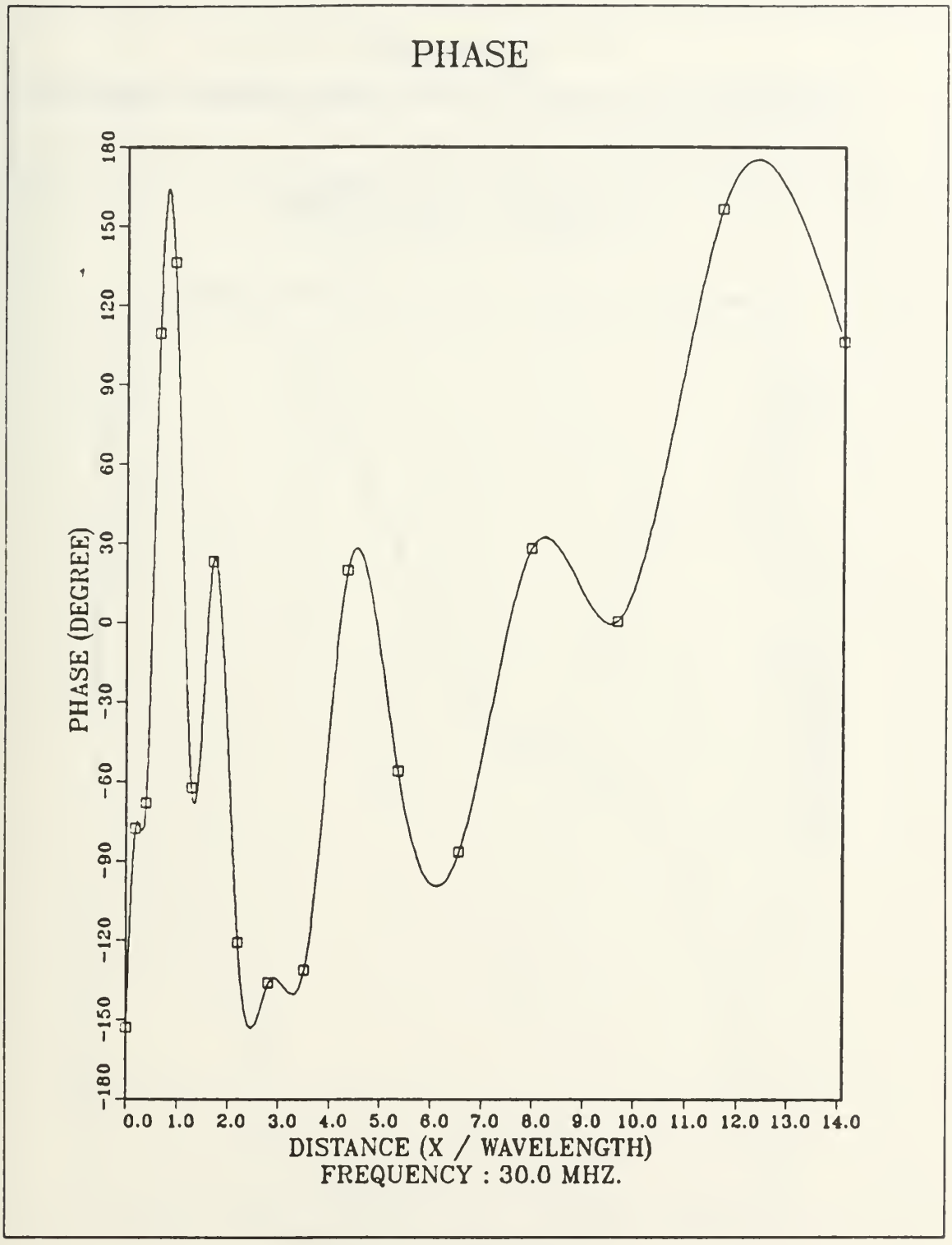

Figure E.34 Current Phase, Frequency : 30.0 MHz.

APPENDIX F
AMPLITUDE AND PHASE PLOTS OVER PERFECT GROUND

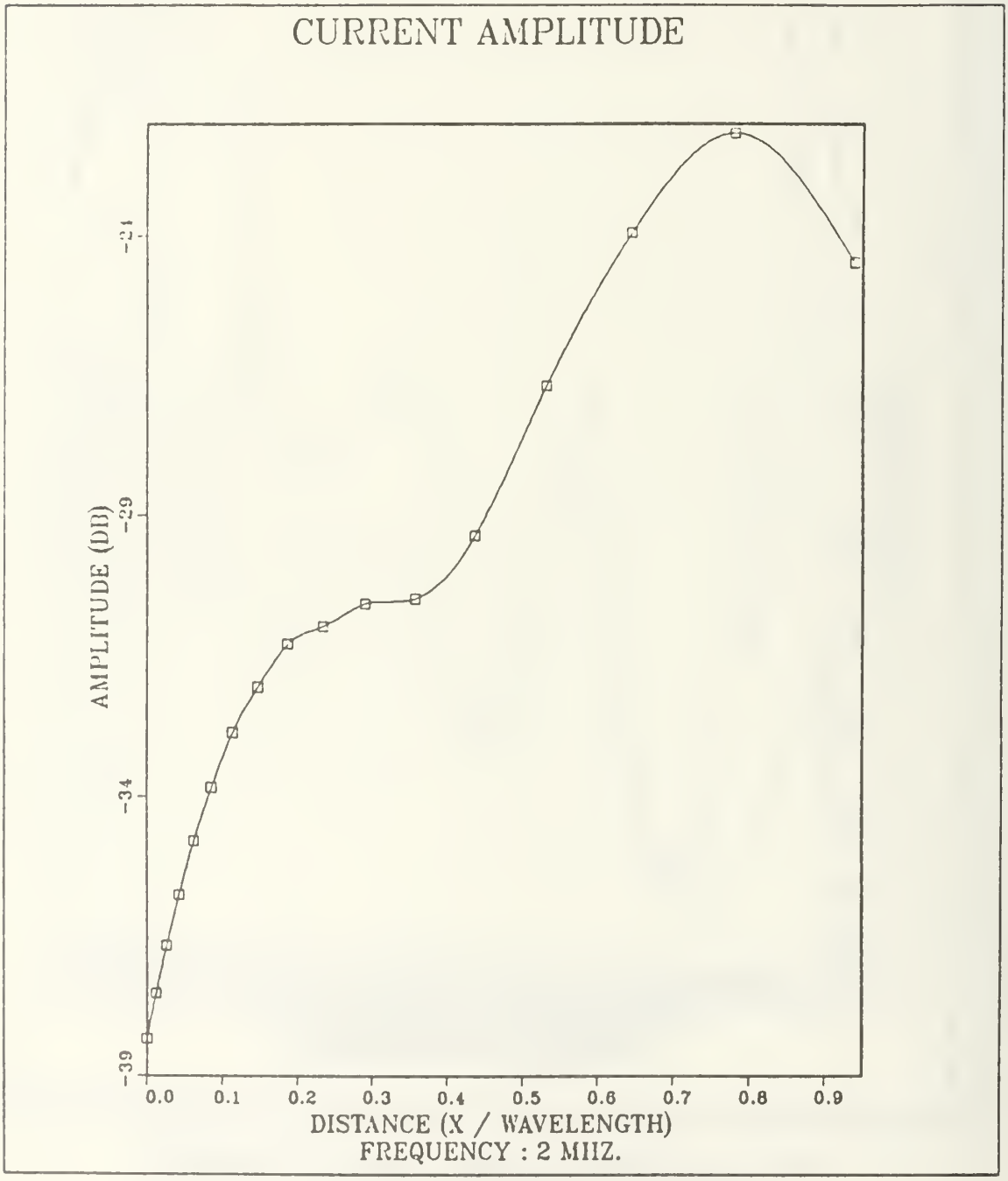

Figure F.1 Current Amplitude, Frequency : 2 MHz.

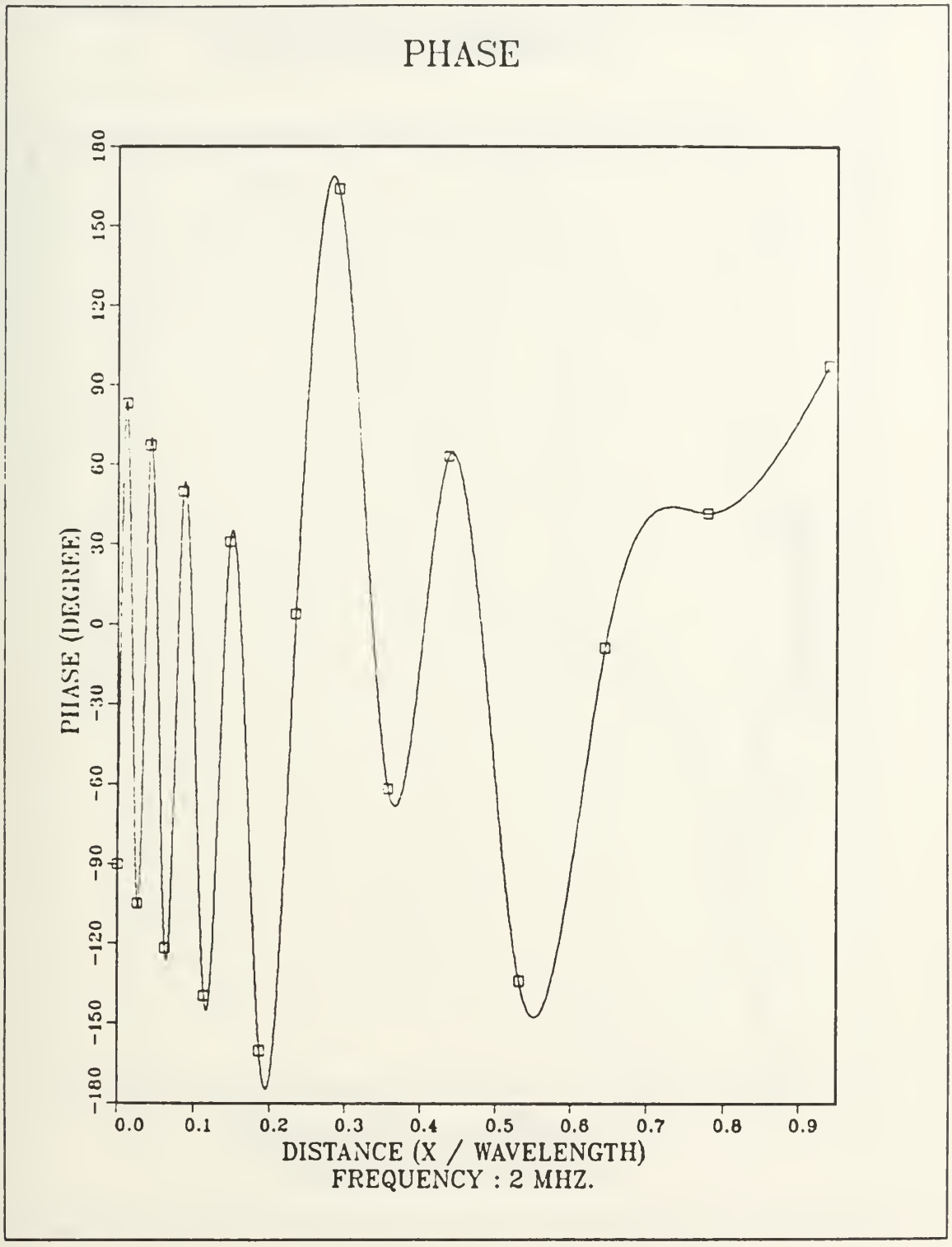

Figure F.2 Current Phase, Frequency : 2 MHz.

Figure F.3 Current Amplitude, Frequency : 2.38 MHz.

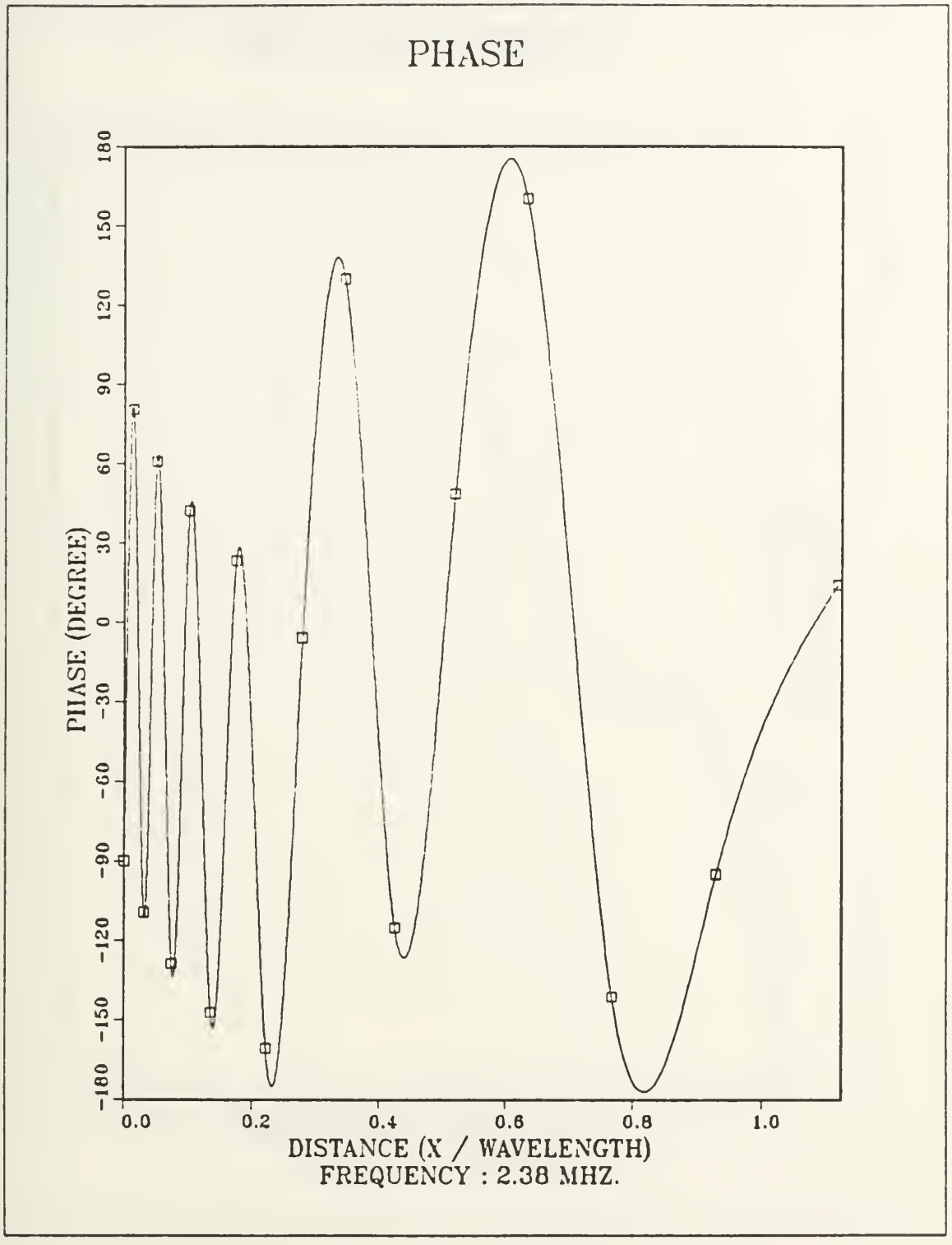

Figure F.4 Current Phase, Frequency : 2.38 MHz.

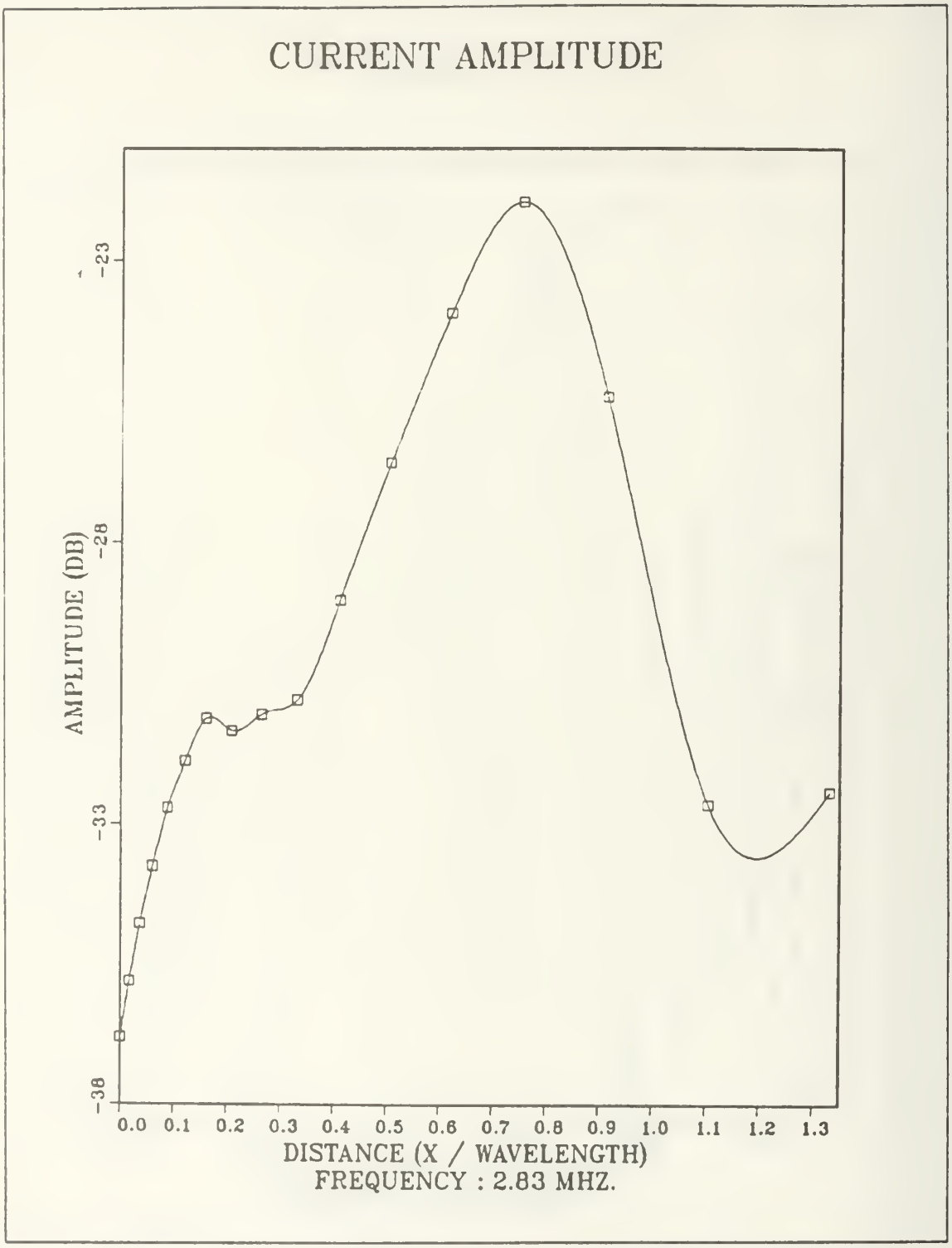

Figure F.5 Current Amplitude, Frequency : 2.83 MHz.

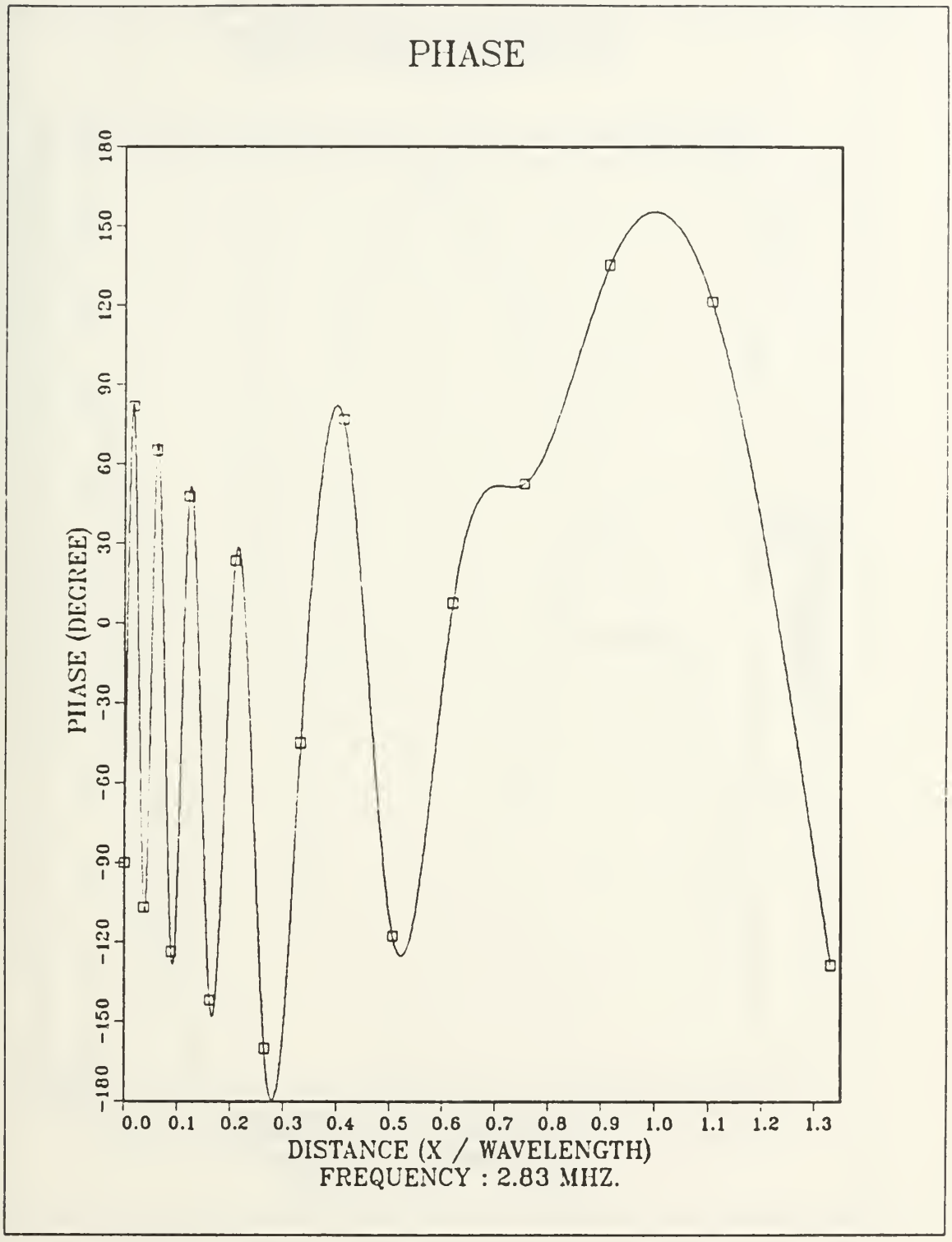

Figure F.6 Current Phase, Frequency : 2.83 MHz.

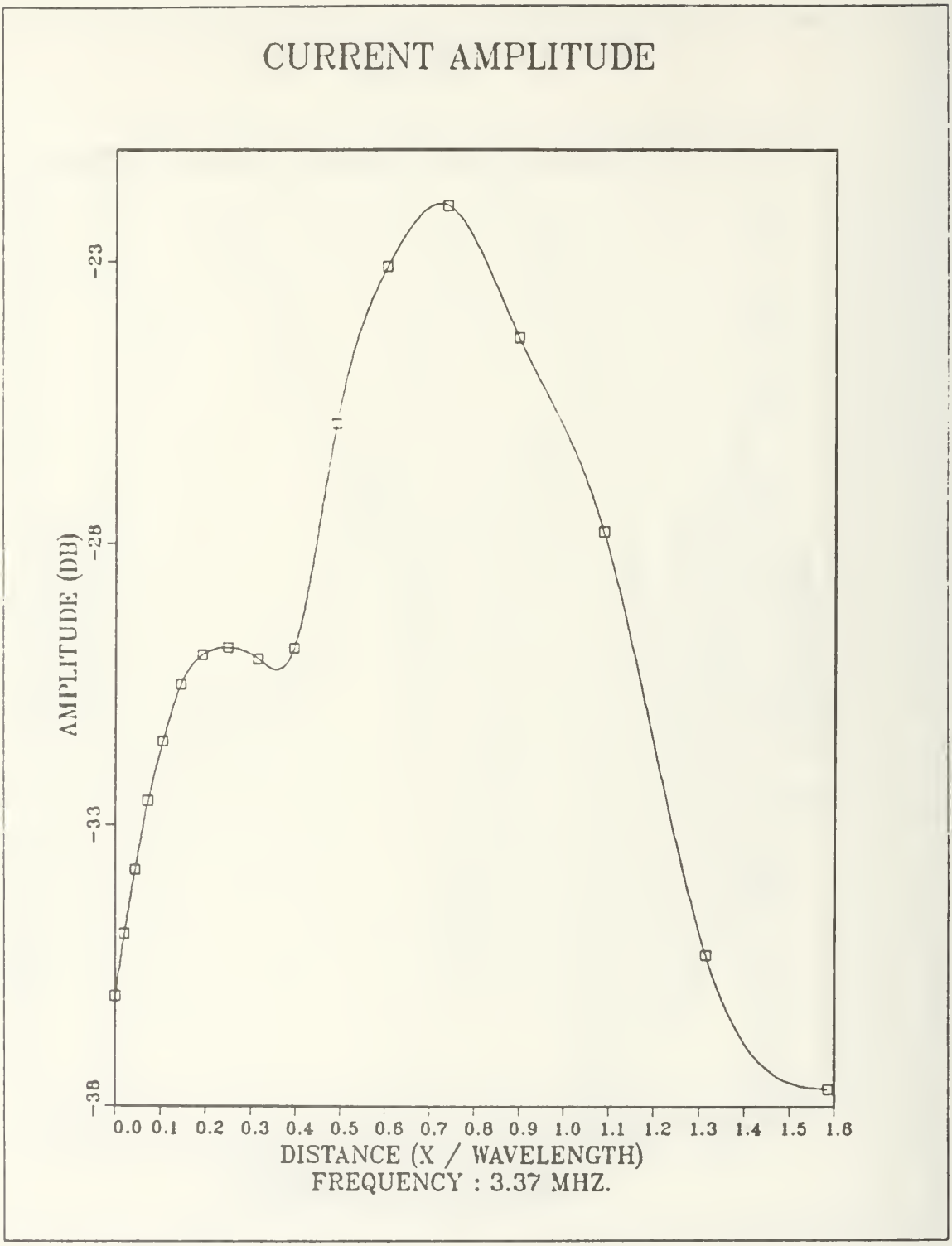

Figure F.7 Current Amplitude, Frequency : 3.37 MHz.

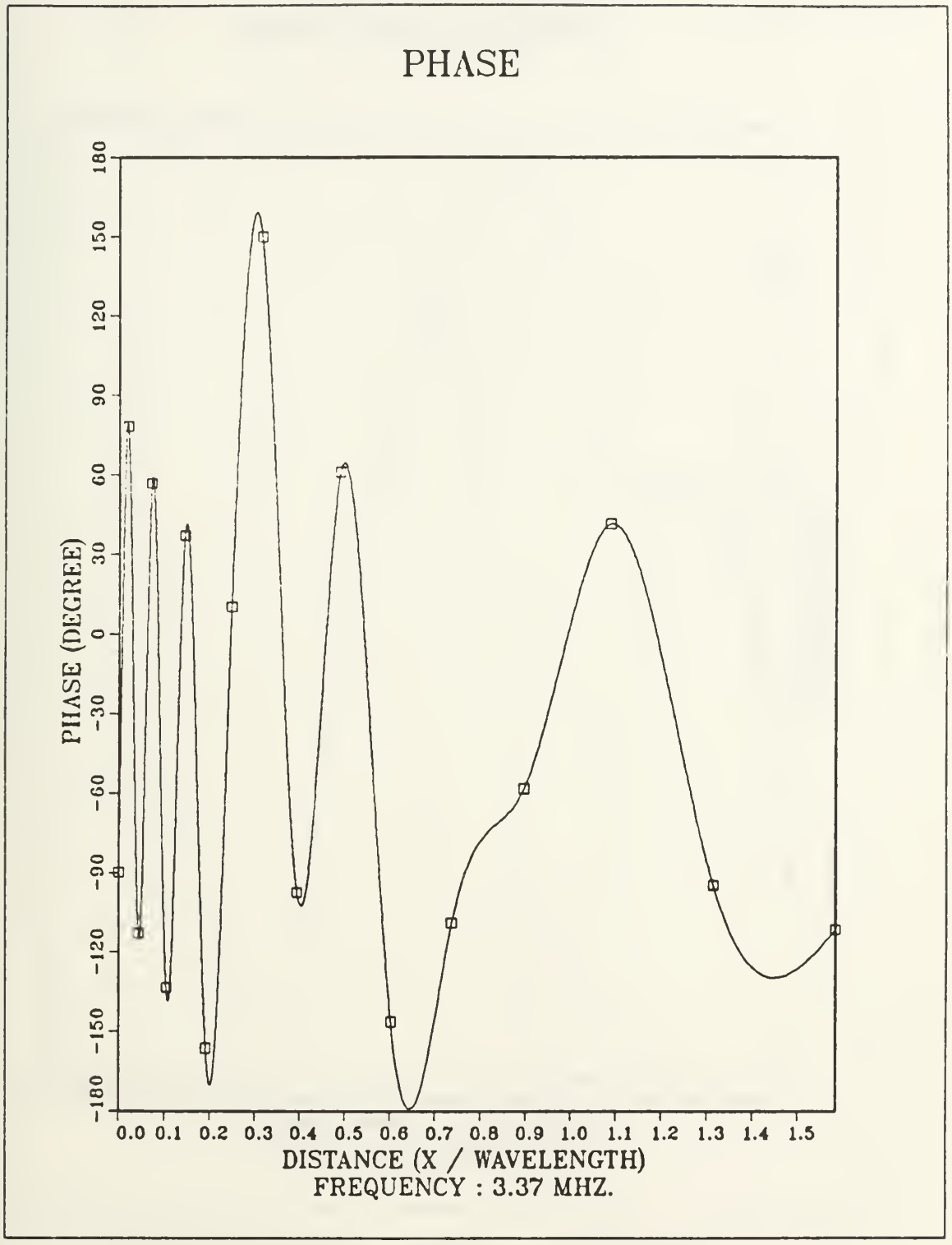

Figure F.8 Current Phase, Frequency : 3.37 MHz.

Figure F.9 Current Amplitude, Frequency : 4.01 MHz.

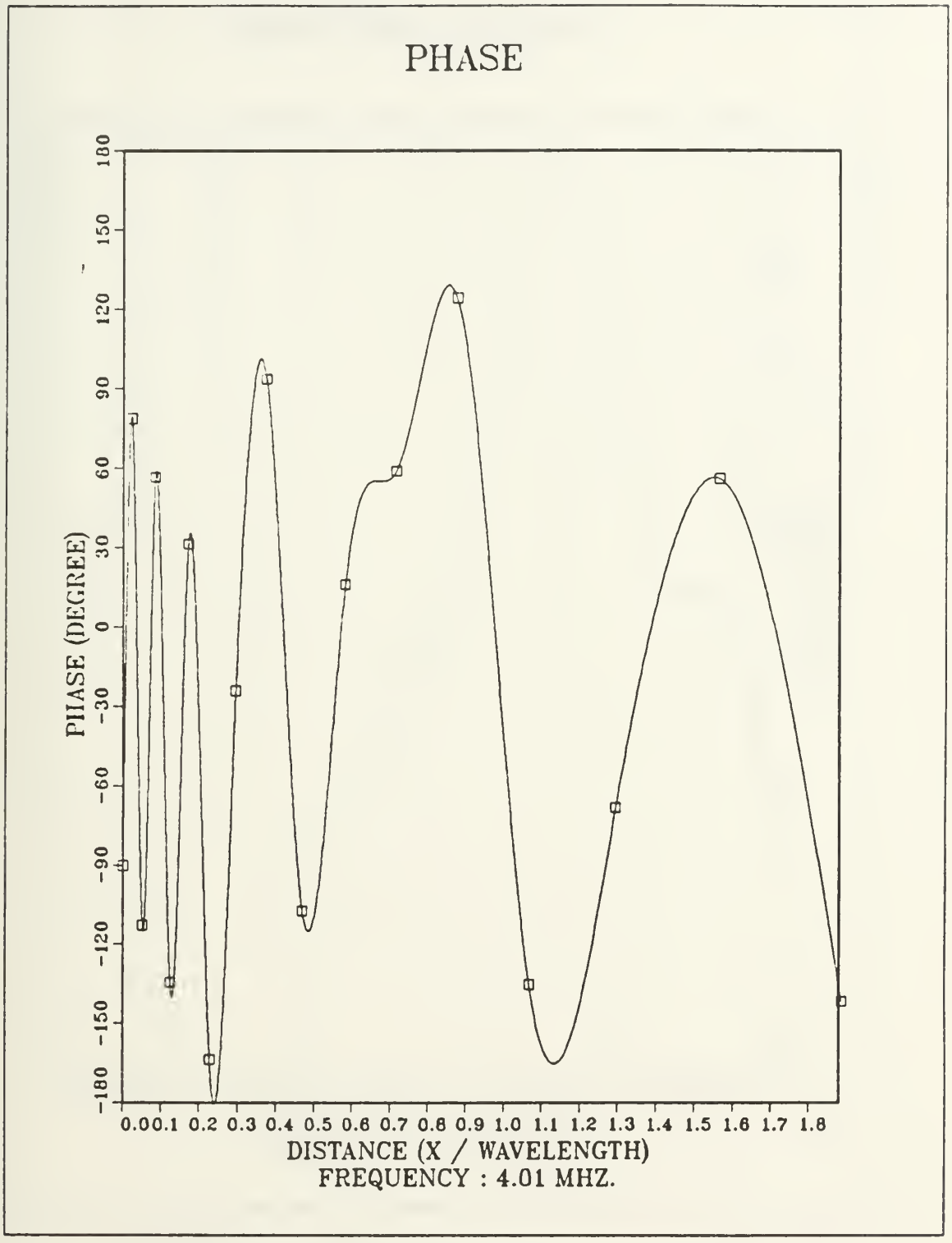

Figure F.10 Current Phase, Frequency : 4.01.

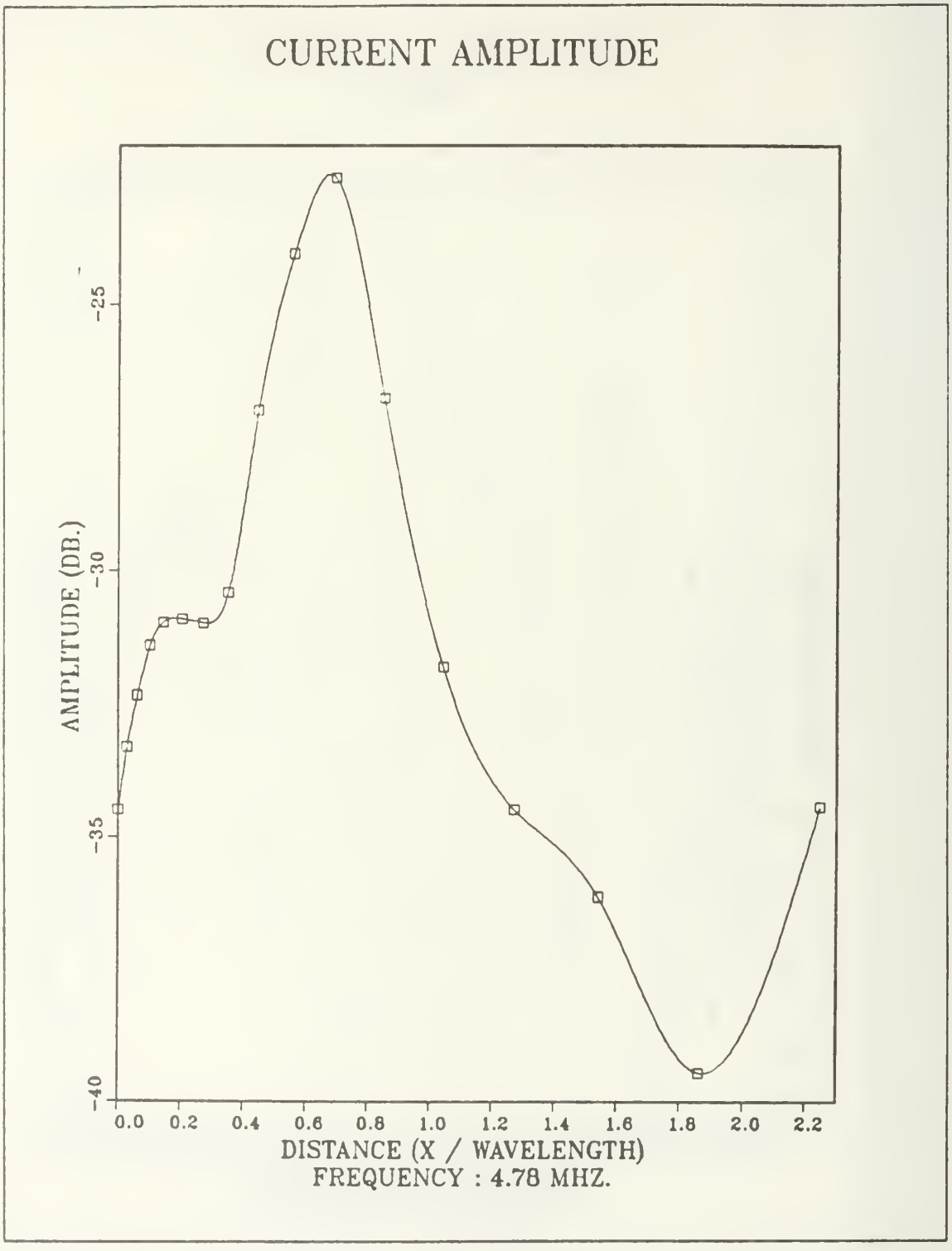

Figure F.11 Current Amplitude, Frequency : 4.78 MHz.

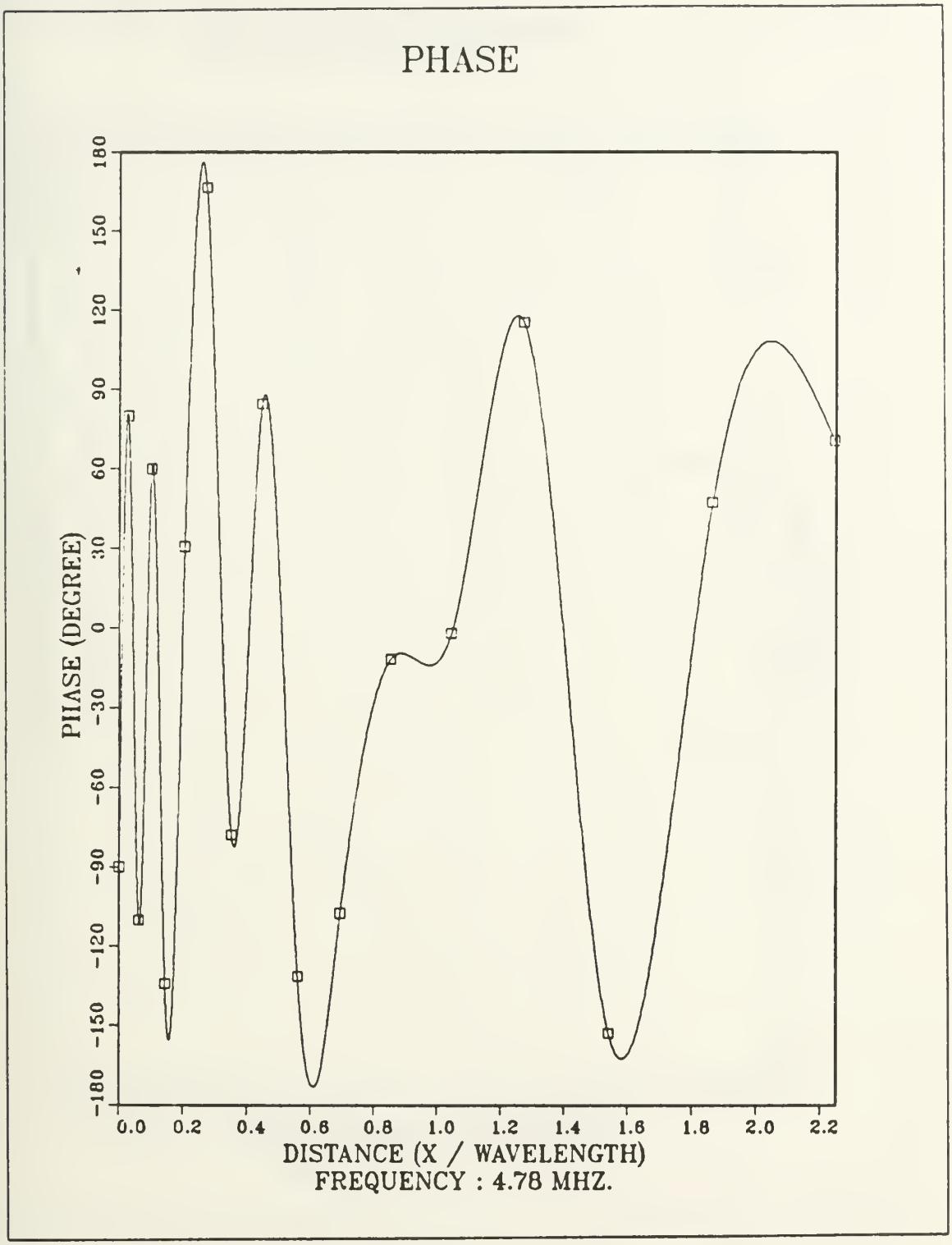

Figure F.12 Current Phase, Frequency : 4.78 MHz.

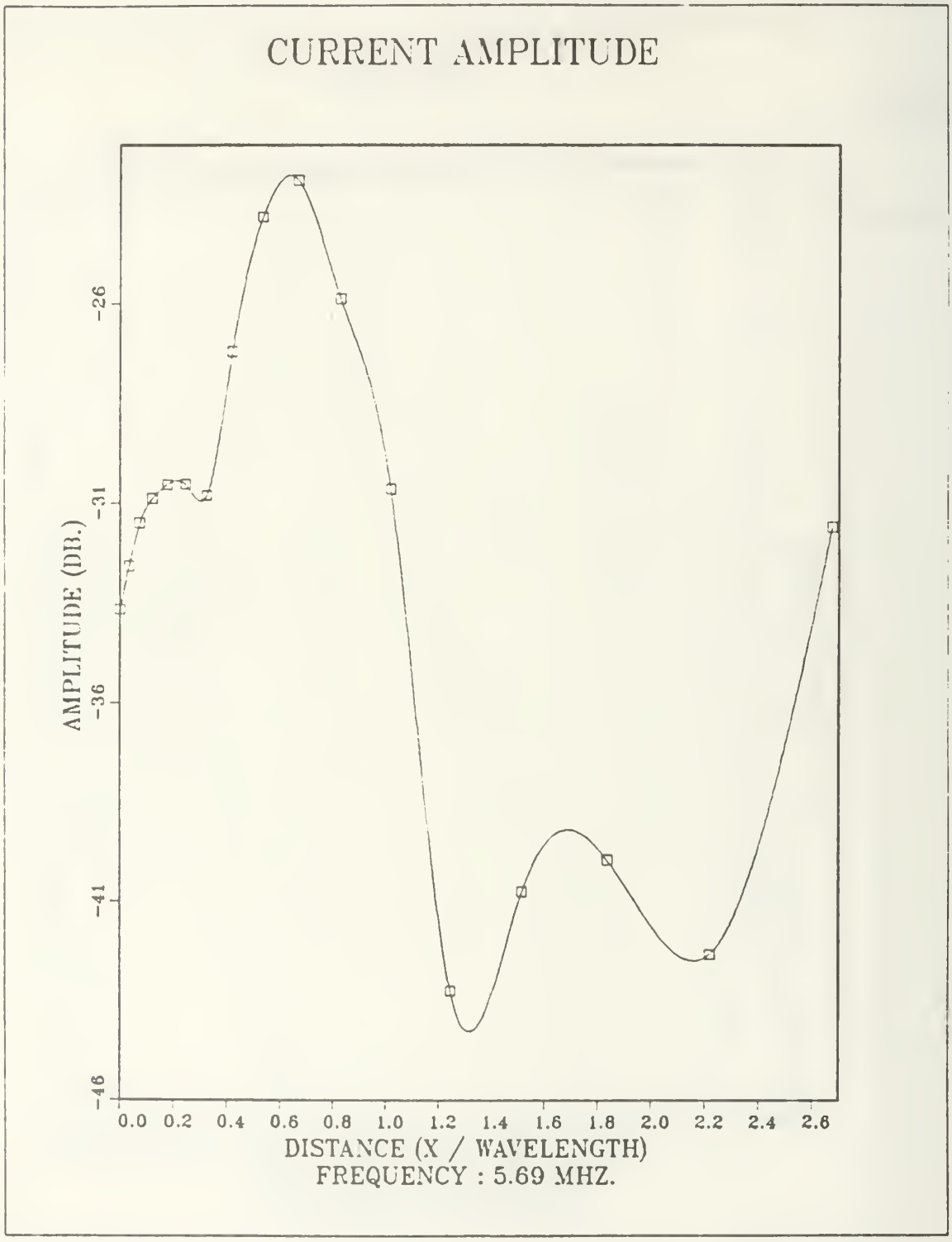

Figure F.13 Current Amplitude, Frequency : 5.69 MHz.

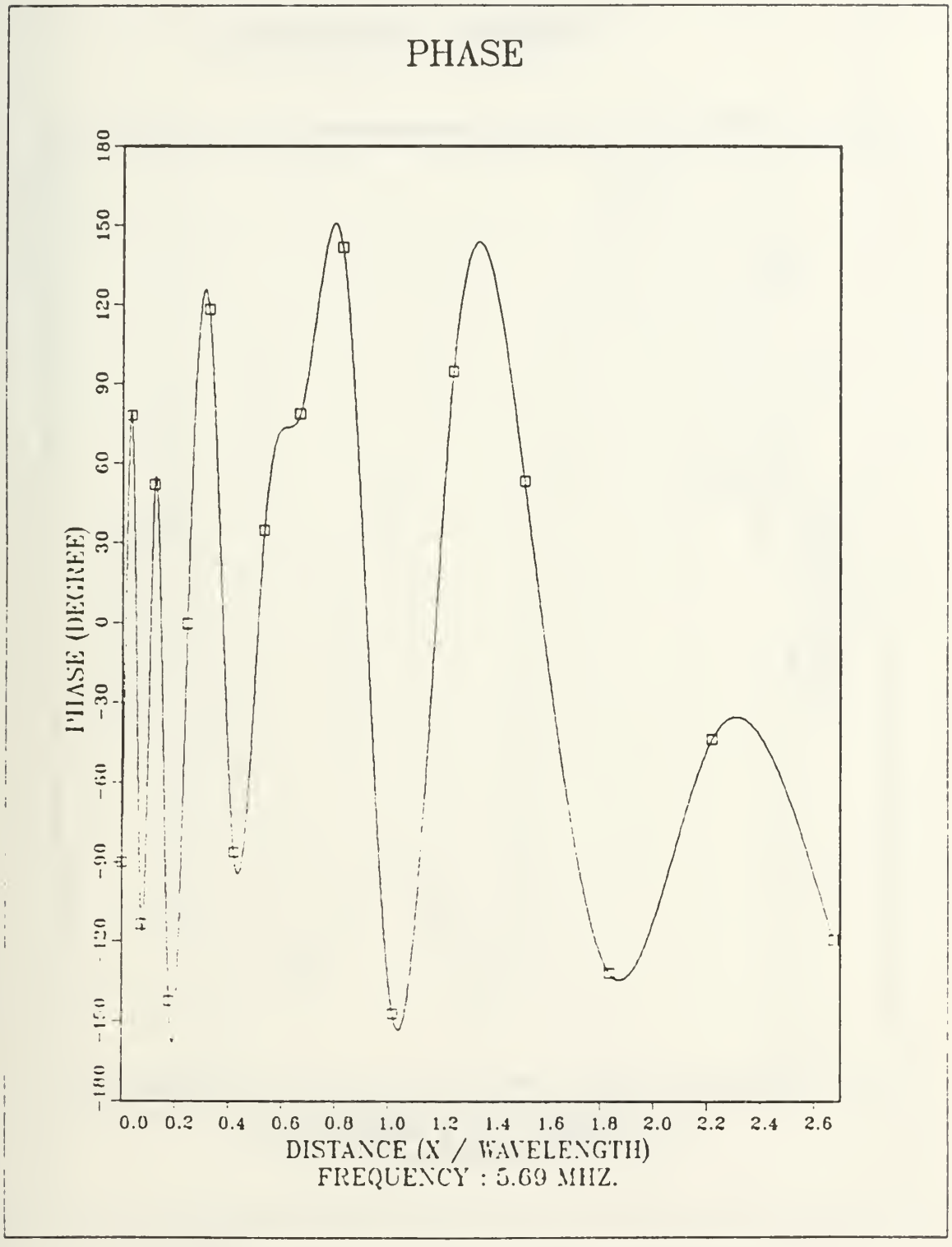

Figure F.14 Current Phase, Frequency : 5.69 MHz.

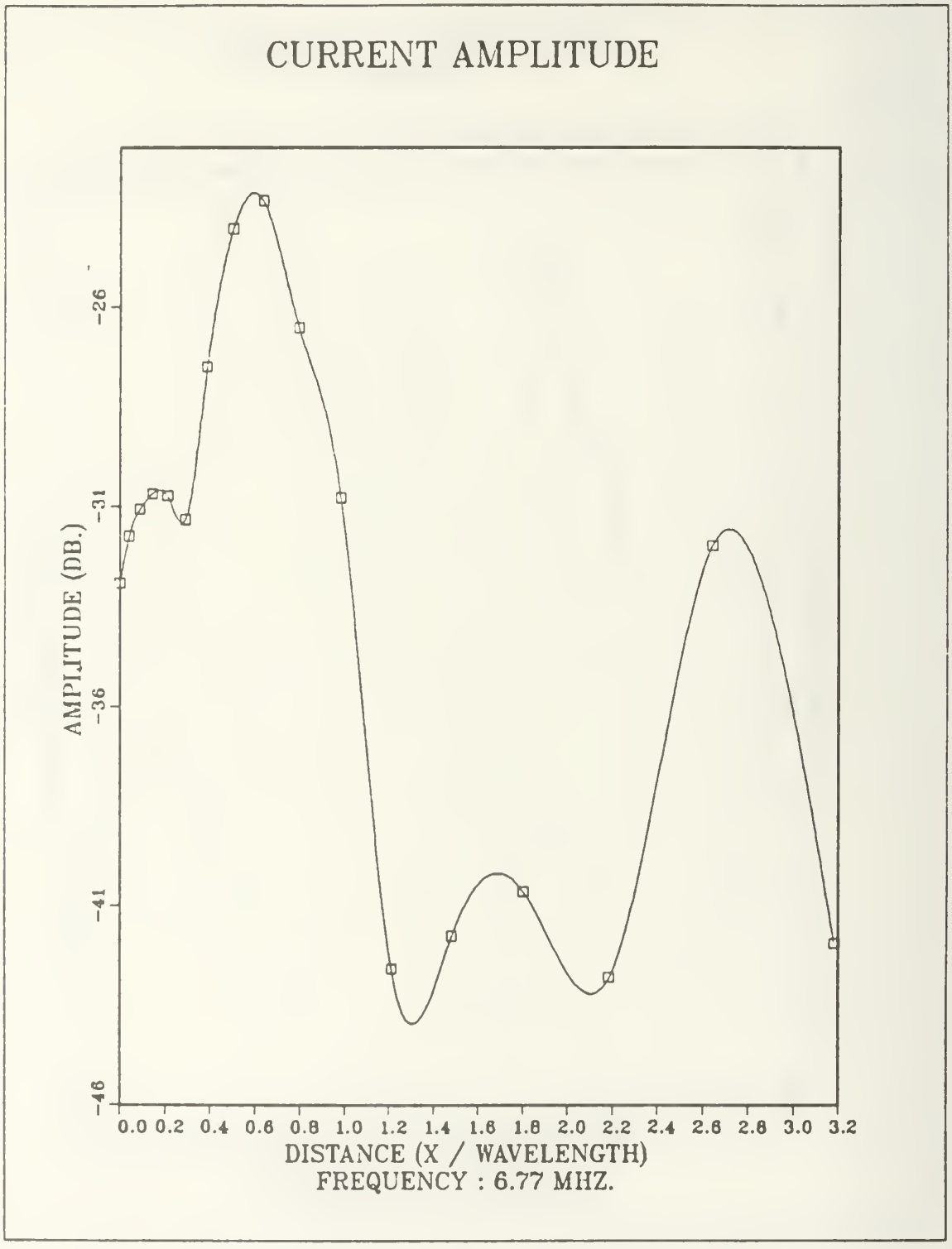

Figure F.15 Current Amplitude, Frequency : 6.77 MHz.

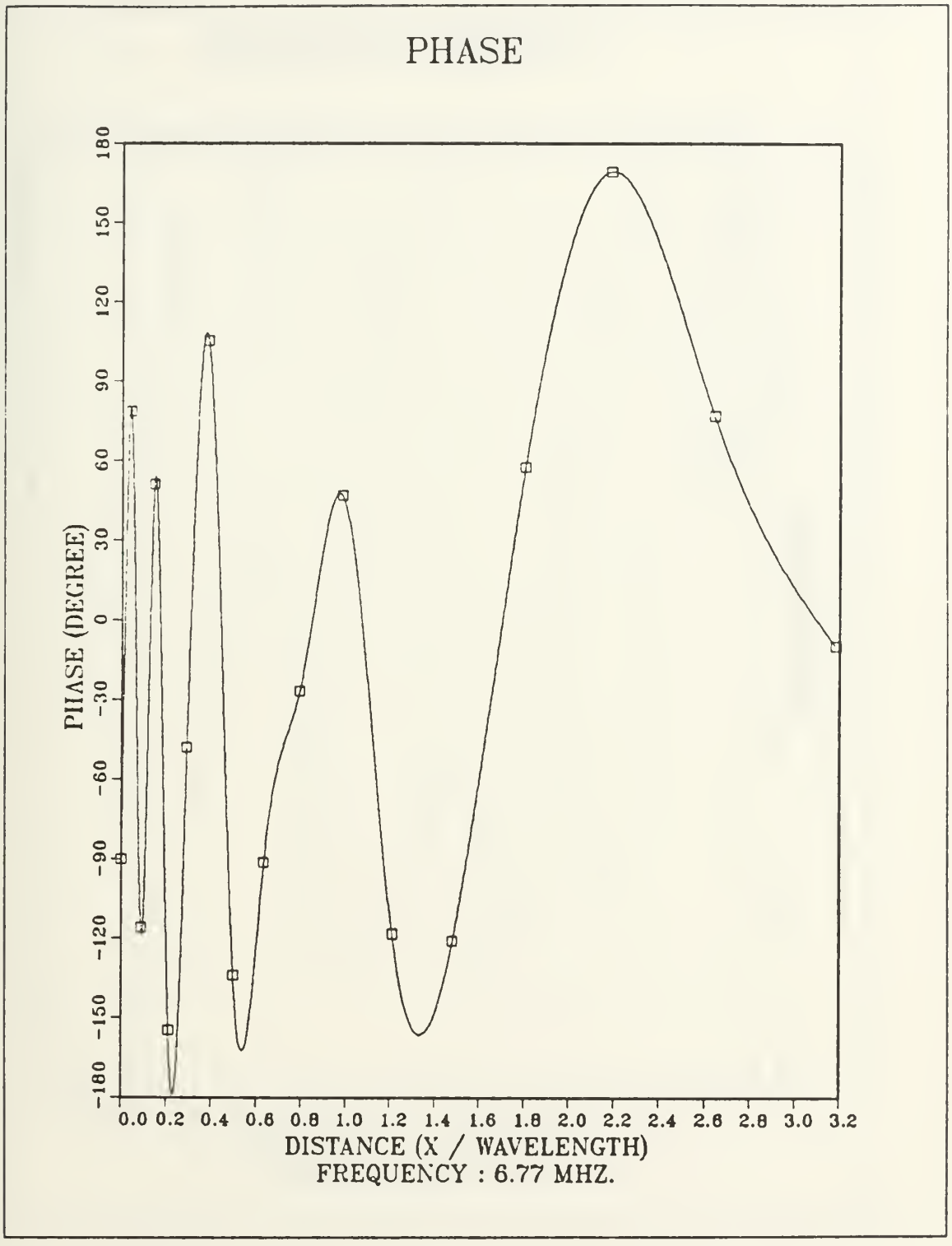

Figure F.16 Current Phase, Frequency : 6.77 MHz.

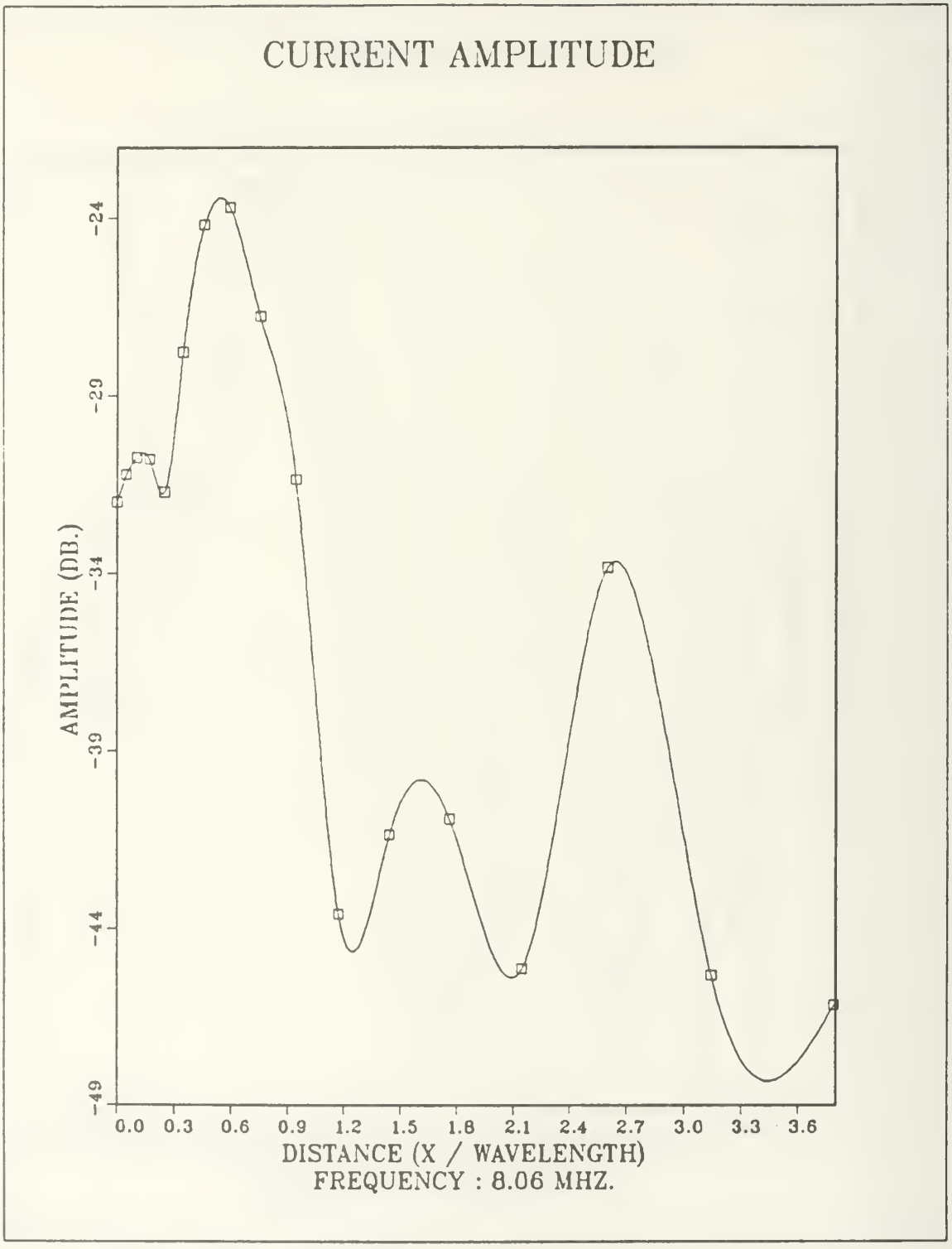

Figure F.17 Current Amplitude, Frequency : 8.06 MHz.

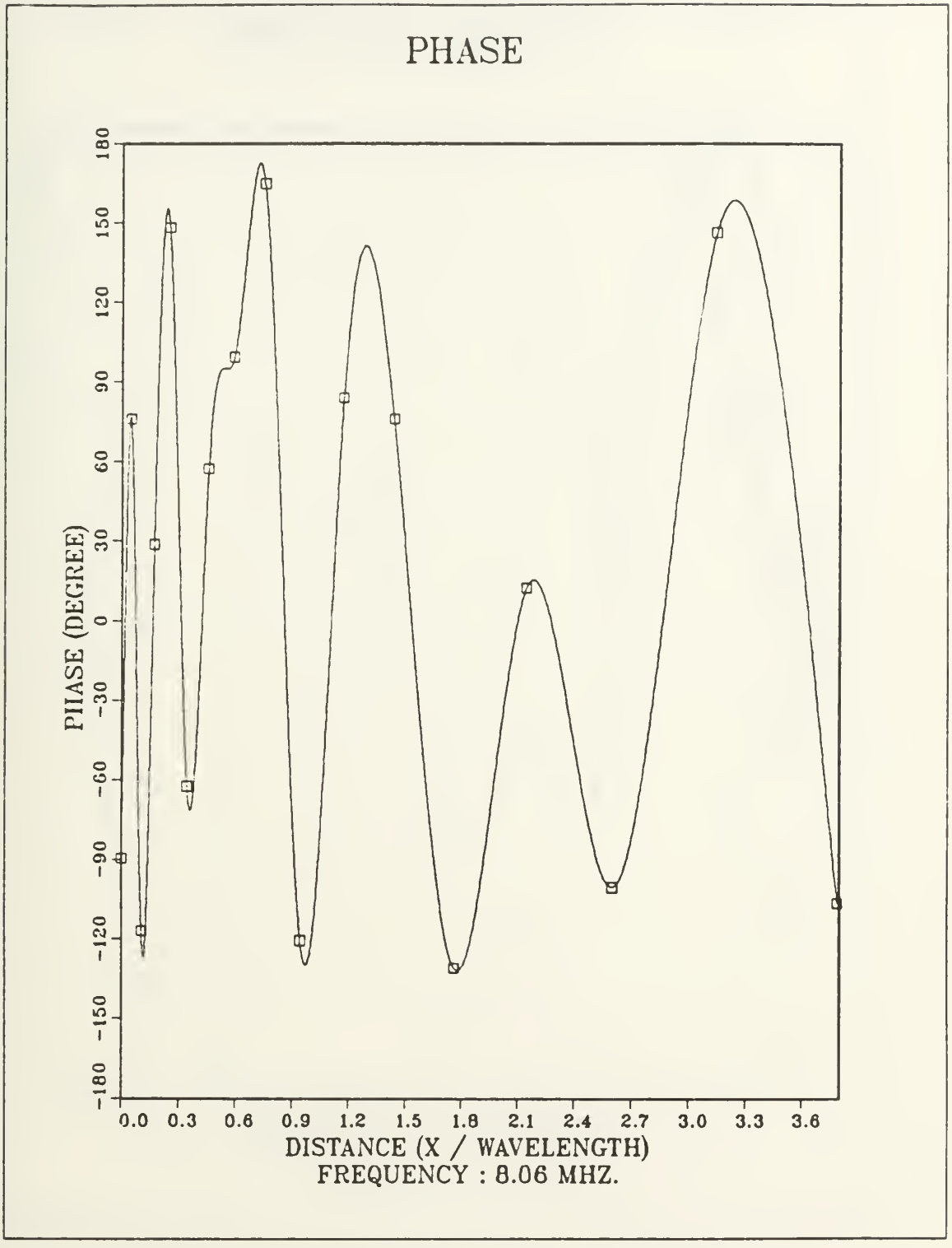

Figure F.18 Current Phase, Frequency : 8.06 MHz.

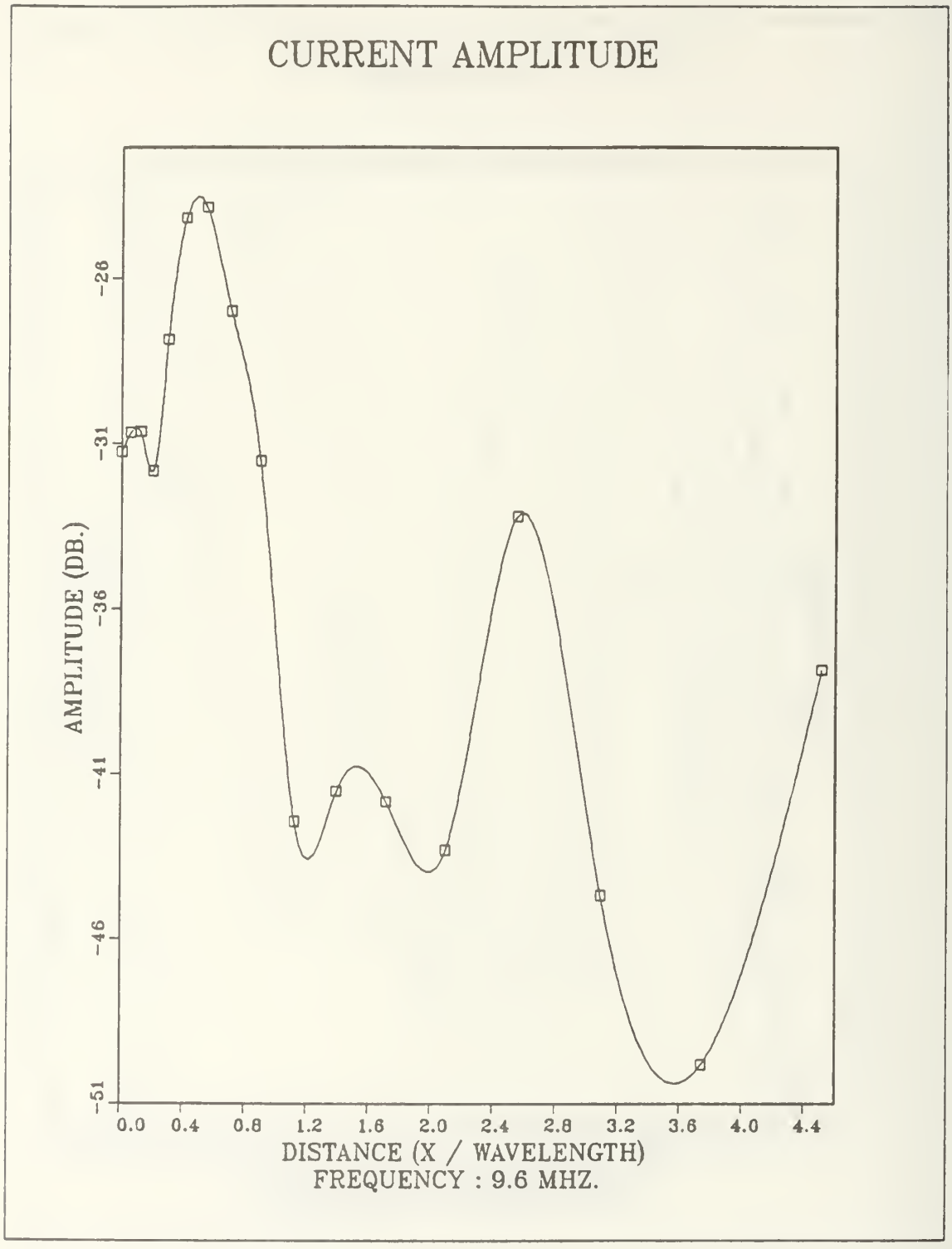

Figure F.19 Current Amplitude, Frequency : 9.6 MHz.

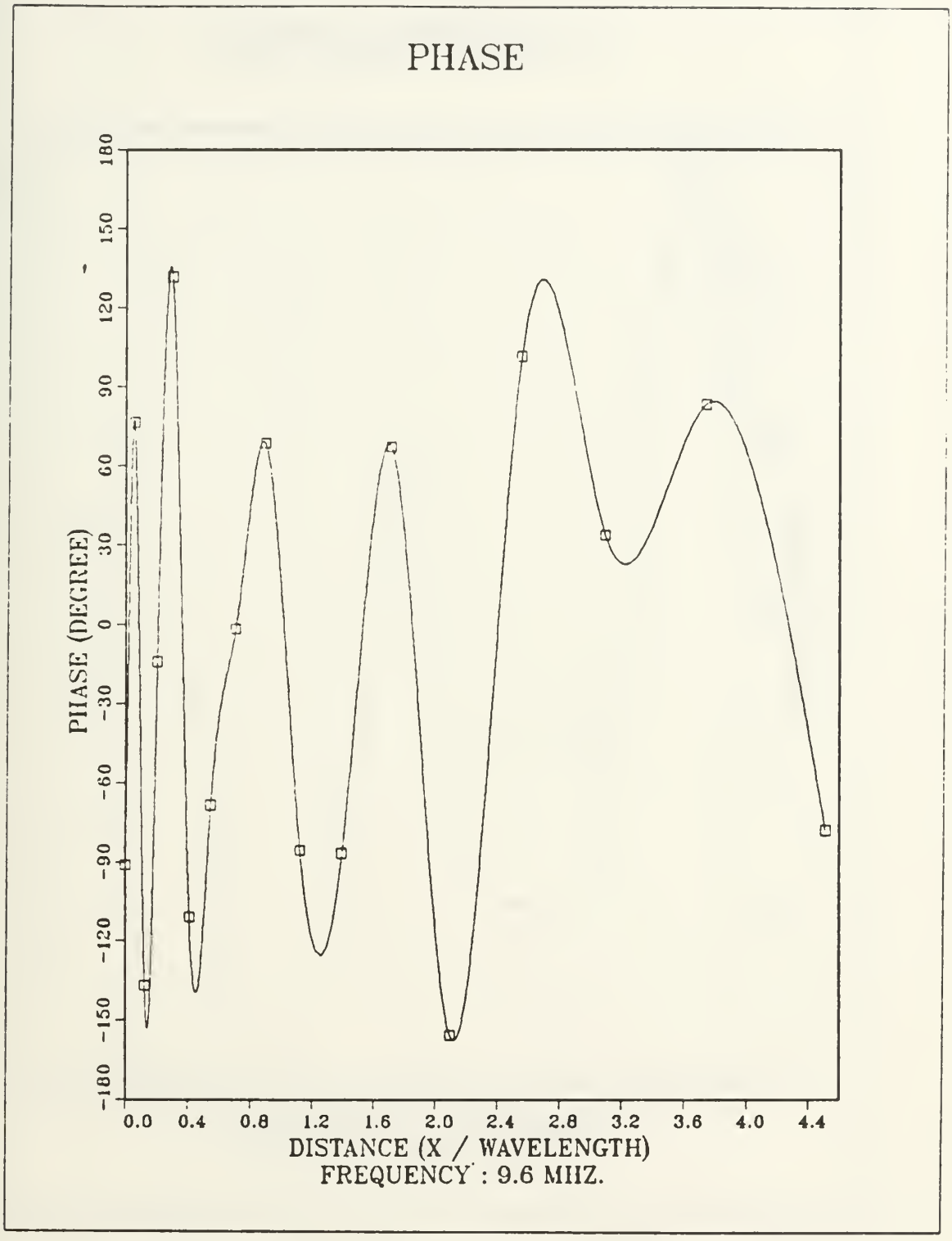

Figure F.20 Current Phase, Frequency : 9.6 MHz.

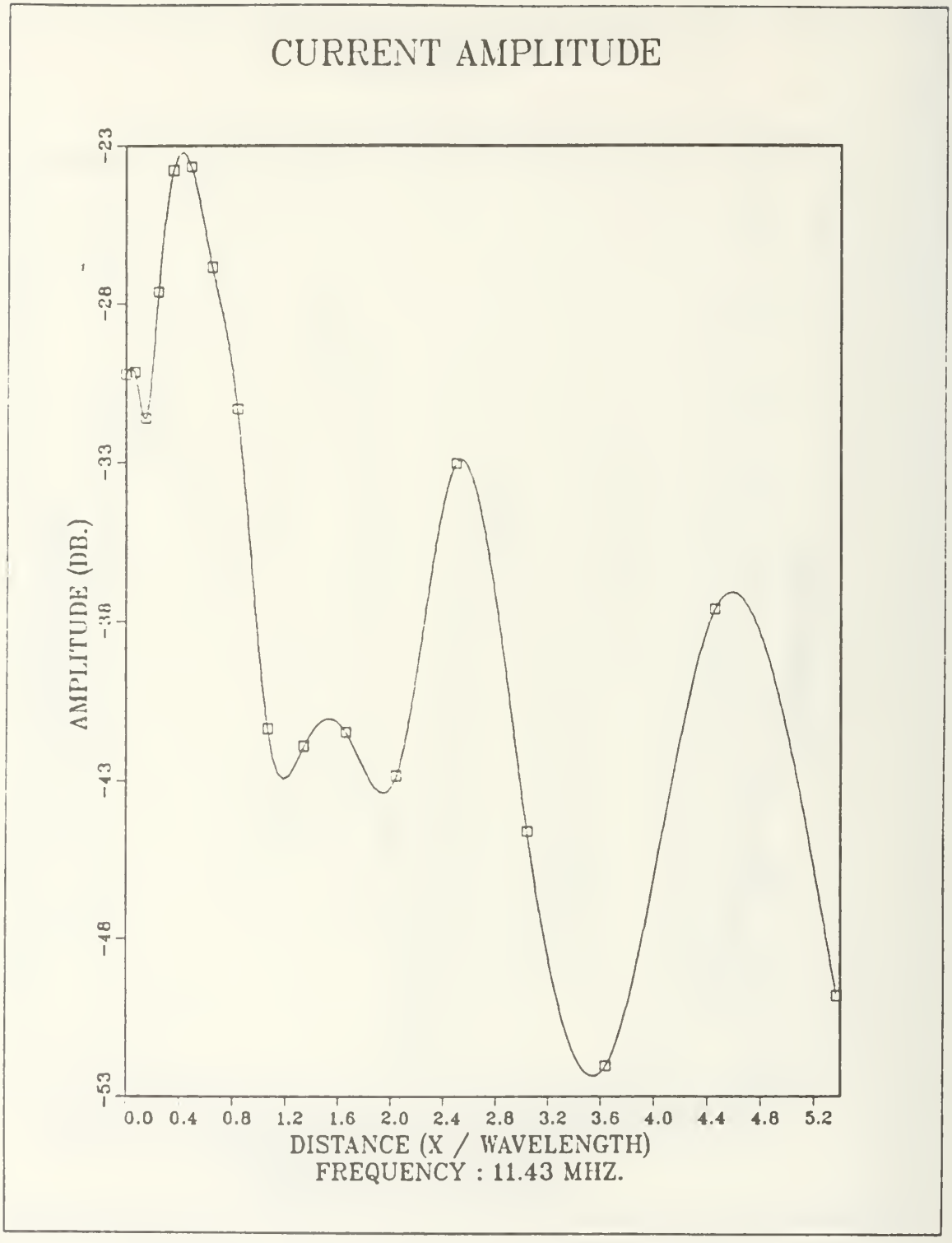

Figure F.21 Current Amplitude, Frequency : 11.43 MHz.

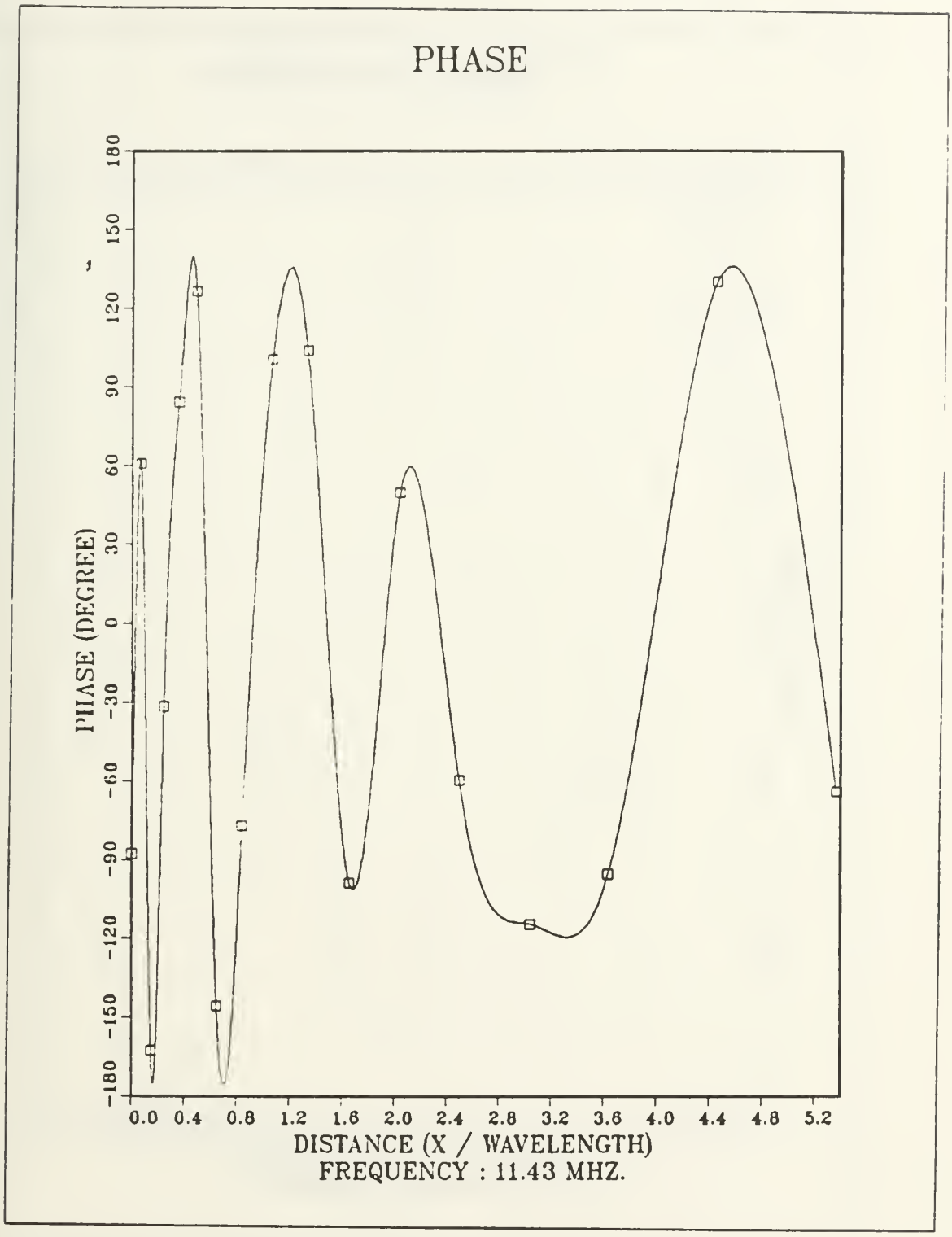

Figure F.22 Current Phase, Frequency : 11.43 MHz.

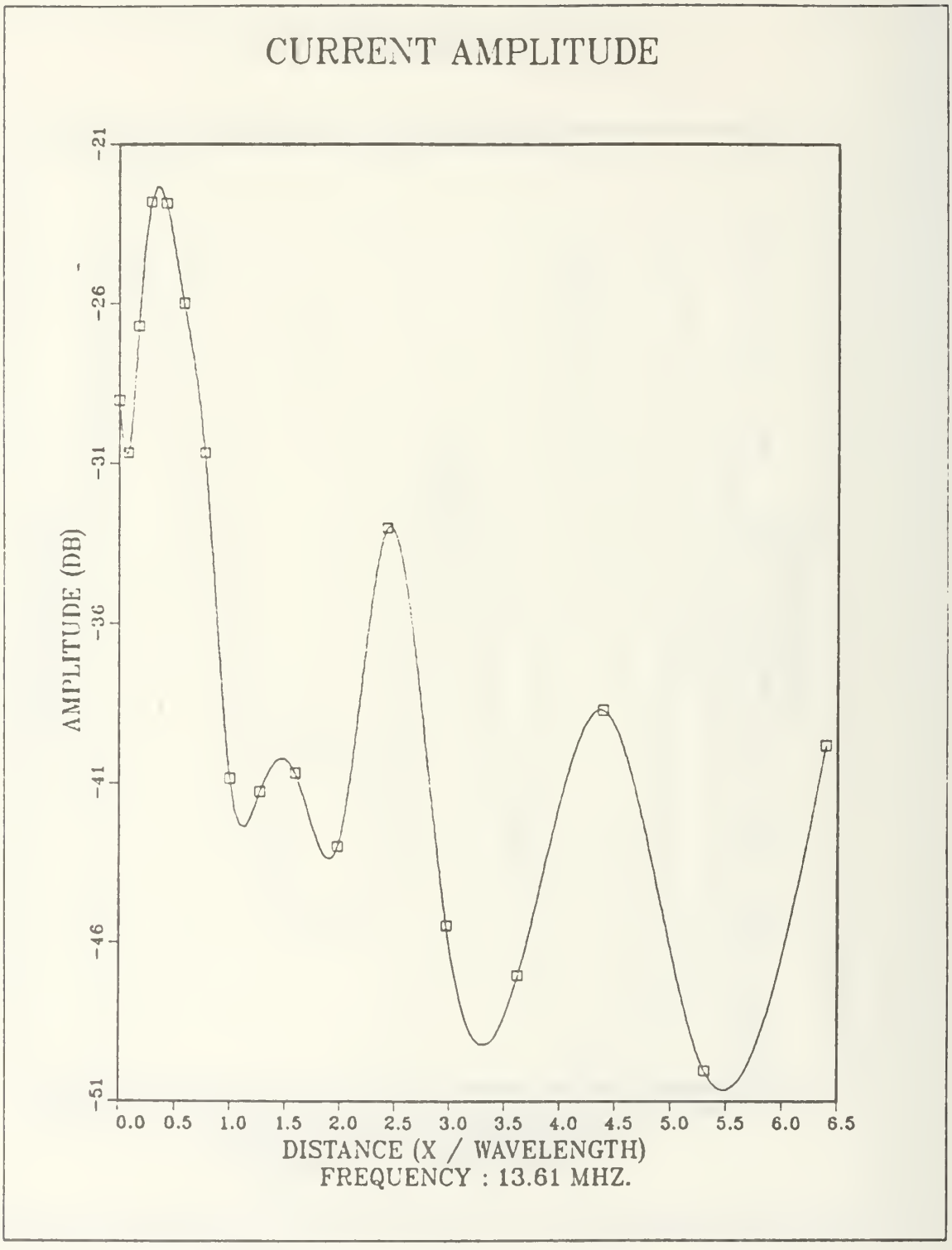

Figure F.23 Current Amplitude, Frequency : 13.61 MHz.

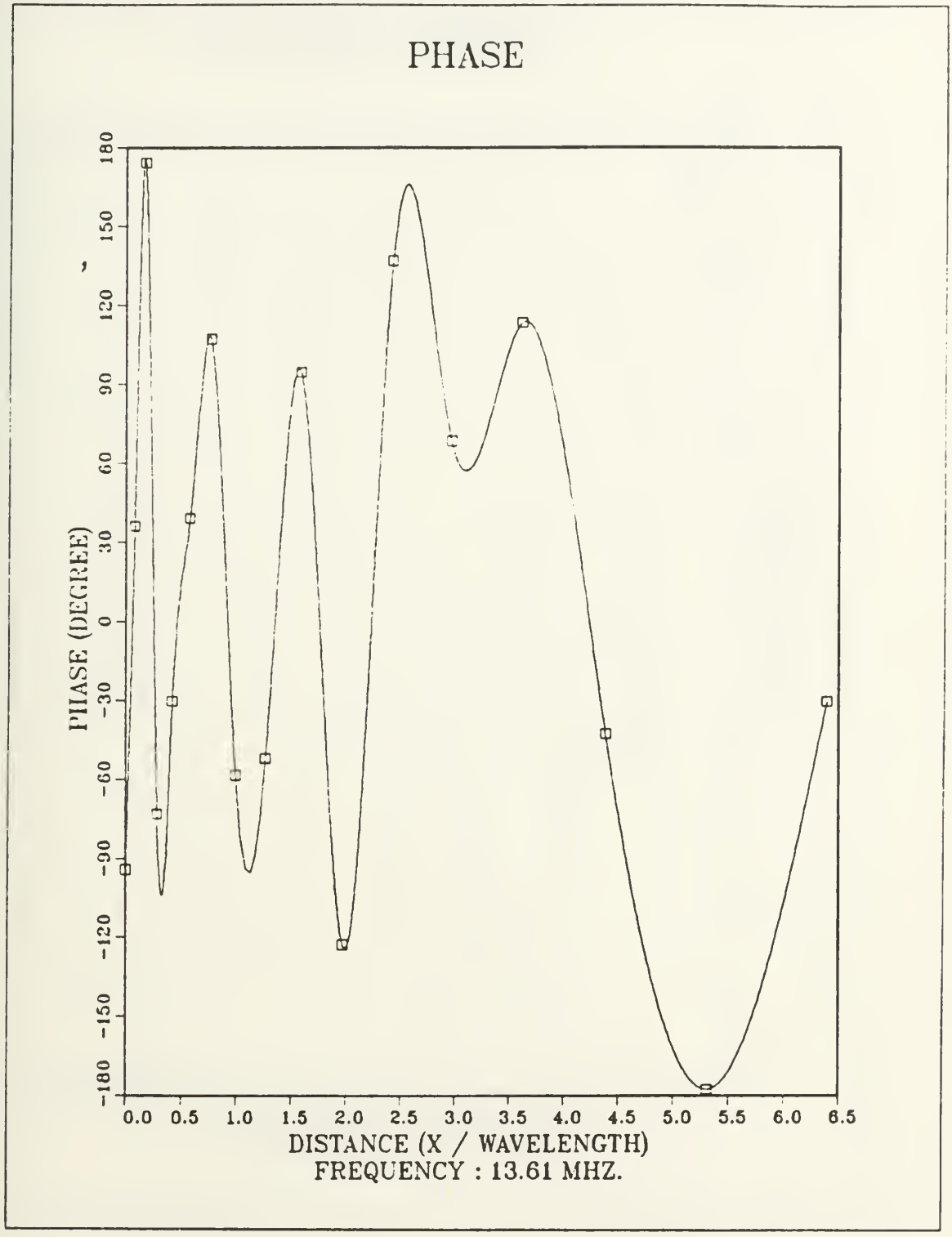

Figure F.24 Current Phase, Frequency : 13.61 MHz.

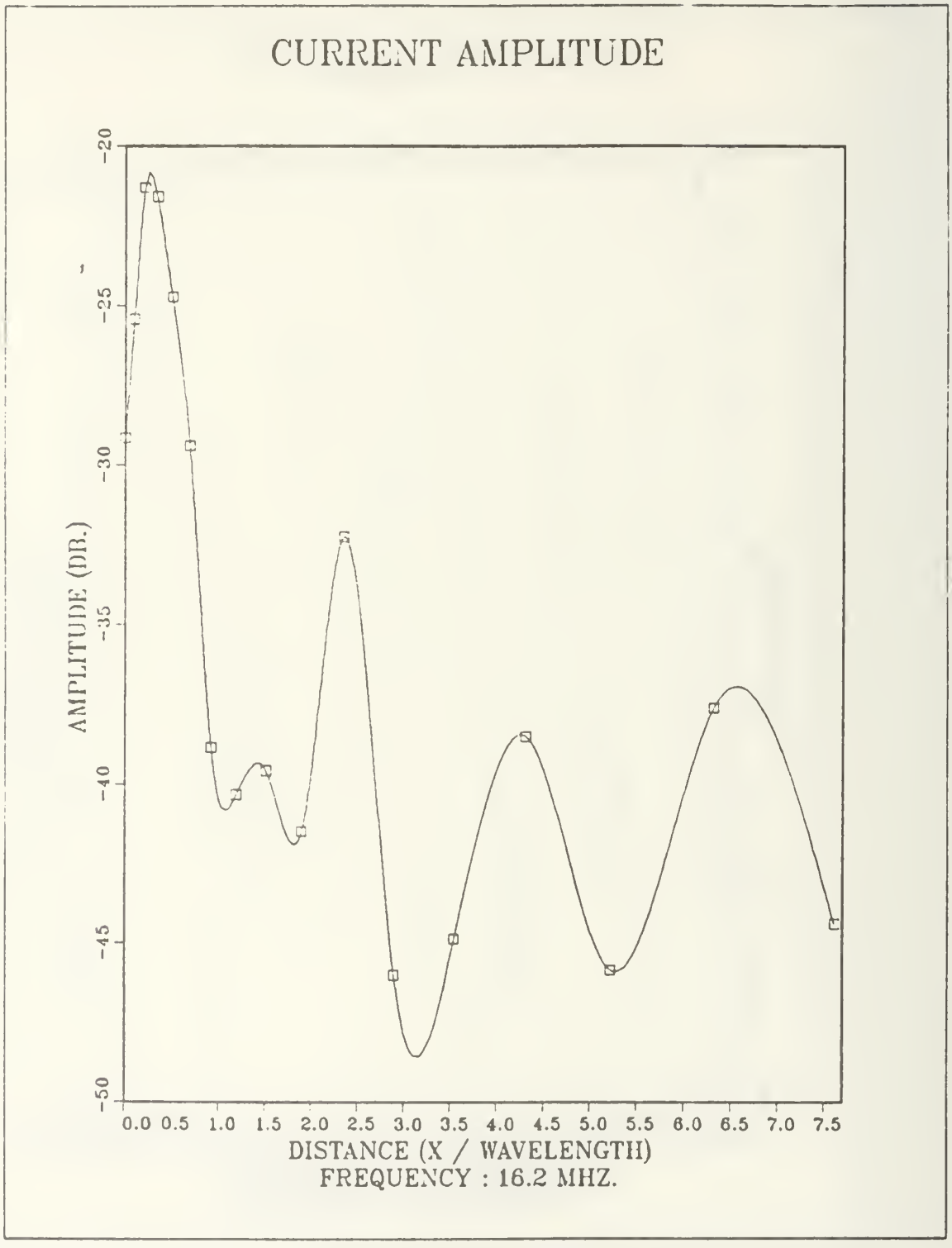

Figure F.25 Current Amplitude, Frequency : 16.2 MHz.

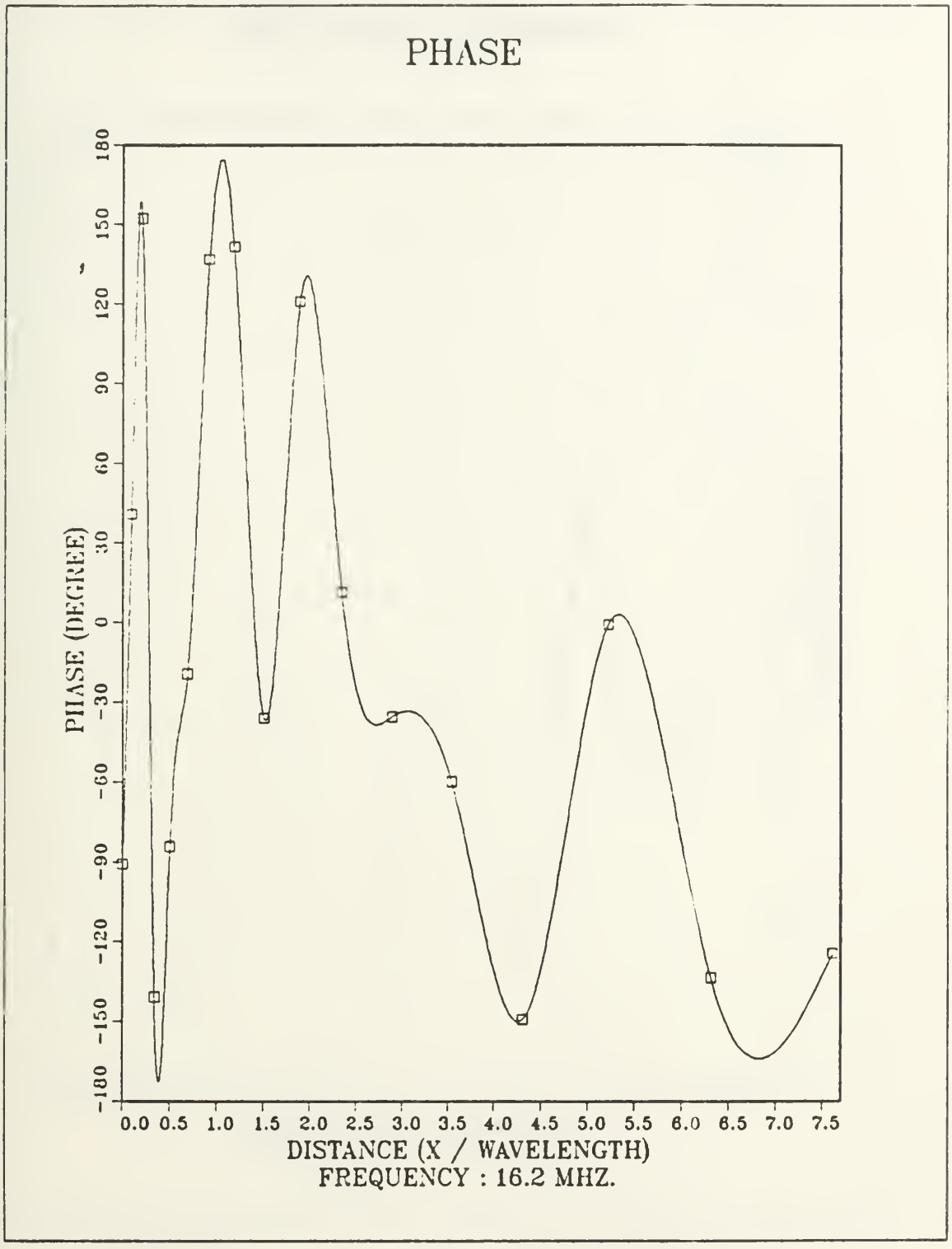

Figure F.26 Current Phase, Frequency : 16.2 MHz.

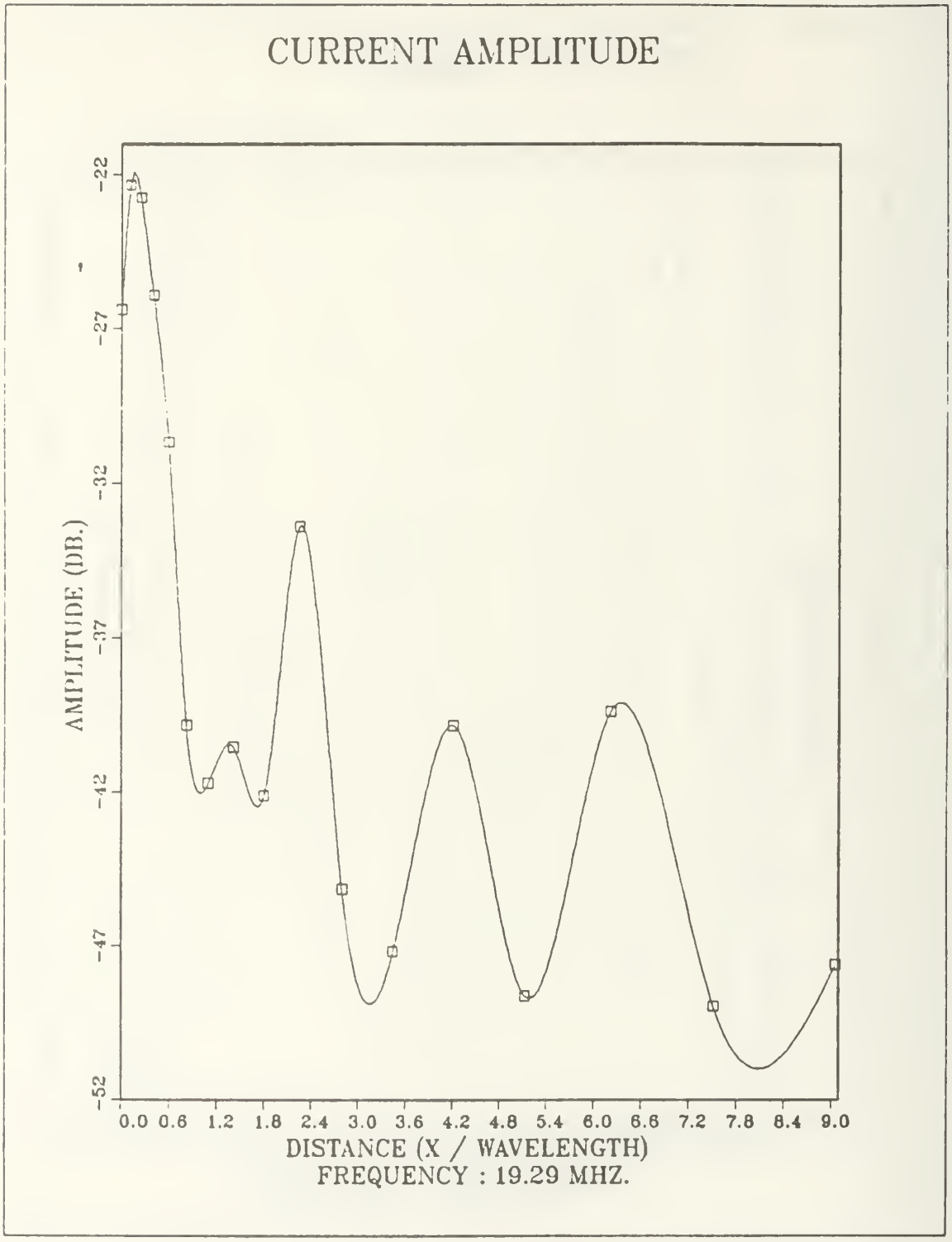

Figure F.27 Current Amplitude, Frequency : 19.29 MHz.

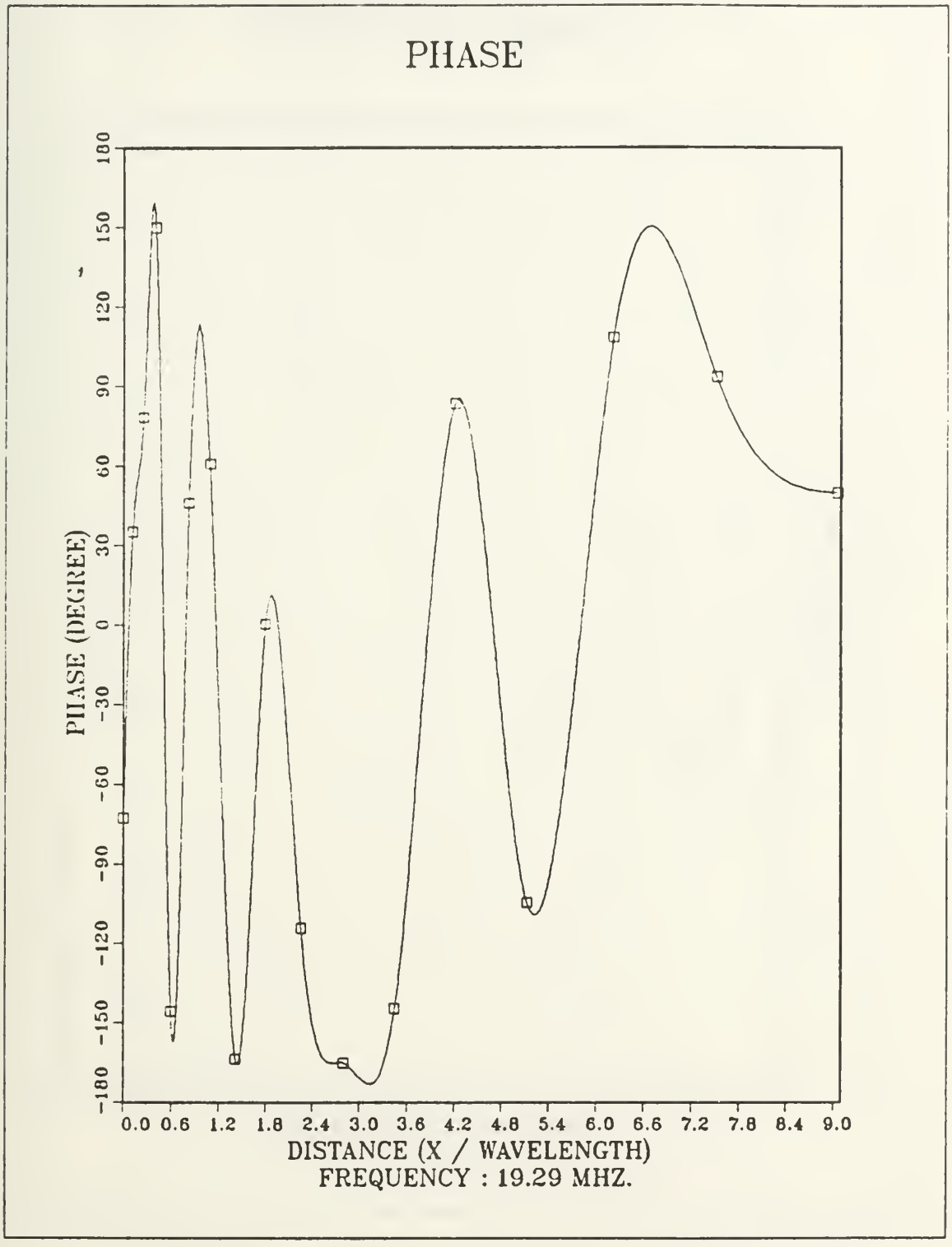

Figure F.28 Current Phase, Frequency : 19.29 MHz.

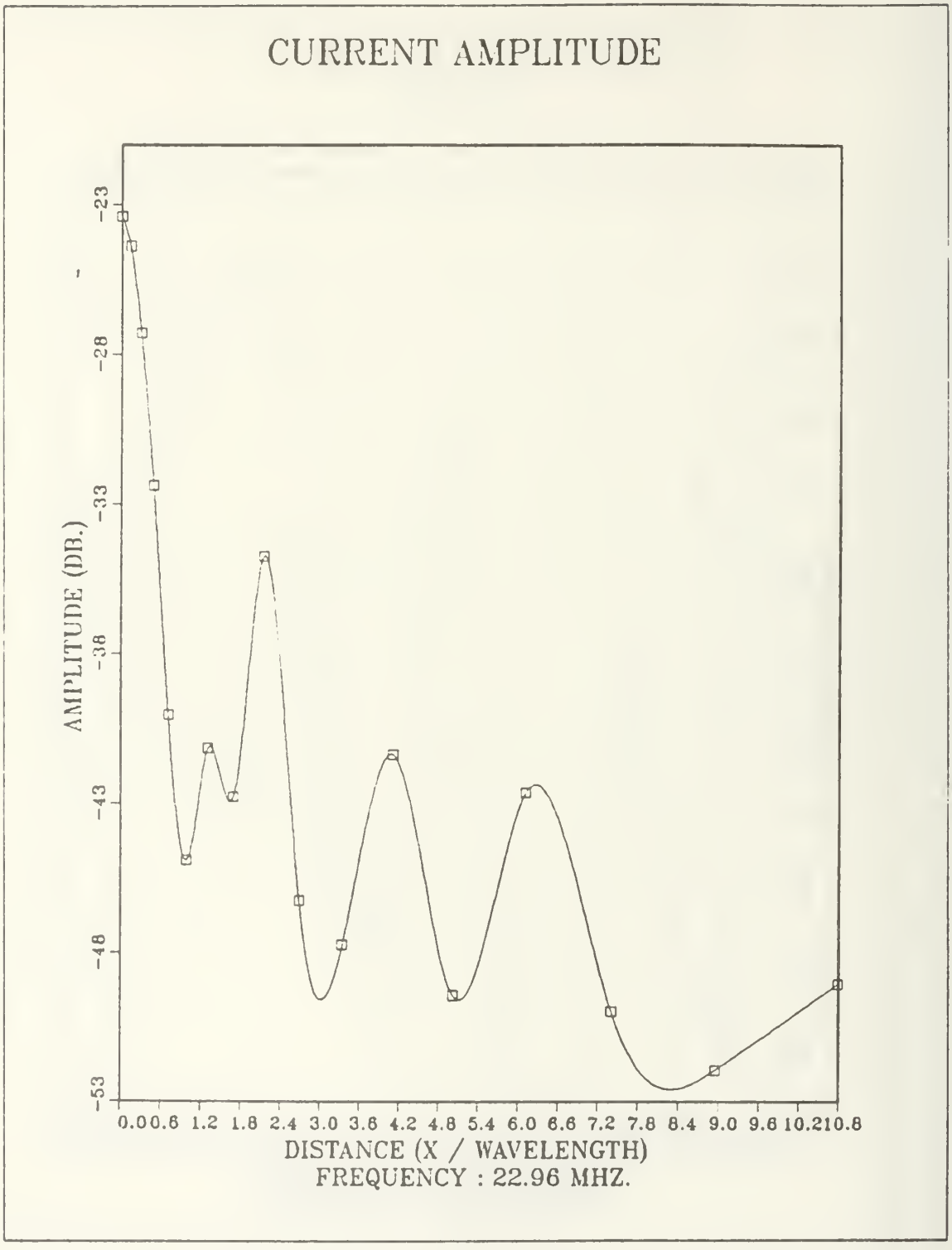

Figure F.29 Current Amplitude, Frequency : 22.96 MHz.

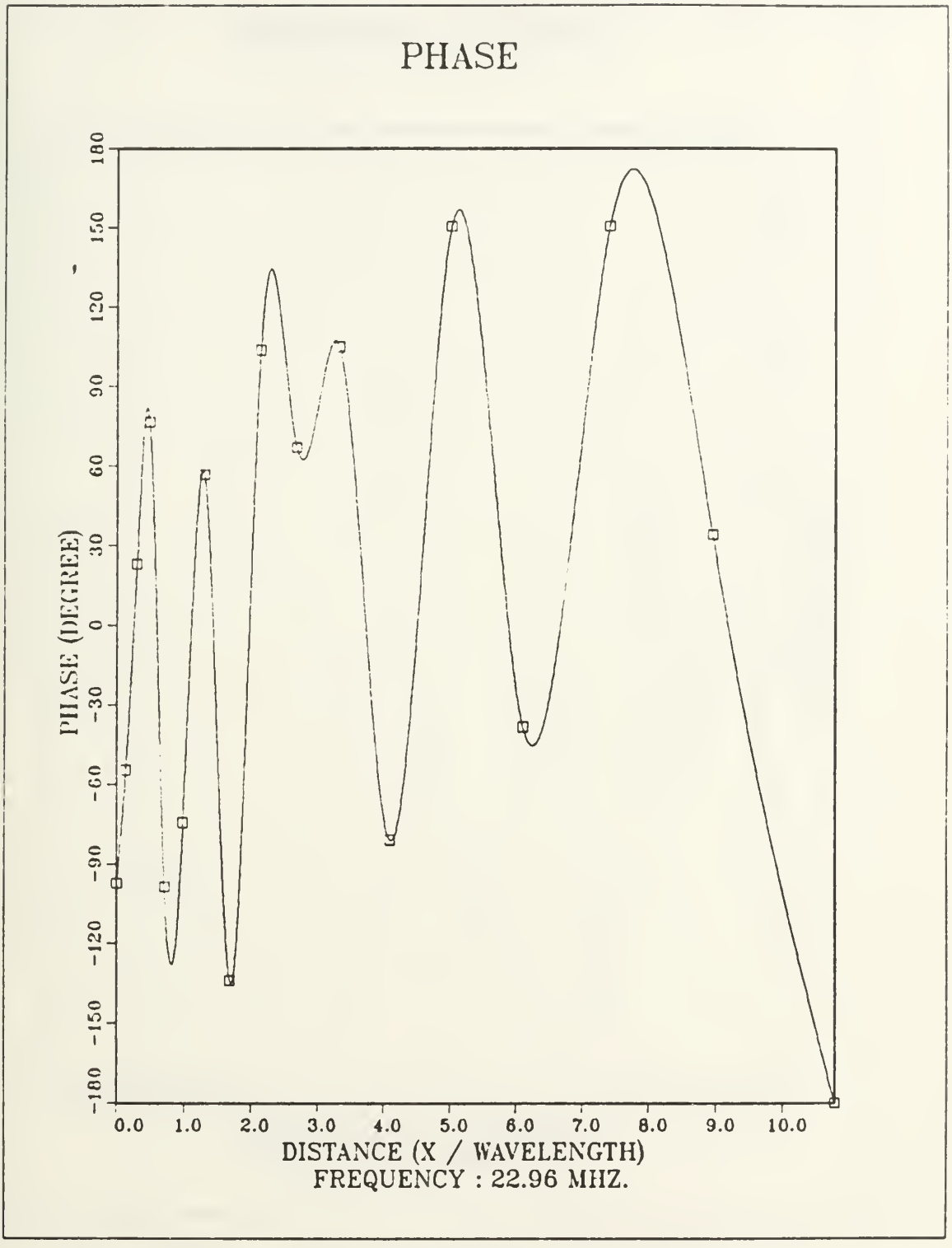

Figure F.30 Current Phase, Frequency : 22.96 MHz.

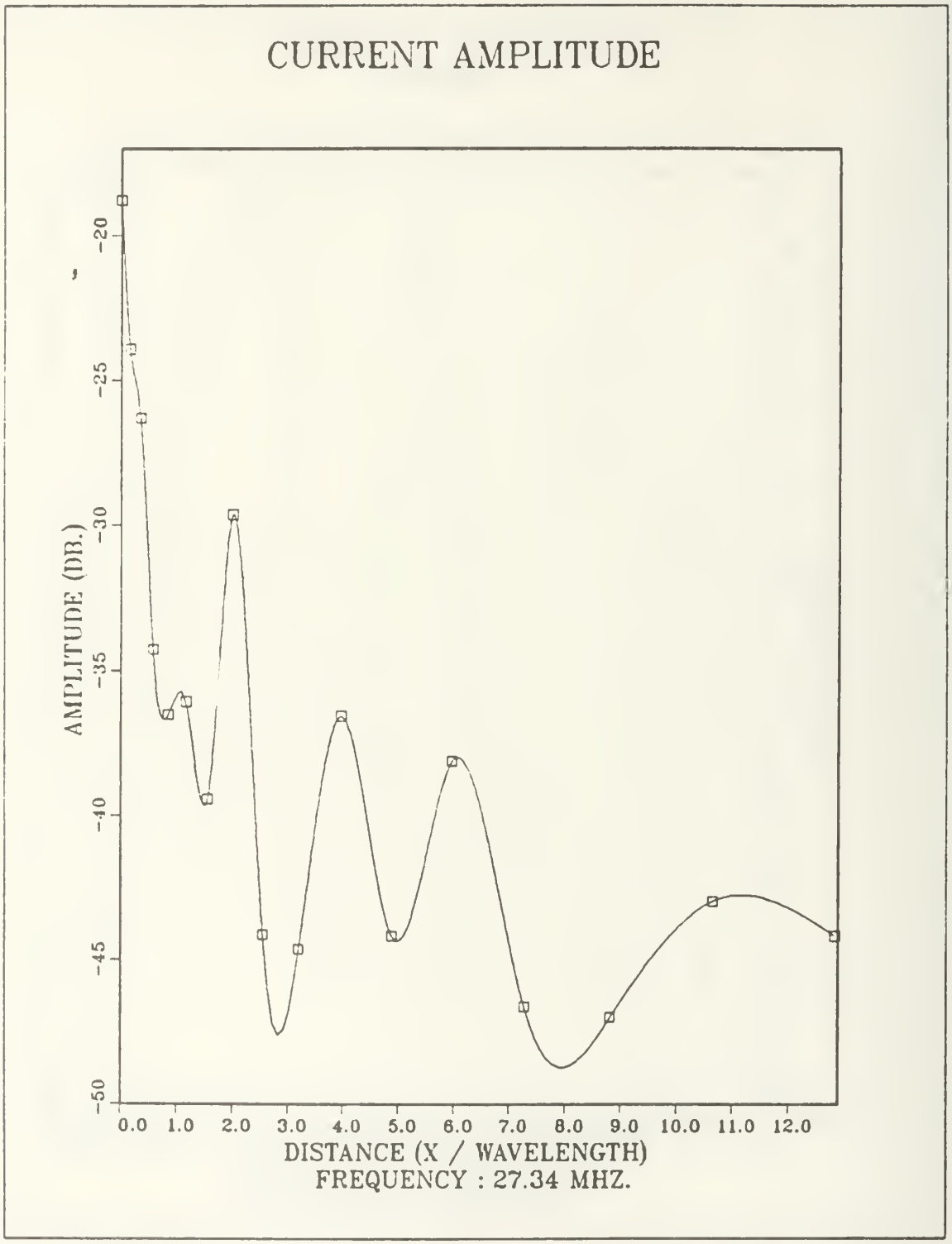

Figure F.31 Current Amplitude, Frequency : 27.34 MHz.

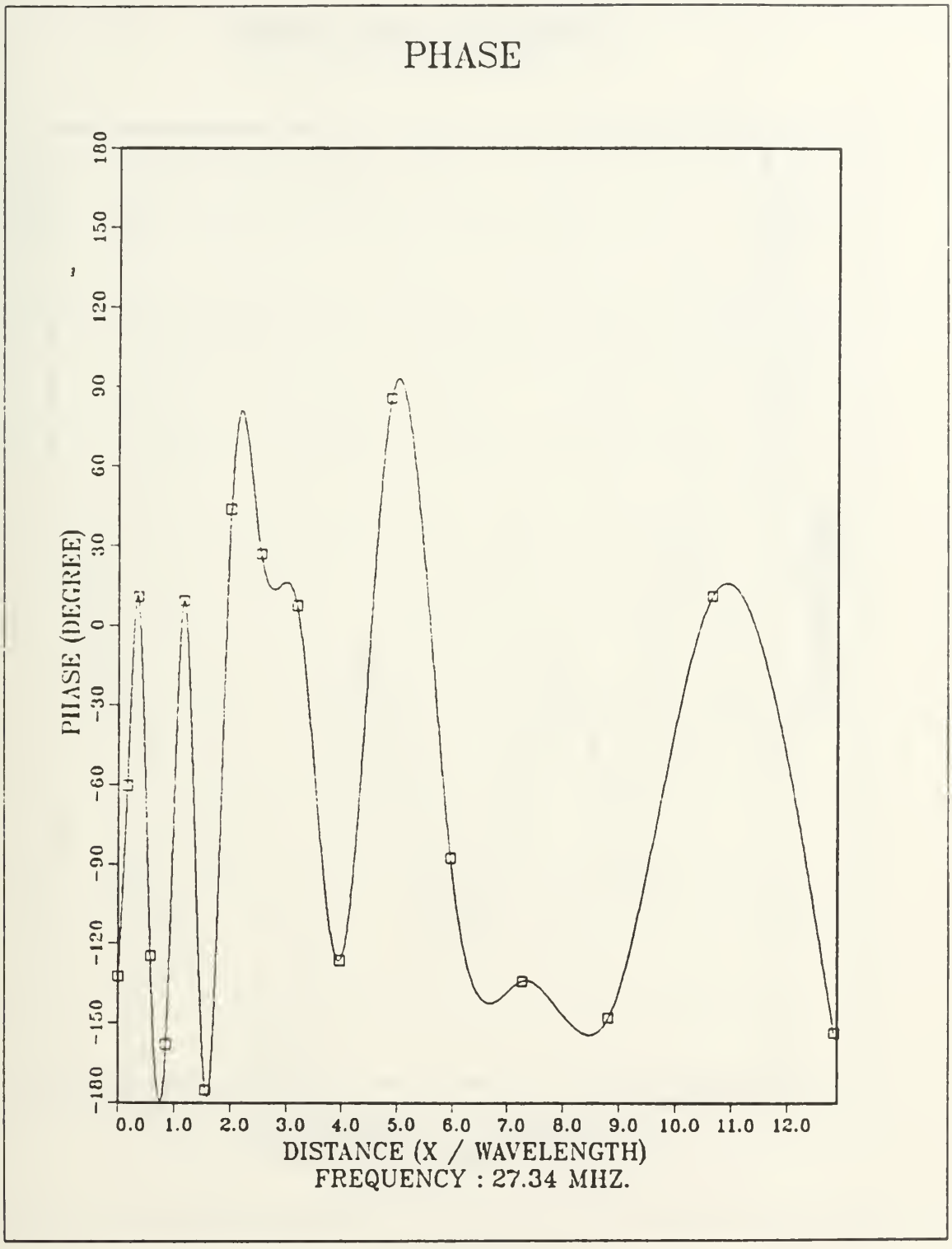

Figure F.32 Current Phase, Frequency : 27.34 MHz.

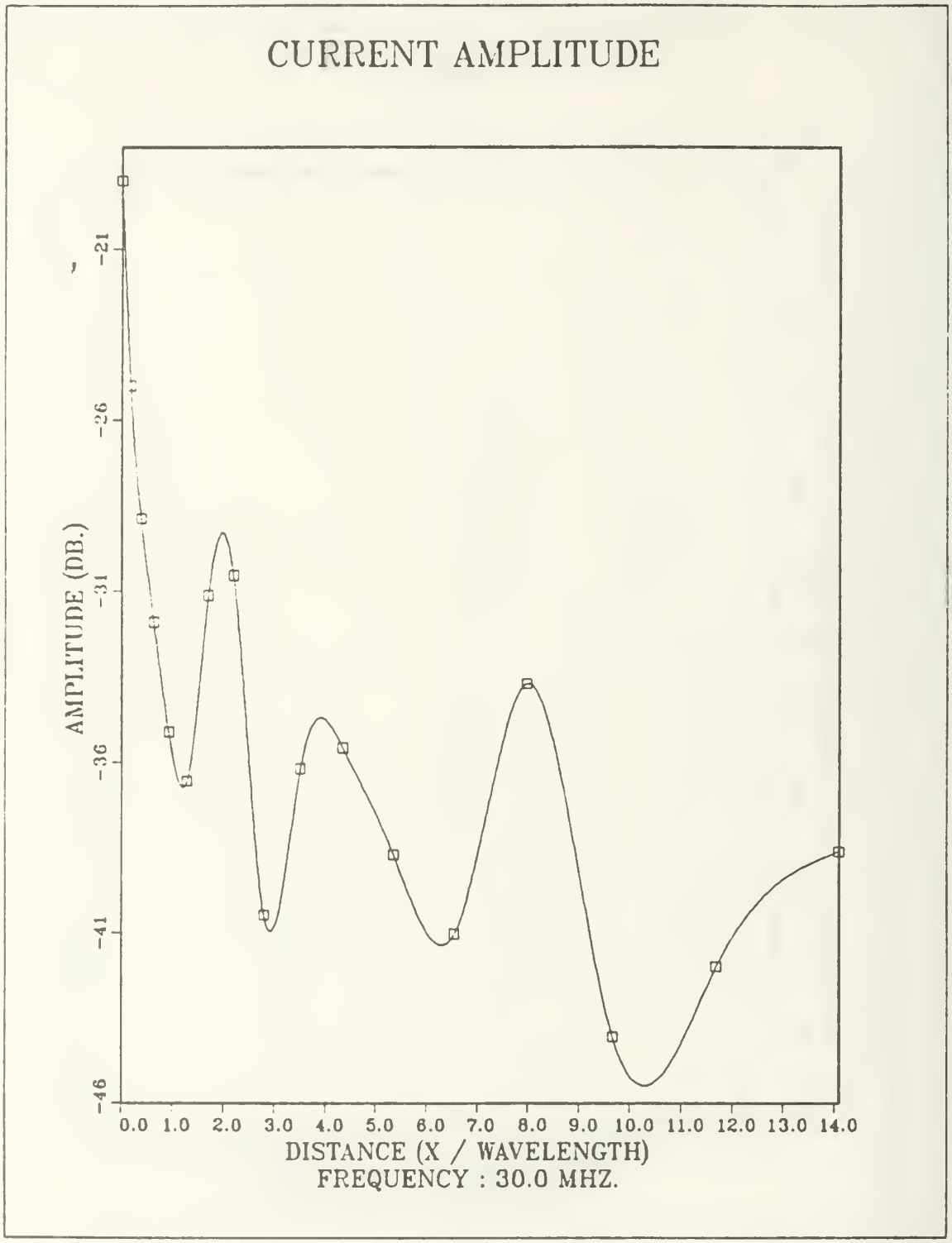

Figure F.33 Current Amplitude, Frequency : 30.0 MHz.

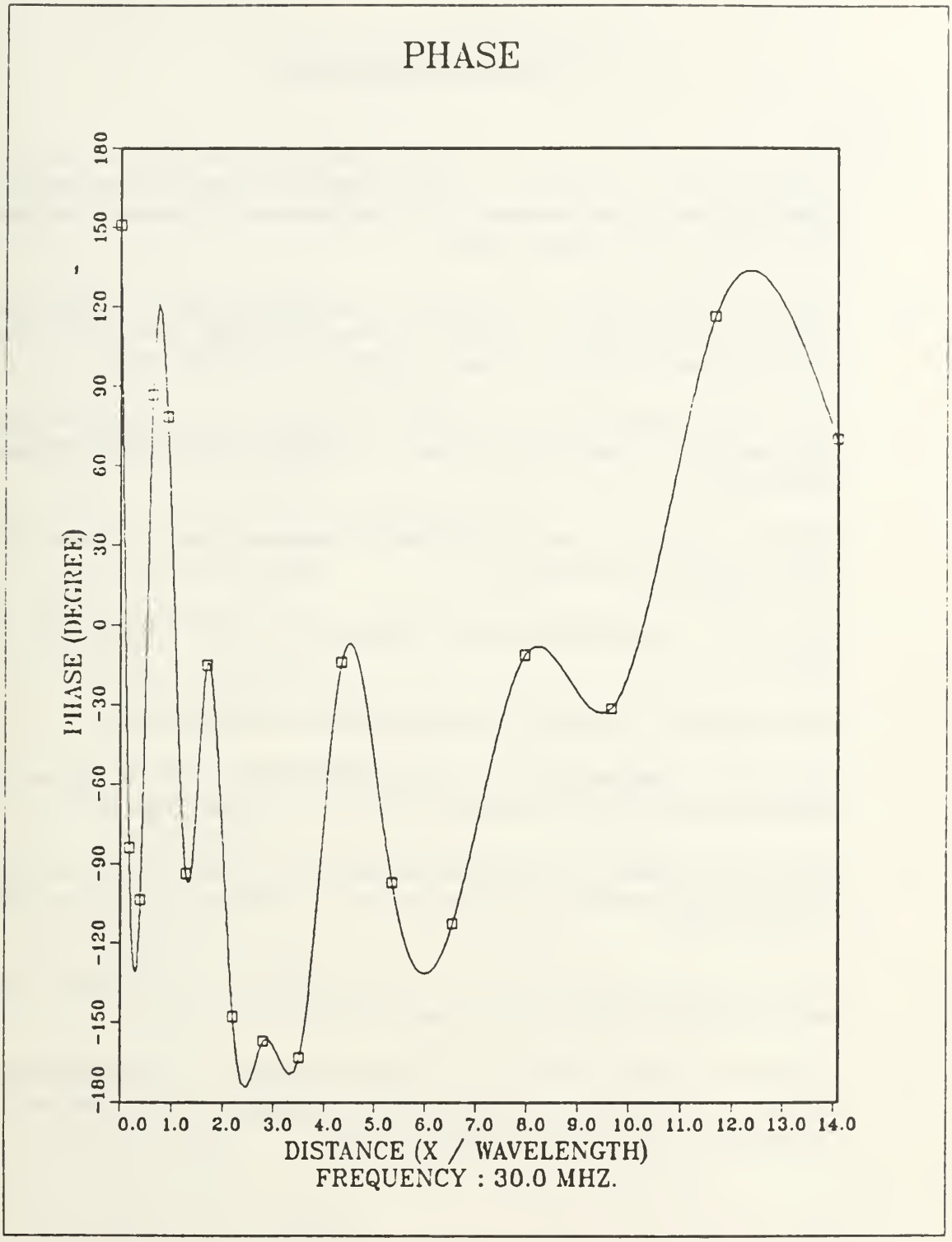

Figure F.34 Current Phase, Frequency : 30.0 MHz.

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